

11-1-2012

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Recommended Citation

Sankle, R. and Singh, J.R. (2012) "Single Sampling Plans for Variables Indexed by AQL and AOQL with Measurement Error," *Journal of Modern Applied Statistical Methods*: Vol. 11 : Iss. 2 , Article 12.

DOI: 10.22237/jmasm/1351743060

Available at: <http://digitalcommons.wayne.edu/jmasm/vol11/iss2/12>

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Single Sampling Plans for Variables Indexed by AQL and AOQL with Measurement Error

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Single sampling plans are investigated for variables indexed by acceptable quality level (AQL) and average outgoing quality limit (AOQL) under measurement error. Procedures and tables are provided for selection of single sampling plans for variables for given AQL and AOQL when rejected lots are 100% inspected for replacement of a nonconforming unit. For a particular sampling plan in operation for an observed measurement, a method for determining true operating characteristic (OC) functions and average outgoing quality (AOQ) is described for various error sizes.

Key words: Measurement error, AQL, AOQL.

Introduction

One difficulty with production processes is achieving a desired quality level of manufactured product while maintaining economy in production cost. Statistical techniques have been successfully applied to address this problem; to employ statistical techniques, inspections are conducted on intermediate and finished products. In every inspection system, there is always a possibility for error in accepting a non-conforming unit and rejecting a conforming unit. These errors, which are mainly due to chance, are termed inspection errors and they can be estimated. This is important because corrective action must be taken if the number of inspection errors is large. Jackson (1957) studied the effect of inspection errors on waste and on the quality of outgoing product assuming 100% inspection. Considering that error is a substantial part of observed variation, Diviney and David (1963)

investigated the relationship between measurement error and product acceptance.

The requirement that the measurement of an individual item does not exceed some specified limit is sometimes more important than the requirement that the mean and variability for the items be at or near some pre-determined value. An acceptance sampling plan in which a specified number of units is sampled from each lot, with the lot being accepted if less than a fixed number of non-conformance products are found in the sample, is one of the traditional statistical tools used for quality control. Lots that are not accepted can either be discarded or rectified. Rectification, that is, replacing or discarding all non-conforming units after 100% inspection of rejected lots, is frequently used when manufacturing costs are high.

Several authors have proposed predictors for estimating the number or rate of non-conformances in lots subjected to acceptance sampling (Hahn, 1986; Zaslavsky, 1988; Brush, et al. 1990; Martz & Zimmer, 1990). Greeberg and Stokes (1992) used the information obtained in rectification to devise a more efficient predictor than those previously proposed. Greenberg and Stockes (1995) also considered an application of quality control in which the test procedure is imperfect. Two problems may exist in acceptance sampling. Devices that are classified as non-conforming may be conforming (false positive) and devices

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that are classified as conforming may be non-conforming (false negative). Johnson, et al. (1991) provided expressions and tables of the average outgoing quality for many types of sampling plans when the false positive and false negative rates are known. Lindsay (1985) described methods for estimating the probability of false positives and false negatives and the rates and numbers of non-conformances when a sample is repeatedly inspected. However, these authors do not consider plans with rectification.

A lot-by-lot rectification inspection scheme for a series of lots calls for 100% inspection of rejected lots under the application of a sampling plan. If it is preferable to use a single sampling plan for variables under a rectification inspection scheme, the index for the selection of the sampling plan will be the average outgoing quality limit (AOQL), which is the worst average quality the consumer will receive in the long run, regardless of the incoming quality. Rejected lots are often a nuisance to the producers because they result in extra work and extra cost. If too many lots are rejected the reputation of the producer or supplier may be damaged. From the producer's point of view, it is preferable to fix an acceptable quality level (AQL) by designing a sampling plan such that, if the incoming product quality is maintained at AQL most of the lots, for example 95%, will be accepted during the sampling inspection stage. Thus, designing sampling inspection plans indexed by AQL and AOQL satisfies both the producer and consumer whenever rectifying inspection is necessary. The predictors are generally assumed to be measured without error, but this is often not the case.

To identify the parameter in the model, the following assumptions are made concerning measurement errors. First, it is assumed that the true values and the measurement errors are uncorrelated and that the mean of the measurement errors is zero. Second, the measurement errors are assumed to be normally distributed with zero mean and a constant known variance. Third, the true values are assumed to be normally distributed with a mean estimated by the mean of the observed values and a variance estimated using the reliability of the observed values. The reliability of a variable measured with error is the ratio of the variance

of the true values to the variance of the observed values; the closer this ratio is to 1 the more reliable the measurement. The reliability can be provided by reliability coefficients (Hand, 2004). Alternatively, a range of plausible reliabilities can be explored to carry out a sensitivity analysis of the results to estimate the severity of the unobserved measurement error.

This study examines single sampling plans for variables indexed by AQL and AOQL under measurement error. Procedures and tables are provided for selecting single sampling plans for variables for given AQL and AOQL when rejected lots are 100% inspected for replacement of nonconforming units. For a particular sampling plan in operation for observed measurement, a method of determining the OC function and AOQ curves is described for various errors sizes.

Model description for Variable Single Sampling Plan indexed by AQL and AOQL under Measurement Errors:

Consider the distribution of the true quality characteristics x to be normal with mean μ and known standard deviation σ_p . The density function is:

$$f(x) = \frac{1}{\sigma_p} \Phi \left(\frac{x - \mu}{\sigma_p} \right), \quad (2.1)$$

where $\Phi(x)$ is the standardized normal probability density function given by

$$\Phi(x) = \frac{1}{\sqrt{2\pi}} e^{-\frac{1}{2}x^2}. \quad (2.2)$$

The mean and standard deviation of the observed measurement ($X = x + e$) can be written as

$$E(X) = E(x) + E(e) = \mu$$

where μ is the mean of x and e is the random error at measurement and is independent of x , and

$$V(X) = V(x) + V(e) = \sigma_p^2 + \sigma_e^2 = \sigma_X^2.$$

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The correlation coefficient ρ between the true and observed measurement is given by

$$\begin{aligned}\rho &= \frac{E\{(x-\mu)(X-\mu)\}}{\sigma_p\sigma_X} \\ &= \frac{E\{(x-\mu)^2 + (x-\mu)e\}}{\sigma_p\sigma_X}.\end{aligned}$$

Noting that x and e are independent, $E(e) = 0$ and $E(x) = \mu$, it can be shown that

$$\begin{aligned}\rho &= \frac{\sigma_p^2}{\sigma_p\sigma_X} \\ &= \frac{\sigma_p}{\sigma_X}.\end{aligned}\tag{2.3}$$

The relation between the size of measurement error r and correlation coefficient ρ is:

$$\rho = \frac{r}{\sqrt{1+r^2}}\tag{2.4}$$

where

$$r = \frac{\sigma_p}{\sigma_e}.$$

In referencing a single sampling variable plan when σ_p is known, the following symbols are used:

L: Lower specification limit;

U: Upper specification limit;

N: Sample size;

k : Acceptance parameter; and

\bar{x} : Sample mean

$$\Phi(y) = \int_{-\infty}^y \left(\frac{1}{\sqrt{2\pi}} \right) \exp\left(-\frac{1}{2}z^2\right) dz,\tag{2.5}$$

where $z \sim N(0,1)$.

The acceptance criterion for the single sampling plan is: For the upper specification limit, accept the lot if,

$$\bar{x} + k\sigma_p \leq U,\tag{2.6}$$

and, for the lower specification limit, accept the lot if

$$\bar{x} - k\sigma_p \geq L.\tag{2.7}$$

The fraction nonconforming in a given lot is

$$\Phi(-K_p) = p,\tag{2.8}$$

with

$$K_p = \frac{U - \mu}{\sigma_p}\tag{2.9}$$

where K_p is the p percent point of the standard normal distribution. If p is the proportion defective in the lot, then

$$U = \mu + K_p\sigma_p\tag{2.10}$$

and its probability of acceptance under measurement error will be

$$P_a(p) = \Phi(w),\tag{2.11}$$

with

$$w = (K_p - k) \frac{\sqrt{n}}{\rho}.\tag{2.12}$$

If the quality of the accepted lot is p and all non-conforming units found in the rejected lots are replaced by conforming units in a rectification inspection scheme, the AOQ can be approximated as

$$AOQ = p.P_a(p).\tag{2.13}$$

If p_m is the proportion non-conforming at which AOQ is maximum, then

$$AOQL = p_m.P_a(p_m).\tag{2.14}$$

If AQL (p_l) is prescribed, then the corresponding value of K_{AQL} or K_1 will be fixed, and if $P_a(p_l)$ is fixed at 95%, then, $w_{AQL} = w_1 = 1.645$; hence,

$$1.645 = (K_1 - k) \frac{\sqrt{n}}{\rho}, \quad (2.15)$$

so that for a given AQL, k is determined by the sample size n .

Results

Table 1 is used for selecting a single sampling variables plan under measurement errors for known σ case. For example, if the AQL is fixed at 1%, the AOQL is fixed at 1.25% and $r = 2, 4, 6$ and ∞ , Table 1 yields $n = 39, 27, 26$ and 25 , and $k = 1.989, 1.990, 1.992$ and 1.998 , respectively. It shows that, when the size of the error increases, the value of n increases and, due to measurement errors, the sample sizes are affected but there is a very minor change in acceptance parameter k . Further, suppose that it is decided to use σ , an acceptance criterion where σ_p is known to be 2.0. Let there exist an upper specific limit $U = 10.0$ and a unit for which the quality characteristic $x > U$ is considered as nonconforming.

Table 2 shows the performance characteristics of a sampling plan with $n = 25$ and $k = 2.0$ under a rectifying inspection scheme. If the true process average quality is operating at AQL ($\mu = 5.346$) and $r = \infty$, then 95% of the lots submitted will be accepted during the sampling inspection stage itself and only 5% of the rejected lots will be rectified by replacing non-conforming units with conforming units. In such a case, the AOQ will be only about 1%. If the submitted quality deteriorates to 1.79 % (error free case, that is, $r = \infty$), then only about 70% of the lots will be accepted by the sampling plan and approximately one out of every three lots will be rejected and rectified. The AOQ in such a case will not exceed the AOQL of 1.25% fixed, meaning that, irrespective of the product quality submitted by the producer, the consumer will receive an average quality not worse than 1.25% under the

rectification scheme. The worst case is when $r = 2$; the AOQ in such a case will just exceed the AOQL of 1.25% fixed for different errors sizes. The values of $P_a(p_m)$ for known σ case are presented in Table 3, and a visual comparison of AOQ curves for different error sizes is shown in Figure 1. As Figure 1 illustrates, the effect of measurement error is serious on the AOQ curves.

When using Table 1 to select sampling plans, limitations of plans indexed by AOQL under measurement error must be taken into account. Sampling with rectification of rejected lots reduces the average percentage of nonconforming items in the lots; however, it also introduces non-homogeneity in the series of lots finally accepted. That is, any particular lot will have a quality of $p\%$ or 0% non-conforming depending on whether the lot is accepted or rectified. Thus, the assumption underlying the AOQL principle is that the homogeneity in the qualities of individual lots is unimportant and only average quality matters.

Table 3 gives $P_a(p_m)$ values for the plans given in Table 1. If AQL is 0.25%, AOQL is 1.25% and $r = 2, 4, 6$ and ∞ , then $P_a(p_m)$ is 0.354, 0.342, 0.340 and 0.338, respectively, and $p_m = AOQL/P_a(p_m)$ for $r = 2, 4, 6$ and ∞ , is 3.53%, 3.65%, 3.67%, 3.69%. Thus, if the lot quality is 3.69% then, on average, among every three lots passed on to the consumer two will be free from non-conforming items while the third lot will contain 3.69% non-conforming items: this is about 15 times the AQL specified. In order to avoid such error, the producer should maintain the process quality approximately at the set AQL because a high rate of rejecting lots at $p = p_m$ will also indirectly put pressure on the producer to improve the submitted quality.

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SAMPLING PLANS FOR AQL AND AOQL VARIABLES WITH MEASUREMENT ERROR

Table 1: Single Sampling Plans for Variables Indexed by AQL and AOQL under Measurement Error

r	AOQL (%)	AQL (%)																
		0.040	0.065	0.100	0.150	0.250	0.400	0.650	1.000	1.500	2.500	4.000	6.500					
2	0.040	74, 3.107																
	0.080	19, 2.905	75, 2.971															
	0.125	10, 2.753	19, 2.765	63, 2.826														
	0.200	7, 2.604	10, 2.595	17, 2.606	43, 2.654													
	0.320	5, 2.458	6, 2.438	9, 2.429	14, 2.437	47, 2.504												
	0.500	3, 2.317	4, 2.289	5, 2.271	8, 2.263	14, 2.276	49, 2.350											
	0.800	3, 2.160	3, 2.235	4, 2.104	5, 2.083	7, 2.077	12, 2.091	47, 2.174										
	1.250		2, 1.965	3, 1.937	3, 1.914	4, 1.894	6, 1.888	12, 1.907	39, 1.989									
	2.000			2, 1.748	2, 1.722	3, 1.694	4, 1.677	6, 1.672	10, 1.692	25, 1.760								
	3.200					2, 1.477	3, 1.454	2, 1.438	5, 1.436	7, 1.453	26, 1.549							
	5.000							2, 1.143	3, 1.186	4, 1.186	7, 1.214	24, 1.326						
8.000								2, 0.889	2, 0.882	3, 0.887	6, 0.923	21, 1.058						
4	0.040	52, 3.109																
	0.080	17, 2.936	51, 2.969															
	0.125	10, 2.800	17, 2.795	45, 2.828														
	0.200	6, 2.665	9, 2.643	15, 2.639	33, 2.662													
	0.320	4, 2.532	6, 2.500	8, 2.481	12, 2.475	34, 2.508												
	0.500	3, 2.402	4, 2.365	5, 2.337	7, 2.318	12, 2.312	34, 2.351											
	0.800	2, 2.258	3, 2.217	4, 2.184	4, 2.157	7, 2.133	11, 2.130	32, 2.175										
	1.250		2, 2.067	3, 2.031	3, 2.000	4, 1.967	6, 1.946	10, 1.946	27, 1.990									
	2.000			2, 1.857	2, 1.823	3, 1.784	4, 1.754	5, 1.734	9, 1.734	19, 1.770								
	3.200					2, 1.585	2, 1.550	3, 1.521	4, 1.504	7, 1.503	19, 1.555							
	5.000							2, 1.299	3, 1.275	4, 1.260	6, 1.264	17, 1.327						
8.000								2, 1.003	2, 0.982	3, 0.968	5, 0.977	15, 1.055						

Table 1 (continued): Single Sampling Plans for Variables Indexed by AQL and AOQL under Measurement Error

r	AOQL (%)	AQL (%)												
		0.040	0.065	0.100	0.150	0.250	0.400	0.650	1.000	1.500	2.500	4.000	6.500	
6	0.040	49, 3.111												
	0.080	17, 2.942	48, 2.971											
	0.125	10, 2.809	16, 2.802	42, 2.829										
	0.200	6, 2.677	9, 2.653	14, 2.646	32, 2.666									
	0.320	4, 2.546	6, 2.513	8, 2.491	12, 2.483	33, 2.511								
	0.500	3, 2.419	4, 2.380	5, 2.350	7, 2.329	12, 2.320	32, 2.354							
	0.800	2, 2.277	3, 2.235	4, 2.199	4, 2.171	6, 2.145	11, 2.138	30, 2.174						
	1.250		2, 2.088	3, 2.050	3, 2.017	4, 1.981	6, 1.958	10, 1.954	26, 1.992					
	2.000			2, 1.878	2, 1.843	3, 1.802	4, 1.770	5, 1.747	8, 1.744	18, 1.773				
	3.200					2, 1.606	2, 1.569	3, 1.537	4, 1.518	7, 1.514	18, 1.558			
	5.000							2, 1.320	3, 1.293	4, 1.276	6, 1.275	16, 1.329		
	8.000								2, 1.026	2, 1.002	3, 0.984	5, 0.989	14, 1.057	
∞	0.040	47, 3.084												
	0.080	17, 2.900	46, 2.972											
	0.125	9, 2.754	16, 2.807	40, 2.831										
	0.200	6, 2.608	9, 2.661	14, 2.652	30, 2.670									
	0.320	4, 2.464	6, 2.523	8, 2.500	12, 2.489	31, 2.513								
	0.500	3, 2.324	4, 2.392	5, 2.361	7, 2.338	12, 2.327	31, 2.355							
	0.800	2, 2.168	3, 2.249	4, 2.213	4, 2.183	6, 2.154	11, 2.145	29, 2.178						
	1.250		2, 2.104	3, 2.065	3, 2.031	4, 1.994	6, 1.968	10, 1.961	25, 1.994					
	2.000			2, 2.006	2, 1.860	3, 1.817	4, 1.783	5, 1.748	8, 1.741	18, 1.788				
	3.200					2, 1.623	2, 1.585	3, 1.551	4, 1.529	6, 1.522	17, 1.561			
	5.000							2, 1.337	3, 1.308	3, 1.288	6, 1.284	15, 1.332		
	8.000								2, 1.044	2, 1.019	3, 1.998	5, 0.999	13, 1.060	

SAMPLING PLANS FOR AQL AND AOQL VARIABLES WITH MEASUREMENT ERROR

Table 2: Performance Characteristics of the Variables Plan under Measurement Error
for AQL = 0.01, AOQL = 0.0125, U = 10, SD = 2

r	μ	v'	p(%)	w	Pa	AOQ
2	5.4330	2.2835	1.12	1.6450	0.9500	1.0640
	5.6000	2.2000	1.39	1.1785	0.8807	1.2245
	5.8000	2.1000	1.79	0.6200	0.7324	1.3083
	5.9000	2.0500	2.02	0.3407	0.6333	1.2782
	6.0000	2.0000	2.28	0.0614	0.5245	1.1932
	6.2000	1.9000	2.87	-0.4971	0.3096	0.8889
4	5.3673	2.3163	1.03	1.6450	0.9500	0.9757
	5.4000	2.3000	1.07	1.5626	0.9409	1.0091
	5.6000	2.2000	1.39	1.0586	0.8551	1.1889
	5.8000	2.1000	1.79	0.5545	0.7104	1.2690
	6.0000	2.0000	2.28	0.0504	0.5201	1.1832
	6.2000	1.9000	2.87	-0.4537	0.3250	0.9334
6	5.3618	2.3191	1.02	1.6450	0.9500	0.9686
	5.4000	2.3000	1.07	1.5491	0.9393	1.0073
	5.6000	2.2000	1.39	1.0462	0.8523	1.1849
	5.8000	2.1000	1.79	0.5432	0.7065	1.2621
	6.0000	2.0000	2.28	0.0402	0.5160	1.1740
	6.2000	1.9000	2.87	-0.4627	0.3218	0.9240
∞	5.3460	2.3270	1.00	1.6450	0.9500	0.9484
	5.4000	2.3000	1.07	1.5100	0.9345	1.0021
	5.8000	2.1000	1.79	0.5100	0.6950	1.2415
	6.0000	2.0000	2.28	0.0100	0.5040	1.1466
	6.2000	1.9000	2.87	-0.4900	0.3121	0.8961
	6.4000	1.8000	3.59	-0.9900	0.1611	0.5788

Table 3: Pa(pm) Values of Known Sigma Plans Under Measurement Error

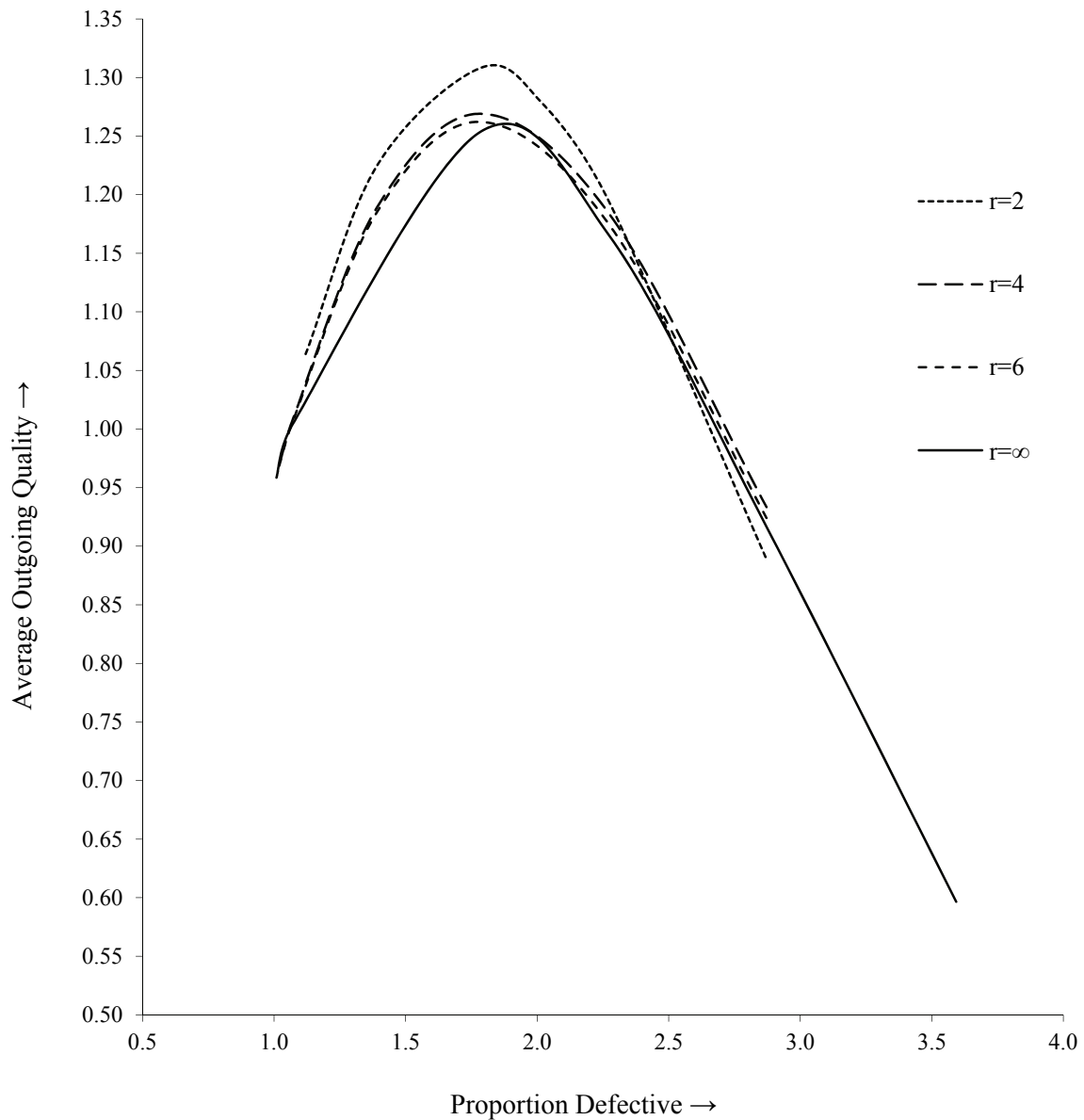
r	AOQL (%)	AQL (%)											
		0.040	0.065	0.100	0.150	0.250	0.400	0.650	1.000	1.500	2.500	4.000	6.500
2	0.050	0.769											
	0.080	0.538	0.774										
	0.125	0.413	0.554	0.781									
	0.200	0.327	0.420	0.541	0.723								
	0.320	0.271	0.335	0.415	0.522	0.762							
	0.500	0.235	0.282	0.338	0.411	0.546	0.765						
	0.800	0.210	0.245	0.286	0.336	0.425	0.549	0.776					
	1.250		0.224	0.255	0.292	0.354	0.436	0.567	0.766				
	2.000			0.236	0.263	0.308	0.364	0.447	0.558	0.729			
	3.200					0.284	0.324	0.379	0.449	0.544	0.753		
	5.000							0.504	0.393	0.454	0.572	0.769	
	8.000								0.367	0.407	0.479	0.581	0.781
4	0.050	0.723											
	0.080	0.510	0.753										
	0.125	0.395	0.527	0.712									
	0.200	0.315	0.402	0.515	0.723								
	0.320	0.262	0.323	0.398	0.498	0.718							
	0.500	0.228	0.273	0.326	0.394	0.520	0.745						
	0.800	0.205	0.239	0.278	0.325	0.408	0.529	0.727					
	1.250		0.219	0.248	0.283	0.342	0.420	0.540	0.737				
	2.000			0.232	0.258	0.300	0.353	0.431	0.533	0.715			
	3.200					0.278	0.316	0.369	0.434	0.522	0.718		
	5.000							0.338	0.383	0.440	0.548	0.727	
	8.000								0.361	0.398	0.465	0.561	0.750

SAMPLING PLANS FOR AQL AND AOQL VARIABLES WITH MEASUREMENT ERROR

Table 3 (continued): Pa(pm) Values of Known Sigma Plans Under Measurement Error

r	AOQL (%)	AQL (%)											
		0.040	0.065	0.100	0.150	0.250	0.400	0.650	1.000	1.500	2.500	4.000	6.500
6	0.050	0.702											
	0.080	0.505	0.728										
	0.125	0.391	0.521	0.711									
	0.200	0.313	0.398	0.509	0.689								
	0.320	0.260	0.320	0.394	0.493	0.696							
	0.500	0.227	0.271	0.324	0.391	0.514	0.714						
	0.800	0.205	0.238	0.276	0.323	0.405	0.519	0.721					
	1.250		0.218	0.247	0.282	0.340	0.416	0.535	0.713				
	2.000			0.231	0.256	0.299	0.351	0.428	0.528	0.707			
	3.200					0.277	0.314	0.367	0.431	0.518	0.701		
	5.000							0.337	0.381	0.437	0.544	0.714	
8.000								0.359	0.397	0.462	0.559	0.728	
∞	0.050	0.700											
	0.080	0.501	0.727										
	0.125	0.389	0.515	0.700									
	0.200	0.311	0.395	0.505	0.663								
	0.320	0.258	0.318	0.392	0.489	0.696							
	0.500	0.226	0.270	0.322	0.389	0.510	0.714						
	0.800	0.203	0.236	0.274	0.321	0.402	0.514	0.719					
	1.250		0.227	0.246	0.281	0.338	0.413	0.530	0.702				
	2.000			0.104	0.255	0.297	0.349	0.425	0.524	0.672			
	3.200					0.276	0.313	0.365	0.428	0.514	0.696		
	5.000							0.336	0.379	0.435	0.540	0.714	
8.000								0.358	0.395	0.460	0.553	0.720	

Figure 1: Average Outgoing Quality Curves under Measurement Error



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