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## Quantitative Resistance Assessment of SFRP-Strengthened RC Bridge Columns Subjected to Blast Loads

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1 **Quantitative Resistance Assessment of SFRP-Strengthened RC Bridge Columns Subjected**  
2 **to Blast Loads**

3

4 Ahmad Alsendi<sup>1</sup> and Christopher D. Eamon<sup>2</sup>

5

6 **Abstract**

7         The blast resistance of a typical reinforced concrete bridge pier column design was  
8 modeled with a nonlinear finite element approach that considers material damage, fracture, and  
9 separation. While varying concrete strength, amount of longitudinal reinforcing steel, and gravity  
10 load, the effect of applying an externally bonded steel fiber reinforced polymer (SFRP) wrapping  
11 was assessed. The presented approach uniquely quantifies column blast resistance in terms of  
12 charge weight. It was found that blast capacity was roughly linearly related to concrete strength  
13 and steel reinforcement ratio, the former of which is most influential. It was further found that a  
14 single layer of SFRP modestly increased blast resistance, while additional SFRP layers provided  
15 minimal benefit.

16

17 **Author Keywords:**

18 concrete, columns, bridges, finite element analysis, blast, explosive load, FRP, SFRP.

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24 **Problem Introduction**

25 To receive federal funding for construction and maintenance of vehicular and pedestrian  
26 bridge structures, State DOTs must meet the minimum design requirements provided in the  
27 American Association of State Highway and Transportation Officials *LRFD Bridge Design*  
28 *Specifications* (AASHTO LRFD 2017). As such, the vast majority of highway bridges in the  
29 United States are designed according to these standards. The limit states given in AASHTO to  
30 which bridge elements must be designed include various loads such as dead, live (vehicle and  
31 pedestrian), wind, seismic, as well as various others. Among these is blast loading (*BL*), which  
32 appears within the Extreme Event II limit state and is given a load factor of 1.0. This limit state  
33 also considers other possible impact loads from ice, vehicles, and ships on a bridge structure.  
34 Although blast load is identified and given a load factor, AASHTO provides no corresponding  
35 design criteria or recommendations for mitigation. Rather, AASHTO notes that blast load is a  
36 function of explosive charge characteristics as well as other parameters, and directs the designer  
37 to obtain any blast-related design requirements from the bridge owner.

38 Depending on the bridge geometry and size and placement of an explosive charge, any  
39 structural element may potentially experience damage, including superstructure components such  
40 as the deck and girders, as well as substructure elements such as abutments, piers, and the  
41 foundation. Of these, the central pier columns, an ubiquitous component of two span bridges  
42 crossing highways, are easily accessible and may cause complete collapse of both bridge spans if  
43 critically damaged. Because AASHTO does not specifically require consideration of blast load,  
44 the vast majority of bridge column designs within the US have not considered such loading. As  
45 most bridges likely face a very low threat to blast damage, this is perhaps appropriate. However,  
46 this accompanying lack of experience with blast loads as well as design provisions in AASHTO

47 LRFD require that engineers tasked with mitigating blast loads on bridge columns look to other  
48 sources for guidance.

49 Various researchers have recognized this need and studied this problem in the last two  
50 decades. The resulting research focused on several different bridge components including girders  
51 (Anwarul and Yazdani 2008; Cofer et al. 2010), decks (Lawver et al. 2003; Foglar and Kovar  
52 2013; Foglar et al. 2017), a complete bridge (Winget et al. 2005), as well as columns (Williamson  
53 et al. 2011a, b; Williams et al. 2008; 2011; Williams 2009), where it was found that column  
54 geometry and reinforcement type, spacing, and splicing affected blast load resistance. Winget et  
55 al. (2005) and Yi et al. (2014) studied column failures and found that multiple modes are possible,  
56 including crushing or shearing of the column base; fracturing reinforcement; surface spalling; and  
57 plastic hinge formation. Much of the above research has been used to provide design guidance for  
58 bridge columns exposed to blast threats.

59 In this study, of particular concern is the large infrastructure of existing structures. If an  
60 existing bridge is found to experience an increased blast threat such that structural enhancement  
61 of the pier columns is warranted, it would be very costly to demolish and replace with a new, blast-  
62 resistant design. This would be especially undesirable if the superstructure is otherwise sound. In  
63 this case, a much cheaper, faster, and less disruptive retrofit option may be most feasible. To this  
64 end, several studies have explored retrofitting as a protective option. Malvar et al. (2007)  
65 examined the response of retrofitted columns with composite wraps or steel jackets under blast  
66 loading, and found that shear capacity could be enhanced. Later, Fujikura and Bruneau (2011)  
67 conducted blast tests on scaled reinforced concrete (RC) columns fit with steel jacketing, and  
68 determined that the columns did not exhibit ductile behavior under blast loading, but rather failed  
69 in base shear rather than flexural yielding. At about the same time, Heffernan et al. (2011)

70 subjected scaled RC columns to blast loads that were strengthened with composite wrapping  
71 formed of carbon or steel fibers. The authors found that not only carbon wrapping, but steel fiber  
72 reinforced polymer (SFRP) wrap could reduce the amount of concrete crushing that occurred in  
73 plastic hinge regions. More recently, Eamon and Alsendi (2017) conducted a cursory study on the  
74 blast resistance of SFRP columns, but few cases considered, with atypical wrapping application,  
75 unusual column boundary conditions, and coarse modeling, significantly limiting the usefulness  
76 of the results. SFRP has been previously studied for strengthening slabs for blast resistance as  
77 well, and was found to provide significant increase in resistance for these components (Silva and  
78 Lu 2007). Of these options, this study is focused on the SFRP alternative, which is not only ductile,  
79 but substantially less expensive than CFRP, and does not meaningfully increase column width as  
80 with most steel jacketing products. As summarized above, only a few numerical and experimental  
81 studies have investigated the effect of blast loads on SFRP-strengthened columns. Although this  
82 existing work is highly valuable, this topic remains significantly underexplored and the ability of  
83 SFRP to strengthen columns under blast, as well as the effect of typical design parameter changes  
84 on the blast resistance of unstrengthened columns, is greatly unquantified. As such, nearly all  
85 available results provide qualitative assessments or are relatively coarse (in a binary sense, either  
86 column failure or survival), leaving the specific change in column resistance to design parameter  
87 changes, such as SFRP strengthening, unknown.

88 Thus, the objective of this study is to estimate the blast resistance of typical bridge columns  
89 retrofitted with SFRP and compare the result to unmodified columns, in order to assess the  
90 potential benefit of this retrofit technique. In this process, a finite element analysis (FEA) approach  
91 is implemented to model hypothetical bridge columns subjected to blast. The effect of several  
92 design parameter changes on blast resistance are quantified, including the amount of longitudinal

93 reinforcing steel, compressive strength of concrete, axial load on the column, as well as the use of  
94 SFRP strengthening.

### 95 **Description of Bridge Columns Analyzed**

96 Although column designs vary significantly, based on typical bridge structural geometries  
97 in the State of Michigan (Eamon et al. 2018), which are representative of many other states,  
98 columns in multi-column bridge piers are usually from 760 – 914 mm square with unsupported  
99 lengths from 3-5 m. The columns are linked together above by a pier cap (beam) which in turn  
100 supports the bridge girders, and the columns are supported below by a foundation. To represent  
101 the larger range of common highway bridge structures which are perhaps more prone to attack by  
102 blast, the upper range of these column dimensions were chosen for consideration in this study (914  
103 mm square and 5 m unsupported length), providing a typical non-slender design (slenderness ratio  
104  $L/r = 18.5$ , where  $L$  = unsupported length of column and  $r$  = radius of gyration), as shown in Figure  
105 1.

106 The columns are assumed to have concrete compressive strength of  $f'_c = 42$  MPa, with  
107 longitudinal reinforcement provided by 7 #8 (25 mm) bars per face for 24 bars total, which results  
108 in a reinforcing ratio ( $\rho$ ) of 0.015. Stirrup ties (#4; 13 mm) are placed at 300 mm on center, with  
109 50 mm cover. All steel is assumed to be Grade 60, with yield strength of 420 MPa. Additional  
110 design variations were also considered, with  $f'_c$  of 28 and 55 MPa, as well as longitudinal bar sizes  
111 of #11 (35 mm) and #14 (43 mm), with resulting reinforcement ratios of 0.029 and 0.042,  
112 respectively. Although these larger bar sizes are not commonly used, they were considered in this  
113 study to quantify the effect of changing reinforcing ratio.

114 The SFRP wrapping considered is based on commercially available products, where the  
115 composite is formed from unidirectional steel strands embedded in a thin polymer sheet to hold

116 the fibers together. In the strong direction, the 1.2 mm thick composite sheets are taken to have a  
117 yield strength of 985 MPa and Young's modulus of 66.1 GPa, where in the weak direction, strength  
118 and stiffness are insignificant (Hardwire 2014). In practice, as with similar externally-bonded  
119 CFRP fabrics, after proper surface preparation, the column faces are coated with resin and then  
120 wrapped with SFRP. These systems are generally designed to increase the axial strength of an  
121 existing column by enhancing confinement strength. However, as noted above, such externally-  
122 bonded retrofit wraps have been repurposed to increase resistance to blast load as well, the focus  
123 of this study. Although more commonly used composite materials are available, the SFRP wrap  
124 is not only ductile but has about the same price as glass FRP, rendering it a less expensive  
125 alternative than more traditional CFRP wrapping. Two cases of wrapping are considered, where  
126 a single sheet and three sheets are applied. In both cases, the SFRP is applied to the column in the  
127 typical sense where the strong direction is oriented horizontally.

## 128 **Models for Concrete and Reinforcement**

129 Concrete constitutive relationships were modeled with the Johnson Holmquist Cook  
130 approach, a model developed for characterizing concrete behavior under large strains as well as  
131 high rates of strain and pressure (Holmquist 1993), conditions specifically associated with blast  
132 loading. In this model, pressure, strain rate, and accumulated damage affect concrete strength,  
133 where cumulative damage is a result of pressure and plastic strains experienced over time. The  
134 relationship between applied pressure and effective material stress is given by:

$$135 \sigma^* = [A(1-D) + BP^{*N}][1-C\ln(\dot{\epsilon}^*)] \quad (1)$$

136 where  $\sigma^*$  is equivalent stress normalized to concrete compressive strength, given as  $\sigma^* = \sigma / f'_c$ ,  
137 where  $\sigma$  is normal stress;  $P^*$  is applied pressure, similarly normalized as  $P^* = P / f'_c$ ;  $D$  is

138 cumulative damage, discussed further below; and  $\dot{\epsilon}^*$  is the normalized strain rate ( $\dot{\epsilon}^* = \dot{\epsilon} / \dot{\epsilon}_o$ ), such  
 139 that  $\dot{\epsilon}$  is the actual rate of strain and  $\dot{\epsilon}_o$  a reference value of  $1.0s^{-1}$ . Eq. 1 requires five material  
 140 constants, which are the normalized cohesive strength ( $A$ ); the normalized pressure hardening  
 141 coefficient ( $B$ ); the strain rate coefficient ( $C$ ); the pressure hardening exponent ( $N$ ); and the  
 142 normalized maximum material strength ( $S_{MAX}$ ). Damage ( $D$ ) is a function of the cumulative  
 143 equivalent plastic strain and volumetric strain, given as:

$$144 \quad D = \sum [\Delta\epsilon + \Delta\mu_p / D_1 (P^* + T_H^*)^{D_2}] \quad (2)$$

145 where  $\Delta\epsilon_p$  is equivalent plastic strain;  $\Delta\mu_p$  equivalent plastic volumetric strain; and  $T_H^*$  the  
 146 maximum tensile hydrostatic pressure, normalized to concrete strength as  $T_H^* = T_H / f'_c$ . Three  
 147 damage constants are used to calibrate the relationship to a specific material, and are given as  $D_1$ ,  
 148  $D_2$ , and  $EF_{MIN}$ , where the latter constant specifies the plastic strain threshold needed for fracture  
 149 damage initiation.

150 A final set of relationships are specified in the model to describe compressive hydrostatic  
 151 pressure  $P$  as a function of volume change. Here, three regions are considered; initial linear elastic  
 152 behavior, prior to concrete crushing ( $P \leq P_{crush}$ ); linear inelastic behavior as pressure is increased,  
 153 to represent the collapse of voids and pores within the concrete, but prior to complete collapse of  
 154 all voids ( $P_{crush} \leq P \leq P_{lock}$ ); and nonlinear inelastic behavior as  $P$  is further increased once all  
 155 voids have been compressed ( $P > P_{lock}$ ). The third region is described as:

$$156 \quad P = K_1\bar{u} + K_2\bar{u}^2 + K_3\bar{u}^3 \quad (3)$$

157 In the above limits,  $P_{crush}$  is the pressure corresponding to initial concrete crushing and loss of  
 158 elastic behavior, given as:  $P_{crush} = K * \mu_{crush}$ , where  $K$  is the elastic bulk modulus and  $\mu_{crush}$  the  
 159 corresponding volumetric strain at crushing; and  $P_{lock}$  is the pressure at which all voids are



160 collapsed. In Eq. 3,  $K_1$ - $K_3$  are material constants and  $\bar{u}$  is a measure of volumetric strain, adjusted  
161 by the volumetric strain at  $P_{lock}$  ( $\mu_{lock}$ ):  $\bar{u} = \bar{u} - \bar{u}_{lock} / 1 + \bar{u}_{lock}$ . The material constants needed to  
162 define the model are taken from values obtained from concrete specimen test results given by  
163 Holmquist et al. (1993) and Williamson et al. (2011), and are summarized in Table 1.

164 A kinematic, elastic-plastic relationship is used to model reinforcing steel behavior. For  
165 all reinforcement, yield stress is specified as 450 MPa, Young's modulus as 200 GPa, and post-  
166 yield modulus as 20 GPa. Strain rate parameters are considered by using Cowper and Symonds  
167 model (Livermore 2018) which scales the yield stress with the factor:

$$168 \quad 1 + \left(\frac{\dot{\epsilon}}{c}\right)^{1/p} \quad (4)$$

169 where  $\dot{\epsilon}$  is the strain rate, and strain rate parameters of  $40.4 \text{ s}^{-1}$  and 5.0 are taken for  $c$  and  
170  $p$ , respectively (Bai and Jin 2016).

171 The SFRP sheet is modeled as anisotropic material with a yield stress of 985 MPa and  
172 elastic modulus of 66.1 GPa in the strong direction with Poisson ratio of 0.3, whereas the weak  
173 direction has insignificant strength and stiffness (corresponding properties taken as approximately  
174 1/100th of the strong direction). Sheet thickness is taken as 1.20 mm (Hardwire 2014).

## 175 **FEA Approach**

176 The concrete material of the column was represented with a regular mesh of approximately  
177 171,000 hexahedral elements (typical length 1.4 – 2.5 cm), whereas beam elements were used to  
178 model steel reinforcement. To avoid highly distorted elements and to simulate fracture debris, in  
179 addition to the concrete model above that includes strength and stiffness softening, once an element  
180 reaches a principal strain of 0.003, the element is taken to be so badly damaged that it is deleted  
181 from the model. Exposed element surfaces caused by deletion are bound by new contact surfaces,  
182 which prevent elements undergoing large displacements from penetrating others and allow

183 fragmented pieces to collide. Similarly, contact surfaces are specified between beam elements  
184 representing reinforcing bars and solid concrete elements. Here, reinforcement is taken as  
185 completely bonded to the concrete until the surrounding concrete elements are disintegrated.

186 The SFRP material was modeled with shell elements, where it was assumed that the SFRP  
187 was applied to the lower half of the column only, where blast load is greatest for a charge placed  
188 on the ground (it was found that wrapping the entire column height made little difference in  
189 performance but significantly increased computational time). As with the beam elements for  
190 reinforcing modeling, the SFRP shells are linked to the model via contact surfaces to allow element  
191 interaction but prevent surface penetration. An SFRP shell element deletion criterion is specified  
192 as exceeding a longitudinal strain limit of 0.021, a value at which steel fiber rupture is expected to  
193 occur (Hardwire 2014).

194 The contact surface representing the SFRP bond initially rigidly links the SFRP shells to  
195 the concrete elements. When a specified failure criterion is reached, the slide surface releases  
196 the nodal constraints, allowing the shells to slide against or separate from the concrete surface.  
197 The failure criterion is given by:

$$198 \quad \left( \frac{F_n}{F_{nf}} \right)^2 + \left( \frac{F_s}{F_{sf}} \right)^2 \geq 1 \quad (5)$$

199 where  $F_n$  and  $F_s$  are the calculated normal (tensile) and shear stresses, respectively, while  
200  $F_{nf}$  and  $F_{sf}$  are the normal and shear stress limits at failure. Here  $F_s$  is equal to the vector sum of  
201 the two shear components on the interface surface. The failure stress limits are based on typical  
202 resin properties, and are taken as  $F_{nf} = 32$  MPa, and  $F_{sf} = 29.4$  MPa. (\*\*add Sika ref \*\*). Once  
203 bond failure occurred, the coefficient of friction ( $\mu$ ) between the SFRP shells and concrete was

204 varied from 0.3-0.7 in the model, but, as expected, no significant difference in ultimate blast  
205 capacity resistance was found as a function of  $\mu$ .

206 The base of the column was taken as fully constrained to the ground, and the column top  
207 was constrained by attaching it to a simple beam element model of the surrounding pier cap and  
208 column frame system (as shown in Figure 1). These elements were given equivalent structural  
209 member properties based on the dimensions of the pier cap and column(s). To develop a  
210 representative dead load on the column, it is assumed that the pier supports a two-span, two-lane  
211 highway bridge where each span is 18.3 m long and the deck is 228 mm thick and 13 m wide,  
212 made of reinforced concrete, and supported by seven W36x170 steel girders. The pier is taken to  
213 be composed of 4 columns as shown in Figure 1, and the pier cap is 13 m long, 1 m high, and 0.9  
214 m wide. These dimensions are similar to those of many highway bridges within Michigan as well  
215 as in other States. Based on this configuration, three different levels of axial load were applied to  
216 represent different gravity load scenarios: dead load only (DL), which includes the self-weight of  
217 the structure detailed above including barriers and diaphragms; the allowable nominal load on the  
218 structure (NL), taken as the total unfactored dead and live load that the column could support  
219 according to AASHTO LRFD criteria; and a maximum axial load (ML) that the column could  
220 resist according to its nominal capacity ( $P_n$ ), given by:

$$221 \quad P_n = 0.80 [k_c f'_c (A_g - A_{st})] + A_{st} f_y \quad (8)$$

222 where  $k_c$  is the ratio of the maximum concrete compressive stress to the design compressive  
223 strength of concrete (0.85);  $f'_c$  is the compressive strength of concrete;  $A_{st}$  is the total area of  
224 longitudinal steel reinforcement;  $f_y$  is the yield stress; and  $A_g$  is the gross cross-sectional area.  
225 Although such a high load is not realistic from a design perspective, it was included to place a  
226 bound on possible column performance, which was found to be significantly influenced by axial

227 load, as discussed in the results section. The dead load (DL) and allowable nominal load (NL)  
228 scenarios resulted in axial loads of 285 and from 14,000-30,000 kN, respectively, while the  
229 maximum load (ML) case varied as high as 24,500–52,000 kN, depending on the column design  
230 considered. Note the great discrepancy between the actual nominal gravity design loads (dead  
231 load = 285 kN; live load, based on the AASHTO HL-93 design vehicle load = 166 kN, for a total  
232 of 451 kN, and the allowable nominal load of 14,000-30,000 kN, indicative of how greatly  
233 oversized these bridge columns are for axial load); other design concerns such as vehicle  
234 collision, uniformity in construction for various bridges, and long-term maintenance typically  
235 dictate column section size.

236 No published data are available on typical charge standoff distances. Based on an  
237 inspection of approximately 100 blast-damaged structures in Iraq from 2014-2016 by the author,  
238 however, a significant variation in apparent charge placement was found. From these observations,  
239 the initiation point of the blast was taken as 50 mm above ground and approximately 1 m away  
240 from the column, a horizontal standoff distance which represented the average of those which  
241 could be identified.

242 The models were solved explicitly with a Lagrangian FEA formulation that allows for large  
243 strains and displacements as well as the separation, subsequent contact, and disintegration of  
244 elements using LS-DYNA (Livermore 2018).

## 245 **Blast Load**

246 The blast load model in this study is based on the CONWEP approach (Hyde 1988), which  
247 is formulated from a modified version of Friedlander’s Equation fit to empirical data of blast  
248 pressures resulting from various charge weights and standoff distances (Kingery and Bulmash  
249 1984). In this method, the resulting overpressure  $P$ , i.e. the air pressure over the ambient

250 atmospheric pressure caused by the compressive shock wave from the blast, is modeled as a  
251 function of time ( $t$ ) as:

$$252 \quad P(t) = P_0 \left(1 - \frac{(t-t_a)}{t_d}\right) \exp \left(-b \frac{(t-t_a)}{t_d}\right) \quad (5)$$

253 where  $P_0$  is peak overpressure;  $t_a$  the time of shock wave arrival;  $t_d$  the duration of the positive  
254 pressure phase, and  $b$  the decay coefficient, as shown in Figure 2. Time constants are a function of  
255 charge characteristics and placement, whereas  $b$  is determined by iteration during the analysis.  
256 When the shock wave strikes an object, rather than being absorbed, it may reflect and strike a  
257 second object. This second object may thus experience both side-on (direct) blast overpressure as  
258 well as reflected overpressure. The combination of these pressures may result in a significant  
259 increase over that generated by the direct blast. The total overpressure  $P_T(t)$  resulting from the  
260 superposition of direct and reflected blast shock waves is given by:

$$261 \quad P_T(t) = P_r(t) \cos^2 \theta + P_{so}(t) (1 + \cos^2 \theta - 2 \cos \theta) \quad (6)$$

262 where, for  $\cos \theta \geq 0$ ,  $P_r(t)$  is the reflected blast overpressure;  $P_{so}(t)$  the side-on overpressure as  
263 determined from Eq. 5 such that  $P_{so}(t) = P(t)$ ; and  $\theta$  the incidence angle between the blast wave  
264 and the normal of the reflecting surface. Although only a single structural element is exposed to  
265 blast in this study, Eq. 6 becomes relevant due to the presence of the ground, where as discussed  
266 above, the charge is located close to the ground and is thus modeled as a hemispherical surface  
267 burst that includes the reflected shock wave.

## 268 **Approach Validation**

269 Very few data are available that allow model validation. However, the general FEA  
270 approach described above was used in this study to successfully model column specimens exposed  
271 to blast load in previous research (Williamson et al. 2011). The experimental columns were similar

272 to those considered in this study, although slightly smaller, with a 760 mm square cross section  
273 and height of 3.43 m. The columns were cast from 28.6 MPa concrete and reinforced with seven,  
274 19 mm (#6) longitudinal bars per face and 13 mm (#4) stirrup ties spaced at 150 mm, with 25 mm  
275 cover. Bar yield strengths were 450 and 345 MPa for the longitudinal bars and ties, respectively.  
276 The cross-section is identical to that shown in Figure 1, except the side width is 0.76 m. The  
277 columns had a fixed base, a pinned top with no axial load, and were subjected to various blast  
278 loads initiated at the column base. A typical result is shown in Figure 3, where a test result is  
279 compared to the FEA model. The model result appears to be a reasonable representation of the  
280 general deformed shape, concentration of cracks, and locations of spalled concrete on the column.  
281 The model also appears to reasonably match the angle of the deformed reinforcement at the base  
282 of the column as well, most clearly seen from the exposed bar on the far right side. Only one  
283 quantitative value was reported for the experimental results, the maximum displacement of the  
284 column base at the end of the blast (approximately 5-6 ms). For the column shown, this was  
285 reported as 6.6 cm, while the analysis result was 7.1 cm. Given that a significant variation in  
286 strength exists even with static tests of nominally identical reinforced concrete specimens, analysis  
287 results were considered to be reasonably representative of column behavior and sufficiently  
288 accurate for assessment of performance for use in this study. Typical model solution time was  
289 approximately 18 minutes using ten 2.6GHz Intel processors in parallel and 5 GB of memory.

## 290 **Failure Behavior**

291 Using the modeling approach described above, the bridge pier column designs considered  
292 earlier were analyzed for blast resistance capacity, which is defined here as the maximum charge  
293 weight that the column could be subjected to and still support the axial load imposed. This was  
294 done by running multiple analyses, incrementing the charge weight up or down as required, to just

295 cause a failure (i.e. collapse) condition. This critical charge weight (within a 1% tolerance) is then  
296 recorded. This specifically quantitative approach, to the knowledge of the authors, has not been  
297 previously considered in the evaluation of column blast capacity.

298 A typical result is shown in Figure 4 for a column with  $f'_c = 41.4$  MPa,  $\rho = 0.029$ , and axial  
299 load of 285 kN, at several points in time beyond blast initiation (at  $t=0$ ), where the blast initiated  
300 at the bottom left of the column in the figures. Note in the figures, the supporting pier cap beam  
301 and adjacent columns (modeled as beam elements, as discussed above) are not shown for clarity.  
302 As shown, column failure is caused by base shearing and crushing. This column was exposed to  
303 the minimum charge weight just required to cause its collapse under the axial load. Although the  
304 exact shape and magnitude of the blast pressure profile vary across the face of the column, Figure  
305 5 provides representative pressure curves at the column midheight, for a blast load just enough to  
306 fail the column (“minimum blast”), as well as a significantly larger blast load (“high blast”)  
307 corresponding to a charge weight 3.5 times greater than that needed to fail the column. As shown  
308 in the figure, the blast pressure peaks at approximately 0.08 s, then decays to a (typically) briefly  
309 negative pressure at about 0.0875 s before rebounding, following the generally expected profile as  
310 shown in Figure 2.

311 At about the same time the peak pressure is reached, the concrete material at the column  
312 base is destroyed after extensive softening, and the column base is pushed away from the blast,  
313 bending the bottom longitudinal reinforcing bars. As the column base becomes eccentric relative  
314 to the top, the column slightly rotates counterclockwise, in turn causing some elements at the top  
315 right of the column to become crushed against the load plate representing the base of the pier cap.  
316 This phenomenon of member rotation causing crushing of the top material into a supporting  
317 component was similarly observed in concrete masonry walls subjected to blast (Eamon et al.

318 2004). This behavior is more evident in Figure 6, where the column is subjected to the higher  
319 level of load as shown in Figure 5, to be discussed further below. Mirroring the experimental  
320 deformation given in Figure 3, the column failure is thus caused by severe damage to the column  
321 base, characterized by base shifting, localized concrete cracking and crushing, and rebar bending,  
322 at which time the vertical load can no longer be supported.

323 A time-history of the column displacement is given in Figure 7 (“Base column, min blast”  
324 results), where a fairly nonlinear rate of vertical displacement is shown. Displacement (measured  
325 at the top of the column) begins to occur at approximately 0.06 s, slightly before the blast peak of  
326 0.08 s, then the rate of collapse quickly increases soon afterwards. It is approximately at the blast  
327 peak that collapse initiates, when the bottom elements are destroyed and the reinforcement begins  
328 to bend, while at 0.12 s the reinforcement bends more significantly and the rate of collapse further  
329 increases. A similar response is seen for horizontal displacement (measured near the middle of  
330 the column) in Figure 8, although the rate of horizontal motion begins more rapidly as compared  
331 to the vertical motion.

332 Plastic strains in reinforcing bars near the bottom of the column are given in Figure 9. In  
333 the figure, labels are give the format: “Bar – Face, load level”, where “L” refers to a longitudinal  
334 bar and “T” a transverse bar; “F” a bar on the column side facing the blast and “B” on the back  
335 side of the column; and “high” and “min” to the two blast load levels considered as discussed  
336 earlier, and “SFRP” to columns so reinforced. For all cases, both longitudinal and transverse bars  
337 begin to yield at about same time of 0.07 s. Here plastic strains increase sharply then remain fairly  
338 constant (to a maximum level of about 0.0024) after the most severe deformation ends. For  
339 transverse bars, plastic strains are significant but not as quite as severe (to about 0.002). Strains



340 in corresponding reinforcing bars on the face of the column opposite to the blast show a similar  
341 pattern, but the total deformation is much less, to about a half to a third in most cases.

342 To investigate the effect of a higher level of load on the failure behavior of the column, the  
343 significantly greater charge weight noted above (3.5 times the minimum necessary for failure) was  
344 applied as well. This result is given by Figure 6 and is also quantified in Figures 7-9 for  
345 comparison. As shown in the figures, the overall behavior is similar to that displayed at the lower  
346 load level, but with exaggerated effects, where failure occurs by concrete damage, sliding, and  
347 reinforcement bending at the base. Similarly, greater damage also occurs at the top of the column  
348 as it is rotated into the load plate. Additionally, a large diagonal “crack” near the base can be  
349 observed, as well as additional significant damage along the height of the column face adjacent to  
350 the blast. Here realize that many of the concrete elements experience damage and softening during  
351 the blast per the constitutive relationship given by the material model as discussed above; missing  
352 elements shown in the figures only represent those that have been so greatly deformed that they  
353 have lost all effective ability to transfer load and were thus removed from the model.

354 As shown in Figures 7 and 8, the displacement response of the column under high blast  
355 load is similar to that subjected to the minimum level. Here, as expected, the rate of displacement  
356 is greater, which is clear from a comparison of the deformation images given in Figures 4 and 6,  
357 although interestingly, differences in vertical displacement are more pronounced than horizontal.  
358 Close to the peak blast time, at approximately 0.075 s, as the base of the column is pushed inward,  
359 longitudinal bars facing the blast yield and quickly deform to a large maximum plastic strain of  
360 approximately 0.0027 (Figure 9). This large deformation can be seen in Figure 6. Transverse bars  
361 similarly begin to yield, though peak plastic strain are somewhat less. Similar to the low load level  
362 case, reinforcement strains on the opposite face are less than half of those facing the blast.

363 As expected, wrapping with SFRP requires a greater charge weight to fail the column. For  
364 example, the base column discussed above required approximately 86 kg of equivalent charge  
365 weight to fail, while the corresponding column wrapped with 1 layer of SFRP required 98 kg to  
366 just fail. The behavior of this column is shown in Figure 10, where at about the peak blast time,  
367 the SFRP strands that face the blast rupture (and thus these elements contribute insignificant  
368 stiffness and are removed from model), producing a few major horizontal “cracks” across the  
369 column face. The column then soon begins to collapse, but without the extensive base damage and  
370 horizontal shift seen with the unwrapped column. However, the blast does cause some slight  
371 rotation, causing the column top of column to crush against load plate. As shown in Figures 7 and  
372 8, the displacement of the column is only slightly delayed with SFRP.

373 As shown in Figure 9, the SFRP wrapping significantly reduced strain in the reinforcement,  
374 from about a maximum plastic strain in the longitudinal bars from about 0.0025 (unwrapped) to  
375 about 0.0015, even though a higher blast load was required to fail the column. For transverse bars,  
376 maximum strains were reduced much further, to only a fraction of the non-wrapped case (from  
377 about 0.002 to 0.00025). This is not surprising, since the SFRP wrap is oriented horizontally and  
378 effectively acts as transverse reinforcement. As with the unwrapped column, strains are much  
379 lower on the opposite face of the blast. At the higher load level, a similar overall response occurs,  
380 but a larger portion of the concrete shell behind the SFRP wrap is crushed, with more extensive  
381 base damage, as shown in Figure 11.

382 It should be mentioned that, although not permitted by the AASHTO LRFD Specifications,  
383 removing the stirrup ties from the column design resulted in a very large drop in blast resistance.  
384 For example, for a model column with 42 MPa concrete strength and longitudinal reinforcement  
385 ratio of 0.029, blast capacity was reduced by approximately two thirds (from 97 kg to 30 kg of

386 equivalent charge mass). Here it is apparent it the use of SFRP alone would not be an affective  
387 alternative to replacing stirrups.

388

### 389 **Results of Parametric Analysis**

390 Before the SFRP-wrapped columns were evaluated, a series of unwrapped columns were  
391 analyzed for blast failure load (in terms of equivalent charge weight) while varying several  
392 different design variables within the initial geometry considered. As discussed above, these were  
393 concrete strength ( $f'c$ ), longitudinal steel reinforcement ratio ( $\rho$ ), and axial load ( $P$ ), for a total of  
394 27 models (all combinations of three variations of each parameter). Figure 12 provides blast load  
395 resistance as a function of concrete strength, while Figure 13 graphs resistance in terms of  
396 reinforcement ratio. As shown in Figure 12, a fairly linear relationship between concrete strength  
397 and blast load resistance can be seen across a variety of reinforcement ratios and axial loads. It is  
398 interesting to note that the slope of the  $f'c$  vs resistance line is similar regardless of axial load or  
399 reinforcement ratio, indicating that change in  $f'c$  provides about the same absolute amount of  
400 capacity increase to blast, regardless of these other parameters. The result of this is, doubling  
401 concrete strength increases blast resistance by approximately 30-50%, where greatest proportional  
402 increases are seen for the least-reinforced columns loaded under dead load (DL) only, and least  
403 proportional increases are observed for columns most highly reinforced and under very high axial  
404 load (ML). Observing the results in Figure 13, it appears that the relationship between blast load  
405 resistance and steel reinforcement ratio is approximately linear. Following the same general  
406 relationship as with concrete strength, about the same absolute value of capacity increase to blast  
407 is seen as the amount of reinforcement is increased, regardless of concrete strength or axial load  
408 level. Blast capacity is less sensitive to reinforcement than concrete strength, however, as a 3.5

409 fold increase in reinforcing ratio provides a blast capacity increase of about 20 kg (with an initial  
410 charge weight resistance of approximately 65 to 105, depending on column configuration). Notice  
411 in both figures that as the applied axial load is increased, blast resistance is increased, albeit at a  
412 relatively slow rate. For a short column not governed by instabilities this is somewhat expected,  
413 where a high axial force effectively acts as a restraint, ‘clamping’ the column down and inhibiting  
414 the horizontal displacement which ultimately leads to collapse. Here is should be noted that shorter  
415 (3 m tall) columns with otherwise identical design parameters were also studied, and only very  
416 small increases in blast resistance were found over the 5 m tall columns. It was determined that  
417 this occurred because both the 3 m and 5 m columns are significantly within the ‘short’ column  
418 range, where capacity is governed by material strength rather than instability.

419 Results for the SFRP-wrapped columns subjected to axial dead load (DL), the expected  
420 gravity load condition, are given in Figure 14, where 18 model results are summarized (three  
421 variations each of  $f'c$  and  $\rho$ , and two SFRP layer arrangements). Applying one layer of SFRP  
422 provided a modest increase in blast capacity from approximately 10%-15% depending on the  
423 column variation considered; columns with initially higher capacities experienced a somewhat  
424 greater benefit in terms of additional charge weight that could be resisted with the same amount of  
425 SFRP. The increase in capacity provided is about equivalent to doubling the amount of longitudinal  
426 steel. As shown in the figure, three layers of SFRP were also applied in the model, which resulted  
427 in blast capacity increases from only about 1% to 3%. Larger increases in blast capacity from  
428 SFRP were observed under higher axial load conditions, up to 30% in some cases, but such high  
429 axial load cases are not reasonably expected in practice.

## 430 **Conclusions**

431           The blast resistance of a typical larger bridge pier column was modeled, and the impact of  
432 changes in concrete strength, amount of longitudinal reinforcing steel, gravity load, and application  
433 of SFRP wrapping were quantified. Blast capacity was found to be a roughly linear function of  
434 concrete compressive strength, where doubling concrete strength increases blast capacity from  
435 about 30-50%. Similarly, reinforcement content is approximately linearly related to blast  
436 resistance but results are less sensitive, where increasing reinforcement ratio by a factor of  
437 approximately 3.5 results in a resistance increase of 10-20%. Increasing axial load on the short  
438 columns studied was also found to increase blast resistance. A single layer of SFRP, applied on  
439 the lower half of the column closest to the blast loads considered, increased capacity by a range  
440 from 10%-15% with typical axial loads applied. Additional SFRP layers provided an insignificant  
441 increase in resistance. Thus, for new construction, of the parameters investigated, increasing  
442 concrete strength appears to be most effective. For retrofits, although SFRP is relatively  
443 inexpensive compared to common alternatives, it appears to provide modest gains on the column  
444 geometry studied.

#### 445 **Data Availability**

446 All data, models, and code generated or used during the study appear in the submitted article.

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Table 1. Concrete Model Parameters.

Parameter	Value	Parameter	Value
<i>A</i>	0.79	<i>T</i>	2.3, 3.5, 4.6 MPa*
<i>B</i>	1.6	<i>P<sub>crush</sub></i>	9.2, 13.8, 18.4 MPa*
<i>C</i>	0.007	<i>u<sub>crush</sub></i>	3.9, 5.8, 7.7x10 <sup>-6</sup> *
<i>N</i>	0.61	<i>P<sub>lock</sub></i>	800 MPa
<i>S<sub>MAX</sub></i>	7.0	<i>u<sub>lock</sub></i>	0.1
<i>D<sub>1</sub></i>	0.04	<i>K<sub>1</sub></i>	85000 MPa
<i>D<sub>2</sub></i>	1.0	<i>K<sub>2</sub></i>	-171000 MPa
<i>EF<sub>MIN</sub></i>	0.01	<i>K<sub>3</sub></i>	208000 MPa

\*For concrete strengths of 28, 41, and 55 MPa, respectively.

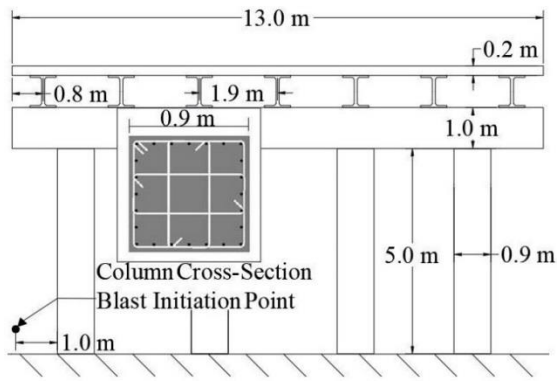


Figure 1. Elevation View of Bridge Pier.

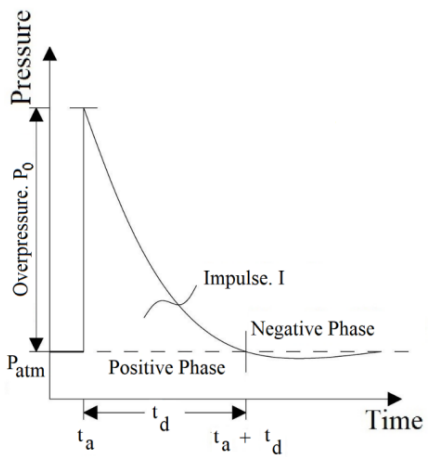


Figure 2. Typical Blast Wave Pressure Time History.



Figure 3. Experimental and FEA Results.

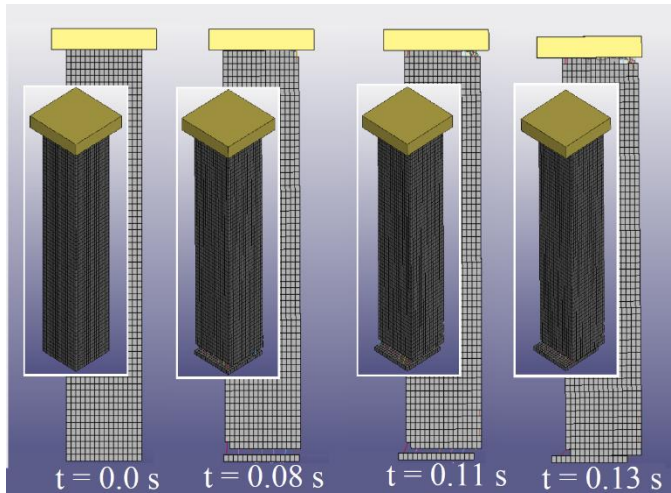


Figure 4. Typical Response of Column (Minimum Blast Load for Collapse).

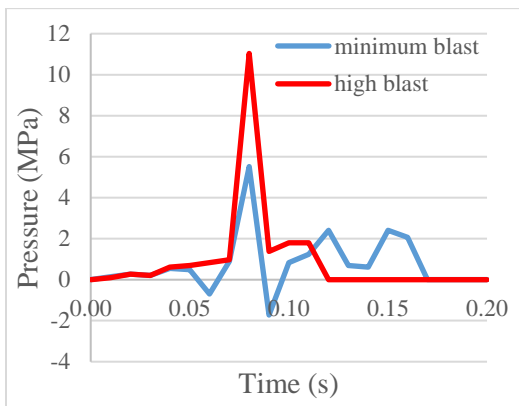


Figure 5. Typical Time-Pressure Relationships Experienced by Column.

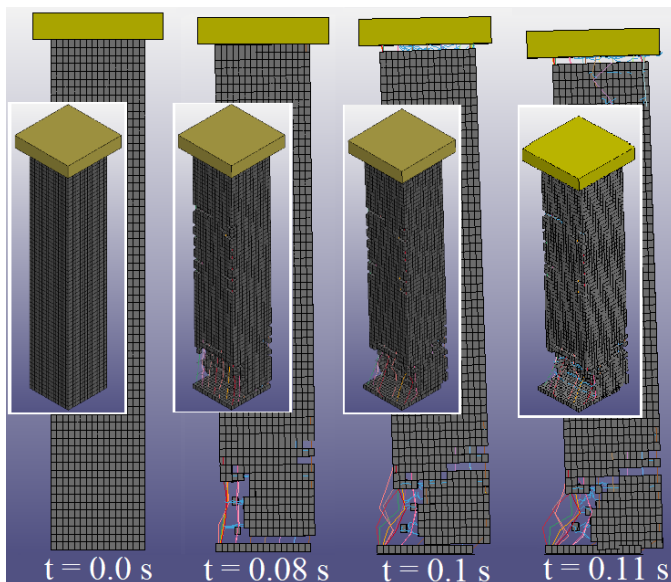


Figure 6. Typical Response of Column (High Blast Load).

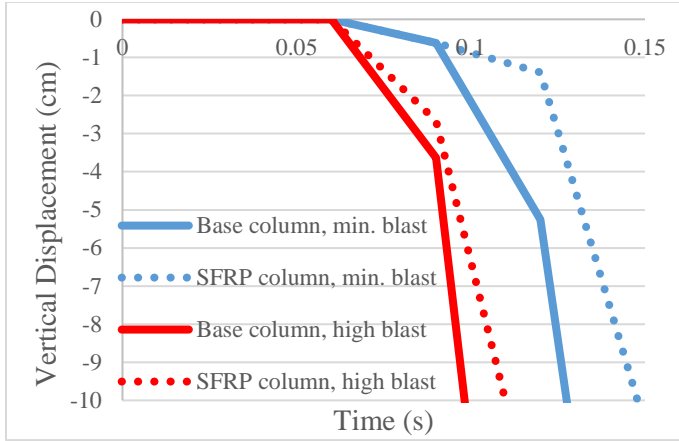


Figure 7. Vertical Displacement.

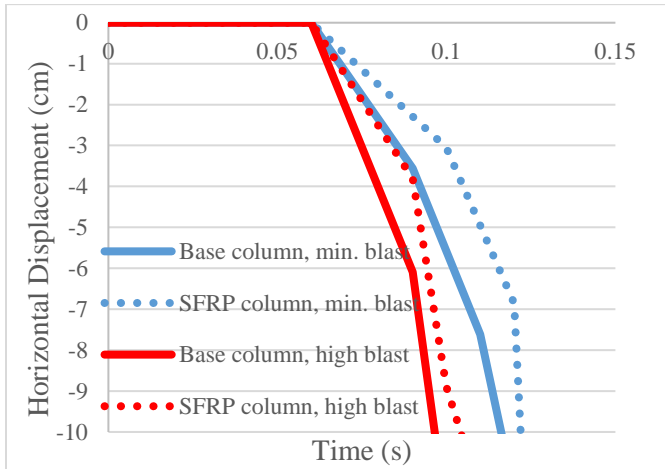


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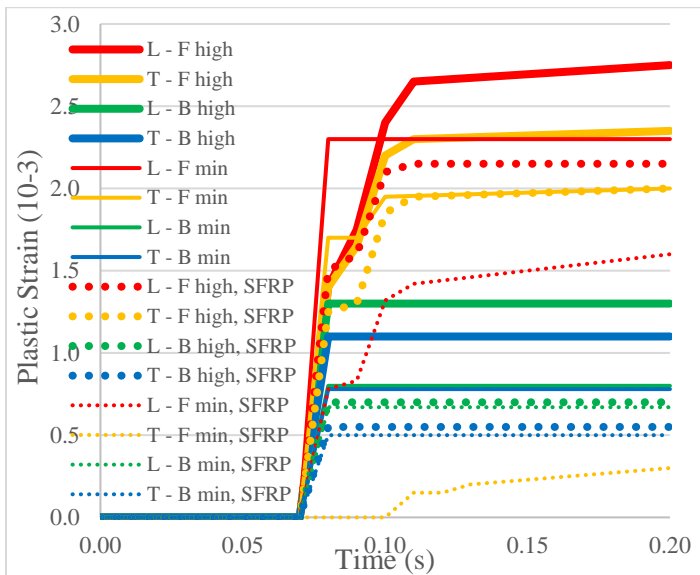


Figure 9. Reinforcing Bar Strains.

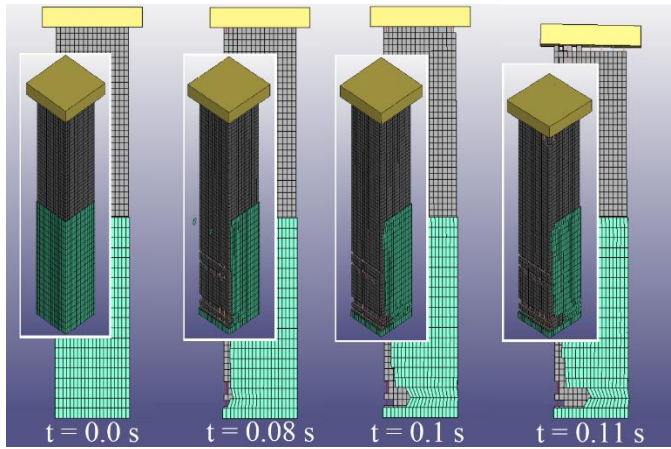


Figure 10. Typical Response of Column Wrapped with SFRP (Minimum Blast Load for Collapse).

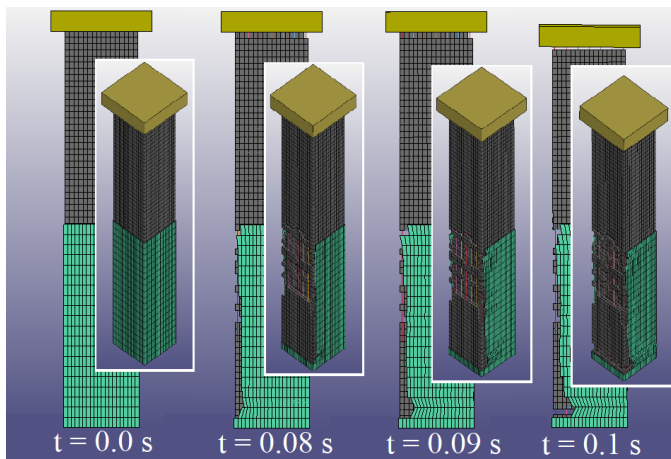


Figure 11. Typical Response of Column Wrapped with SFRP (High Blast Load).

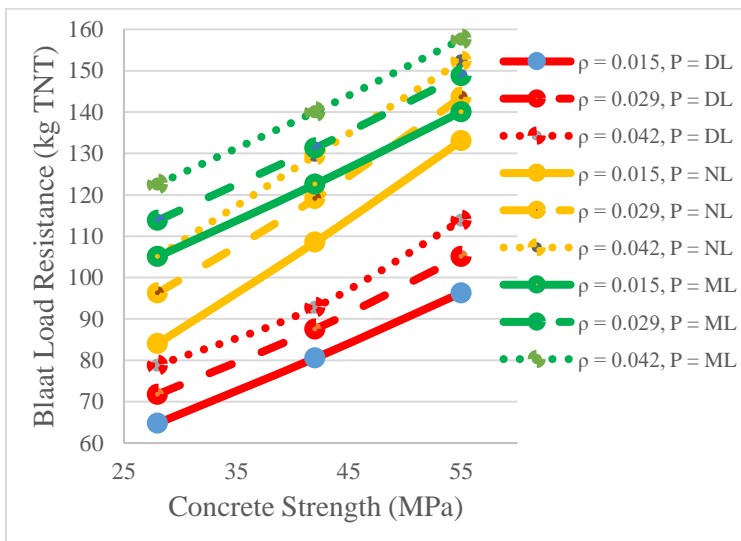


Figure 12. Column Blast load Resistance as a Function of Concrete Strength.

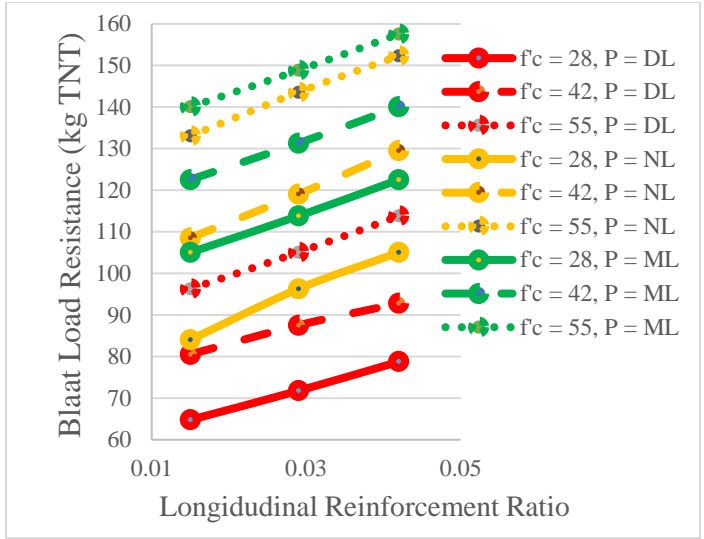


Figure 13. Column Blast load Resistance as a Function of Longitudinal Reinforcement Ratio.

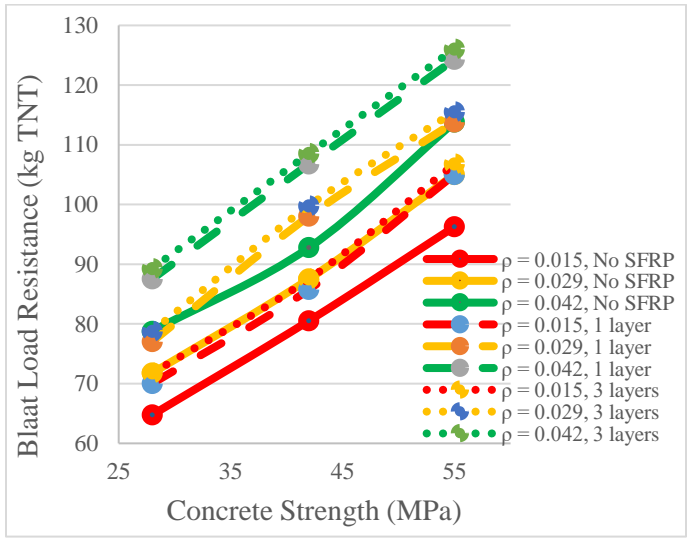


Figure 14. SFRP-Wrapped Column Blast Resistance.