An Analytics Approach To Reducing Hospital Readmission

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AN ANALYTICS APPROACH TO REDUCING HOSPITAL READMISSION

by

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DISSERTATION

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of Wayne State University,

Detroit, Michigan

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Chapter I Introduction

Hospital readmission is disruptive to patients and costly to healthcare systems. Unnecessary return to hospitals shortly after discharge has been increasingly perceived as a marker of the quality of care that patients receive during hospital admission (Chassin et al., 2010). About one in five Medicare fee-for-service beneficiaries, totaling over 2.3 million patients, are rehospitalized within 30 days after discharge, incurring an annual cost of $17 billion, which constitutes nearly 20% of Medicare’s total payment (Jencks et al., 2009).

However, it is reported by the Medicare Payment Advisory Commission (MedPAC) that about 75% of such readmissions can and should be avoided because they often result from a fragmented healthcare system that leaves discharged patients with preventable flaws such as hospital-acquired infections and other complications, poor planning for follow up care transitions, inadequate communication of discharge instructions, and failure to reconcile and coordinate medications (Medicare Payment Advisory Commission, 2007). Variations in both medical and surgical readmission rates by different hospitals and different geographic regions also indicate that some centers (or regions) perform better than others at containing readmission rates (Tsai et al., 2013; Jencks et al., 2009) Studies also show that the adjusted readmission rate in the US is among the highest ranking in comparison to European countries (Westert et al., 2002).

Hospital readmission rates have been identified as a main measure of quality of care received by patients (Friedman, Basu, 2004) since they are happened due to such factors as premature discharging process or inadequate access to care. More importantly, it is found that rehospitalization causes an unfitting share of costs for inpatient hospital cares.
In 2009, (Jencks et al., 2009) reported that 19.6% of Medicare fee-for-service patients discharged from a hospital were readmitted within 30 days, 34.0% within 90 days, and more than half (56.1%) within one year of discharge, collectively accounting for $15 billion of Medicare spending. And recently, based on Obama Care Rule (known as Patient Protection and Affordable Care Act or PPACA), about two-thirds (or 2,211) of U.S. hospitals have been penalized a cumulative $280 million (1%) in Medicare funds because of excess readmissions starting Oct. 1, 2012. This cut will grow to maximum of 2% for the 2014 program year and 3% for 2015 (Fiegl, 2012).

Generally, a readmission may be defined as a return hospitalization to a same (or different) acute care hospital following a prior acute care admission within a specified time interval. Although selection of a time interval can have an impact on rate of readmission, no standard time frame is used by all hospitals and various periods such as 14 days (Reed at al., 1991) or 90–180 days (Benbassat et al., 1995) have been considered. Nevertheless, the Veteran Health Administration (VHA) defines readmission rate as a proportion of patients who were readmitted to the acute care wards of a hospital within 30 days following the discharge with some exclusions such as patients died up to one day after discharge or patients with psychiatry, rehabilitation and hospice ward stays.

Another issue which makes the hospital readmission analysis rather complicated comes out from of the fact that not all readmission can be grouped as preventable. Although several studies have tried to define preventable readmission, still no census exists on how to systematically separate those readmissions that might be avoidable and those that might not (Stone, Hoffman, 2010) It is also found that lots of patient characteristics such as age, gender, race, financial condition and even illness type are
substantially related to patient risk of readmission (Soeken, et al., 1991; Boutwell et al., 2009). However there is still little support to effectively determine which patient factors result in a high risk of rehospitalization based on credible clinical criteria. And this issue is to be tackled in our research.

Basically one part of related literature involves providing interventions programs to reduce avoidable readmissions without a supporting theoretical or mathematical methodology as mentioned in (Demir, E., et al., 2009).

In contrast, there are some methodological studies that explore the readmission process with the help of a mathematical and/or statistical modeling approach. For example, (Cotter et al., 2012) proposed a framework based on transition models to model the risk of readmission for chronic obstructive pulmonary disease (COPD) patients in UK. They also presented a method to come up with suitable choice of a time window which defines readmission. Another study of older UK inpatients showed that the internationally-accepted LACE index (Length of stay, Acuity of the admission, Charlston co-morbidity index score, and Emergency department visits within six months) is a poor tool for predicting 30-day readmission according to logistic regression analysis (Cotter et al., 2012). In addition, (Norouzzadeh, S., et al., 2011) presented a comparative study of three classification methods with respect to the conventional LACE score and their proposed weighted LACE score, and demonstrated the superiority of theirs with experimental results.

In addition, effective October 2012, as directed by Patient Protection and Affordable Care Act (PPACA, also called Obamacare), the Centers for Medicare and Medicaid Services (CMS) started to cut reimbursement funds for hospitals that have excessive
30-day readmission rates for heart failure, myocardial infarction, and pneumonia patients. This included 2,213 US hospitals with approximately $280 million funds nationwide, which constitutes 1% of the total Medicare budget. Moreover, this cut will grow to 2% and 3% for FY 2014 and 2015, respectively. As a result, numerous intervention programs have been proposed by policymakers and healthcare organizations to reduce rehospitalizations and improve quality and access to care (Hansen et al., 2001).

While it would be perfect to include all patients in a transitional care intervention, due to their resource intensive nature on one hand and hospital supplies constraints on the other, it is inevitable to target and deliver such efforts to those subgroups that are at greater risk. Nevertheless, identifying patients at increased risk of readmission is challenging and calls for advanced analytics tools that help to stratify risk into clinically relevant classes and provide information early enough during the hospitalization.

Various methods have been proposed in recent years to predict hospital readmission but most of them do not yield acceptable predictive accuracy, or they are based on patient factors that are not typically collected during clinical care (Kansagara et al., 2011).

Furthermore, a few methods have tried to distinguish avoidable readmission from all other types of readmissions (Walraven et al., 2011), but it remains a disagreement how to systematically define and identify those readmissions that can be prevented based on credible clinical criteria.

Another important aspect of readmission studies is related to the choice of timeframe used to count the number of readmissions. Although the CMS establish 30-day cutoff point for the three acute conditions (heart failure, myocardial infarction, and pneumonia), researchers have considered other periods from two weeks (Reed, Pearlman, Buchner,
1991) to 180 days (Benbassat, Taragin, 2000) for certain surgical and medical conditions. Moreover, with the new chronic and surgical conditions to be penalized in the next few years, questions regarding the suitability of the 30 day time window remain to be explored.

1.2. Research background

Hospital readmission is disruptive to patients and costly to healthcare systems. During FY 2003-04 near one-fifth of Medicare beneficiaries—over 2.3 million patients—were readmitted within 30 days of discharge, yielding to a cost of $17 billion, which is about 20% of Medicare’s total payment. In 2005 the Medicare Payment Advisory Commission (MedPAC) reported that 17.6% of all-cause hospitalizations followed by readmissions in a 30-day period after discharge, 11.3% within 15 days, and 6.2% within 7 days. Studies also showed that adjusted readmission rate in US is among the highest rank in comparison to European countries (Westert et al., 2002).

Further, readmission is found to associate with health service access and quality of care (Kangovi & Grande, 2011). Patients readmitted to hospitals may experience premature discharge planning, poor coordination of care, and even erroneous diagnosis. Researches also indicate that increased 30-day risk-standardized readmission rates are connected with lower patient satisfaction (Boulding et al., 2011). Nonetheless, a large proportion of readmissions is obviously planned and deemed appropriate especially when they are followed by procedures or surgeries. And to date, there is no consensus on how to systematically separate among “bad” readmissions and those that might be advisable.

On the other hand, with publically reporting 30-day readmission rates, the Centers for Medicare and Medicaid Services (CMS) has begun comparing hospital’s performances
by their readmission rates on its Hospital Compare website. And as stipulated by §3025 of the Patient Protection and Affordable Care Act (PPACA, known as Obama Care Rule), medical centers with high readmission rates for acute myocardial infarction (AMI), heart failure (HF), and pneumonia have lost 1% of their Medicare budget starting Oct. 1, 2012. Unfortunately this included 2,213 US hospitals with approximately $280 million funds nationwide, and the cut will grow up to 2 percent for FY 2014 and up to 3 percent for FY 2015. As a result, about one-third of Michigan hospitals (55) were penalized near $14 Million in FY 2013 (Russell & Eller, 2013). Therefore numerous intervention programs have been emerged by policymakers and health care practitioners in the past 5 years to decrease readmissions and improve the quality of patient care.

Generally, a readmission (also referred to as re-hospitalization) is defined as a return hospitalization to a same (or different) care unit within a specific time interval, following a prior admission and discharge. Although selection of a time interval influences the rate of readmission, no standard time frame is yet adopted and various periods from 7 days to one year have been considered (Stone & Hoffman, 2010). Typically when it comes to acute care hospitalization, the calculation of readmission rate is adjusted with some exclusions. These may include admissions within 24 hours of discharge, patient stays with nursing home and rehabilitation wards, and patients died up to one day after discharge.

From a systems engineering viewpoint, there are lots of factors that drive readmission problem and make its analysis rather complicated. First, various risk attributes contribute to patient likelihood of readmission and they come from different levels of health care such as patient’s level (age), provider’s level (years of experience), or even facility’s
level (bed supply) risk factors. Also these tend to be varied substantially by geographic area and at different points in time—spatial and temporal variations (see Fig.1 and Fig.2).

Second, although not all readmissions are avoidable, policy makers assert that some types of services and procedures have excessive readmission rates thus hospitalization costs could be declined a lot if a higher quality of care were brought to patients throughout hospital stays or post-discharge settings.

Figure 1 Rate of readmission between Oct. 1, 2003 and Sep. 30, 2004.
In addition, different approaches of defining avoidable readmissions result in different rates of readmission and yet there is no agreement on a unified way of definition and also on strategies implemented to prevent such readmissions. Third, the time frame, which defines the readmission, is changed for different illness types and while this case has direct effects on computing the percentages of readmission, no systematic method is existed in the literature. Fourth, readmission depends directly on discharge organism in a health care system so the dynamics therein could affect or be affected by discharge changing aspects. At the same time, strategies addressing the readmission problem may involve a large part of organization such as operations, planning, and even finance department.
As mentioned, a number of intervention programs have been under way to reduce avoidable readmissions across the nation. Some commonly advocated strategies include patient education about their medications, patient-centered discharge instruction, follow-up telephone calls, and post-discharge home visits. When designed by randomized controlled trials, such interventions were easily evaluated and found to be really effective as compared to observational studies in a variety of patient populations. (Bradley et al., 2012; Hansen et al., 2011). However due to budget limitations, there is a need to mark patients with high risk of readmission who benefit the most from implementing such provisions. This is typically done using predictive models that either try to classify high-risk patients with the help of learning algorithms, or produce a likelihood score for change of getting readmitted with some probability.

The former class utilizes supervised and/or unsupervised approaches without any assumptions about the underlying mechanism that generates the data, while the latter basically uses statistical models with data assumed being stemmed from a given stochastic data model. Each class of methods has its own advantages and drawbacks in terms of misclassification errors as well as specific assumptions and computational difficulties they pose. Overall it is found that most such predictive models perform poorly in terms of discrimination power (Kansagara et al., 2011). Thus one part of the current study will be devoted to propose better prediction models that alleviate such pitfalls in the literature. Moreover, the existing methods cannot be directly applied in some specific circumstances within the readmission problem. Examples may include longitudinal observations when patient information is censored before the end of study period,
repeated measure data with imbalanced class problems, and multilevel competing risk models with time-dependent covariates.

Apart from various predictive analytics that can be thought for the readmission problem, the literature also lacks an optimization framework to deal with operational costs and benefits that intervention programs can cause in a medical center. Such approaches would provide insights to determine better ways to operate admission/discharge activities and target business objectives of the health care system while satisfying some operational constraints. Thus another part of current study would pertain to developing a mathematical programming framework to optimally allocate intervention programs to patients most prone to readmission in a medical facility.

In my research we will use Veteran Health Administration (VHA) database systems to aggregate required information from different health care levels such as patient demographic, general medical status, and also provider data. By doing this, my approach would better capture both patient-based and population-based variations of readmission.

1.3. Research objective

The key purposes of this research are listed as follows:

1. Tackle the difficulties around the time frame that defines readmission. I seek to propose an approach based on phase-type distribution and continuous-time Markov chain to optimally define time interval for readmission (Predictive Analytics).

2. Combine population-based and individual-based risk prediction models in order to capture the inherent variations of readmission caused from both patient population and single’s past history of readmission. By this, we provide reliable initial estimate of readmission for each patient based on characteristics of the population he/she
belongs to and then we can personalize it for one’s own behavior with incorporating risk factor changes over time (Predictive Analytics).

3. Formulate the readmission problem within an optimization framework that dynamically uses predictions from 2 to find the best way of allocating the interventions to a set of patients. That way, by obtaining data in say weekly schedule we can analytically reflect migration of patients in and out of a hospital to the readmission intervention planning (Prescriptive Analytics).

We plan to perform lots of descriptive analytics too by summarizing and plotting variables in the past and present VA datasets. This is particularly helpful to find basic questions about the patient populations under study: Are they rather old? What is the sex ratio among them? What types of diseases they are most prone to?

Moreover, some research questions that I would like to address in this study are as follows:

1. What patient characteristics contribute the most to the chance of being readmitted? Are provider or facility level factors related to the risk of readmission? Do readmission variations of any patient-level risk factors change at different providers or facilities? If these are the cases, at which levels of risk factors is the readmission rate higher?

2. Are the patients more likely to be readmitted in the first week after discharge? What are the most frequent diagnoses that patients get readmitted after? Do the odds of readmission for those diagnoses change with patient demographic variables and timing of readmission?
3. How can we distinguish between advisable and preventable readmission in administrative data systematically? To what extent does preventability alter the true rate of readmission and hospital profiling method?

4. What is the effect of intervention programs on reducing readmission rates? Does this effect vary among pre-discharge, bridging, and post-discharge interventions? Which type of intervention is most useful for VA patients diagnosed for heart failure, acute myocardial infarction, and pneumonia (these are common illnesses with the highest readmission rate according to CMS)?

5. What is the discriminative ability of different groups of risk factors, such as demographic variables, SES attributes, utilization variables, and laboratory measures, on predicting high-risk patients? Does this ability change for all-cause and specific-cause readmission risk prediction?

6. Statistically, how much change in readmission prediction we would expect in case of repeated measure and/or censored observations? How much variation do different levels of health care hierarchy such as patient level, provider level, and facility level account for?
We propose a feedback loop analytical framework that includes the key objectives for this research.

**Descriptive Analytics**
- Identify cohort of interest with ICD-9-CM codes. Label readmission indices.
- Aggregate patient-level data with provider/facility tables. Do data pre-processing and summarizing.
- Recognize preventable readmissions by an analytical method and exclude others.

**Predictive Analytics**
- Develop population-based models for readmission timing and occurrence.
- Develop individual-based models for readmission timing and occurrence.
- Propose a hybrid approach with population-based and individual-based models.

**Prescriptive Analytics**
- Identify most common faults causing readmission: inadequate follow-up, etc.
- Optimally assign pre-, bridging, and post-discharge intervention programs to given set of patients.
- Dynamically update patient risk prediction model and intervention allocation programming.

*Figure 3 Proposed Framework*
In this research, we propose a risk prediction model based on hierarchical nonlinear mixed effect framework to extract significant prognostic factors associated with patient readmissions that mainly caused by patient non-compliance to the medication instructions. The novelty of our method is to directly incorporating patients’ history of readmissions, along with other patient characteristics, into the modeling framework thus enabling one to explain both patient and population based variations of readmission process at the same time. Moreover, we propose a predictive analytics framework that enables medical decision makers to characterize and (more accurately) predict avoidable readmissions, and to investigate the effects of different patient risk factors on the likelihood of rehospitalization. The goals of our study are three-fold: 1) to develop and internally validate an administrative algorithm for characterizing avoidable readmissions from all types of readmissions, 2) to address the difficulties around selection of an appropriate timeframe that defines readmissions for chronic conditions, and 3) to create and validate a simple and real-time readmission risk prediction model that can produce more desirable prediction accuracy than the literature. The proposed methods and tools are evaluated using a wide range of electronic health records from four Veteran Affairs (VA) hospitals in the State of Michigan.

1.3. Dissertation Organization

The dissertation is organized as follows. In chapter 2, first we propose an algorithm for identifying potentially avoidable readmissions and then we discuss about determining readmission time interval for chronic conditions. Next, we introduced phase-type distribution and phase-type Survival Forest for predicting the risk of readmission and
then, in the later part of the Chapter 2 we state some performance evaluation measures.

In Chapter 3, we first describe the data source and the attributes, which is used for our research. In addition, the data preprocessing is presented completely. Next we determine the potentially avoidable readmissions rates for the given data from VA. With the help of proposed method in chapter 2, we predict the risk of readmission. Next, we do some descriptive analytics and compare different readmission risk prediction models with our proposed model. Conclusions and future studies are presented in Chapter 5 of the dissertation.
Chapter II Methods and Measures

In this section, we first describe an algorithm built on administrative data to characterize avoidable readmissions from all outcomes. Then an analytical approach based on Coxian Phase type (PH) distributions is introduced to determine the optimal readmission time interval for chronic diseases and particularly COPD patients.

2.1. Identifying potentially avoidable readmissions

One of the main difficulties that makes the study of hospital readmission rather sophisticated is that no consensus yet exists on how to separate among so called “planned” readmissions (e.g., scheduled at or soon after the time of discharge) and those that might be prevented by implementing better transitional care programs. Different methods consider distinct outcomes and result in different readmission rates. Here we classify the existing approaches into two broad categories:

- Methods designed to detect and exclude planned hospitalizations from the outcome of interest. Examples in this group include the well-known CMS method (Horwitz et al., 2015) and SQLape (Striving for Quality Level and Analyzing of Patient Expenses) (Halfon et al., 2002), which is a validated hospital comparison system practiced in Switzerland.

- Methods intended to label avoidable readmissions from all index hospitalizations, such as 3M Health Information Division Potentially Preventable Readmission measure (Goldfield et al, 2008).

The CMS approach takes specific index stays and uses unplanned all-cause readmission rate as the primary outcome by removing all non-acute readmissions as well
as readmissions for maintenance chemotherapy. It employs AHRQ (Agency for Healthcare Research and Quality) Clinical Classification System (CCS) to identify planned procedures that contain an inpatient stay, along with the conditions that are acute or are complications of care and associated with the planned procedures. Also consistent with National Quality Forum (NQF) standards, the approach performs risk adjustment for case mix (patient comorbidity) and service mix (types of conditions/procedures cared for by the hospital) with the help of CMS Condition Category groupers.

The 3M approach, on the other hand, considers all types of index hospitalization then decides on whether a readmission is avoidable with regard to clinical relationships between the reasons of admission and readmission. To this end, All Patient Refined Diagnosis Related Group (APR DRG) codes are first utilized to classify the patient cohorts; then a group of physicians evaluate the association between the initial admission and its following returns, and define preventable readmissions as those returns having a clinical relevance with the first hospitalization. Moreover, the approach makes use of APR DRG based Severity of Illness (SOI) measures to adjust for case mix risk factors.

Both approaches are built (and validated) on administrative data, and they are mainly used for the purposes of (1) profiling hospitals with respect to their readmission rates and (2) adjusting Medicare or Medicaid payments to low-performing medical centers. However, according to a recent study in the VHA (Mull et al., 2013), they show only a moderate correlation in specifying the readmission rates, which is found related to the preventability element of the 3M method.

In this study, since our goal is more to develop and validate a risk prediction model that can be used for clinical applications (rather than hospital profiling and payment
adjustment), we derive a hybrid approach adopting both the CMS and 3M rationales to choose from the patient outcomes. In a nutshell, we first apply the CMS method to exclude those planned procedures that are followed by a non-acute or a non-complication of care condition; then the 3M procedure is implemented on the remaining indices in order to extract potentially avoidable readmissions (PARs). However, we modify the exclusion criteria of both methods and implement VHA definitions of eligible discharge.

To increase the overall precision of the proposal, we also got help from three reviewers to judge all cases identified, after completing each constituent algorithm. Moreover, instead of the APR DRG system, the newly-developed Diagnostic Cost Group Hierarchical Condition Category, version 21 (DCG/HCC v21) was utilized to assess the clinical relationship between each readmission and its initial admission(s) (Pope et al., 2004). We chose the DCG/HCC risk adjustment system because 1) it is a part of models that have been used and evolved over two decades of research; 2) it has special adjustments for elderly beneficiaries as well as patients with chronic conditions; and 3) it is recalibrated regularly according to recent modifications on diagnosis and expenditure data.

The algorithm, which we call Potentially Avoidable Readmission (PAR), can then be stated as follows:

**Step 1** (general inclusion/exclusion)

I. Identify HF, AMI, PN, and COPD cohorts based on principal (or secondary) discharge diagnoses, and eliminate all other conditions. Merge records of the same patient if he/she had multiple hospitalizations on the same day to the same medical unit. This applies to both medical and surgical patients.
II. Establish readmission time interval (henceforth $T$) and categorize each entry as either admission or readmission. Also, define eligible admissions as all admissions that are at risk of having a readmission.

III. Exclude:

a) From the admission set, cases whose discharge status is “death,” since they cannot have any readmission. These correspond to stand-alone admissions.

b) From the admission set, cases whose discharge status are “transfer” to another acute care facility, except the four hospitals studied. The reason is that the hospital cannot affect a patient’s consequent care under such circumstances. If transferred among the four hospitals, however, the final discharging hospital is considered responsible for any readmissions.

c) From the admission set, cases whose discharge status is “against medical advice.” Because in such cases, the planned treatment(s) could not be fulfilled and thus they do not represent a quality-of-care signal.

d) From the readmission set, those entries that fall within 24 hours of their prior index discharge. This is consistent with the VHA operations policies.

e) From the readmission set, cases in which any of the CMS planned procedures are conducted if not followed by an acute or a complication-of-care discharge condition category. Examples of such procedures include peripheral vascular bypass, heart valve, kidney transplant, mastectomy, colorectal resection, and maintenance chemotherapy.
f) From the readmission set, AMI patients hospitalized for a percutaneous coronary intervention (PCI) or coronary artery bypass graft (CABG), except those that are diagnosed for HF, AMI, unstable angina, arrhythmia, and cardiac arrest.

g) From both admission and readmission sets, hospitalizations in long-term care, palliative care, nursing home, aftercare of convalescence, psychiatry, rehabilitation, and hospice wards; or for fitting of prostheses and adjustment devices.

h) From both admission and readmission sets, stays for special conditions with high mortality risk, for which chances of post-discharge death is much higher than chances of being readmitted. These include, but are not limited to, patients with malignant neoplasm without specification of site; and medical patients with cancers of breast, skin, colon, upper digestive tract, lung, liver, pancreas, head, neck, brain, and fracture of neck of femur (hip). This is consistent with the CMS approach.

i) From both admission and readmission sets, records that are related to major or metastatic malignancies, multiple trauma, burns, neonatal, obstetrical, Human Immunodeficiency Virus (HIV), and eye care. The rationale is that these conditions usually require specialized follow-up cares and are often not avoidable. This is consistent with the 3M approach.

j) From both admission and readmission sets, patients not enrolled in the VA and thus lacking sufficient historical data for the 12 months prior to the index admission. The logic is that the information is required to adjust for the case-mix and comorbidities.
k) From both admission and readmission sets, records with inconsistent and/or error components such as age and gender discrepancies, invalid HCC assignment, discharge date that preceded the admission date, disagreements between the patient’s VA status and its service-based attribute values, hospitalizations charged for less than $200 or greater than $4 million, and records with distances longer than 3000 miles.

IV. Calculate eligible admissions as all records remaining in the admission set. Note that, situations described in a), b), and c), i.e., “death,” “transfer,” or “against-medical-advice” may happen to both admission and readmission entries.

Step 2 (labeling PARs)

V. Mark records from the readmission set that have a clinical relationship with their initial admissions as defined by one of the eight following categories:

a) Readmissions for an ambulatory care-sensitive condition as specified by the AHRQ (Agency for Healthcare Research and Quality).

b) Medical readmissions for repeated happening or extension of the reason for the initial (or a closely-related) condition.

c) Medical readmissions for an acute decompensation of a chronic condition that relates back to the care given in the course or immediately after the initial admission (e.g., a return hospitalization for diabetes by an initially diagnosed AMI patient).

d) Medical readmissions for acute medical complications acquired during or soon after the first admission (e.g., a readmission for addressing a urinary tract infection of a patient originally hospitalized for hernia repair).
e) Readmissions for a mental health or substance abuse condition that follows an admission for a non-mental health or non-substance abuse condition.

f) Readmissions for mental health or substance abuse reason following a hospitalization for a mental health or substance abuse reason.

g) Surgical readmissions to deal with repeated happenings or extensions of the condition causing the initial hospitalization (e.g., a readmission for appendectomy surgery of a patient who was initially admitted for abdominal pain and fever).

h) Surgical readmissions to tackle a medical or surgical complication resulting during the initial admission or in the post-discharge course (e.g., a readmission for treating a post-operative wound resulting from an initial hospitalization for a bowel resection).

**Step 3 (clinical panel review)**

VI. All exclusions from step 1 and marked PARs in step 2 are reviewed by three physicians, and final decision about the outcomes was made by a majority of vote scheme.

**Step 4 (calculating PAR rate)**

VII. Define a PAR series as a sequence of one or more PARs that are all clinically associated with a similar initial admission. In this way, the succeeding PARs are always assessed for having a clinical relationship in reference to the very first admission (which starts the sequence), not with the intermediate PARs. As a result, the total time interval encompassing a PAR series can be larger than $T$. 
VIII. Update the eligible admission set by reclassifying cases in the readmission set that are NOT found to be PARs (i.e., not having clinical relationship with their prior admissions) and at the same time, do not fall in “death”, “transfer”, or “against-medical-advice” categories.

IX. Calculate PAR rate as \[ \frac{\text{#PAR Series}}{\text{# Eligible Admissions}} \].

The DCG/HCC system is used throughout the algorithm to assess the clinical association between an initial admission and its PAR series. In other words, we first apply the CMS HCC model to assign HCC codes for all indices; then the reviewers examine the HCC codes of an initial admission and all of its related PARs to judge whether the readmission(s) could have been avoidable. If available, we also take into account other sources of information such as clinical visits between admission and readmission, and communication with the patient, patient’s family and primary care physician assigned, to help on the avoidability assessment of the PARs.

The readmission time interval introduced in II is defined as 30 days for HF, AMI, and PN cohorts. For the COPD, we follow an analytical approach that is outlined in the next section.

2.2. Determining readmission time interval for chronic conditions

It is clear that, similar to the type of readmission (planned vs. avoidable), the length of time window between the dates of initial discharge and index readmission affects the ratio of avoidable readmissions (see sections VIII and IX in the PAR algorithm). The longer the interval is the more readmissions will be recognized and the more money the insurer could save under the bundled policy; however, the chances that a readmission has
a clinical relevance with its initial admission become diminished. Although the CMS and health policy makers adopt a 30-day time window for profiling hospitals and public reporting, other intervals from two weeks (Reed et al., 1991) to 180 days (Benbassat et al., 2010) are examined in different situations from certain types of surgery to a specific clinical condition. Researchers also raise the issue of improper interval selection in the literature (Hasan, 2011). In this study, to decide on the appropriate timeframe for COPD patients, first we examine the patterns of empirical readmission rates over days after discharge and recommend a graphical-based estimate; then we develop an analytical framework founded on Coxian phase-type distribution to determine the optimal cut off time defining the readmission.

2.2.1. Graphical based approach

The trend of COPD readmission rate over days following discharge is shown in Figure 4. Consider that the vertical axis displays percentage of patients not readmitted. As shown, the rate is high in the first weeks after discharge, then it levels off and becomes constant, before rising again near 60 days. The rate of (all-type) readmission is 17.3% for the CMS-endorsed 30-day time window. However, inspecting the plot, we find that the slope of the readmission curve becomes stable around the 39th day, so we suggest that 39-day interval may be more appropriate choice for counting COPD readmissions. We believe this finding is also clinically justifiable because chronic conditions, as opposed to acute conditions, are getting worse over an extended amount of time so those readmissions that occur even after the 30th day may also be associated with the quality of the “inpatient” care and should thus be considered for transitional care intervention programs.
2.2.2. Phase-type distribution

Phase-type (PH) distributions comprise a rich class of probability distributions that have been exploited extensively in various applications of stochastic modeling such as financial engineering, teletraffic modeling, drug kinetics, biostatistics, and survival analysis.

Figure 4 Percentage of COPD patients not readmitted

The distribution is created by one or more inter-related Poisson processes on nonnegative real numbers, which can be represented as the time to reach an absorbing state in a finite-state continuous time homogeneous Markov chain. Despite its prevalence in other areas, the number of applications of PH distribution in healthcare literature is limited, with most publications focusing on modeling patients’ length of stay (Fackrell, 2009).
Inspired by the observations from Figure 1, we assert that the rate of COPD readmission is not constant and changes over time. Further, using all-cause inpatient data from the same VA facilities, it was previously demonstrated that the (mean) hazard of readmission over time is influenced by a set of relevant patient factors including source of patient admission and treatment specialty (Shams et al., 2014). Therefore, it is desired to define the readmission timeframe in accordance with avoidability level and representativeness of quality care. We also recognize that the determination of the interval should not be based on the (instantaneous) risk or hazard of readmission, as the hazard (in the terminology of survival analysis) is a time-dependent conditional probability function that changes with both time and the patient’s case mix. On the other hand, since bias may be introduced when using the graphical inspection method, the approach taken should be able to objectively stratify the patients into clinically distinct groups according to avoidability strength of their readmission.

Considering these characteristics, here we undertake a patient flow approach and develop a conceptual framework for the movements of patients after release from the hospital (see Figure 5). It is assumed that discharged patients travel between two major states (Short-Stay and Long-Stay) in their community before being returned to the hospital. In other words, patients begin their post-discharge period from the Short-Stay (SS) group consisting of m sequential transient phases; then they are either readmitted to the hospital at the rate of $\lambda_{ss}$ or move to the Long-Stay (LS) group with rate $\lambda_m$. Patients entering in the LS group remain another $r$ (transient) phases in the community before going back to the hospital at the rate of $\lambda_{LS}$. Here, consistent with the CMS and MedPAC logic, we ascertain that readmission from the SS group is a marker of poor quality of
inpatient care possibly because of premature discharge and poorly-designed process of inpatient care, whereas readmission from the LS group represents deficient quality of post-acute and outpatient follow-up care. Note that the rates are not identical within or between the two groups.

The current framework results in a special case of order \(m + r\) Coxian PH distribution, which is represented by an absorbing continuous-time Markov chain (CTMC) with \(m + r\) transient states and one absorbing state (Hospital). Then the dynamics of the underlying finite-state stochastic process \(\{X(t); t \geq 0\}\) is governed by the transition intensity matrix \(A = \{\alpha_{hj}\}; h, j \in E\) where \(E = \{1, 2, K, m + r\}\) and

\[
\alpha_{hj}(t) = \lim_{\Delta t \downarrow 0} \frac{P[X(t + \Delta t) = j | X(t) = h]}{\Delta t},
\]
\[
\alpha_{hh}(t) = - \sum_{h \neq j} \alpha_{hj}(t).
\]

Hence, the random variable time to readmission \(T\) is equal to the time spent in the above CTMC until absorption in the Hospital state, which is also known as the sojourn time (Stroock, 2005). In this case, the probability density function \(f\), the survival function \(S\), and the \(k\)-th noncentral moment of \(T\) can be expressed by

\[
f(t) = \pi \exp(Qt)(-Q1)
\]
\[
S(t) = \pi \exp(Qt)1
\]
\[
m_k = (-1)^k k! Q^{(-k)}1, \quad k = 1, 2, \ldots
\]
Figure 5. Markov model for movements of COPD patients after...
where $\pi$ is the row vector of the initial probabilities over the transient states, $Q$ is the $(m+r) \times (m+r)$ transient partition of the intensity matrix, and $I$ represents an $(m+r) \times 1$ column vector of 1’s. Here, $\exp(A)$ denotes the matrix exponential of a square matrix $B$ (Golub, Van Loan, 2012). Based on the transition flow diagram shown, the Coxian PH distribution is represented by $PH(\pi, Q)$ where $\pi = (1, 0, K, 0)$ and $Q = \{q_{h}\}$ can be simplified as:

$$q_{h,h+1} = \lambda_{h}; \ h = 1, 2, K, m + r - 1$$
$$q_{h,h} = -\lambda_{h}; \ h = \{1, 2, K, m - 1, m + 1, m + 2, K, m + r - 1\}$$
$$q_{m,m} = -(\lambda_{SS} + \lambda_{m}); \ q_{m+r,m+r} = -\lambda_{LS}.$$

(5)

It is worth mentioning that the actual states of the Markov model are not observable; that is, we do not know the state (SS or LS) from which the patients absorb (readmit) to the hospital. In addition, the phases within each major state (SS and LS) do not carry any practical interpretations, but time spent in each phase follows an exponential distribution. Therefore, the PDF of time-to-readmission (2) can be viewed as a mixture of two generalized Erlang distributions (McLachlan, Peel, 2004) and then is reduced to

$$f(t) = pf_{SS}(t) + (1 - p)f_{LS}(t)$$

(6)

where $f_{SS}$ and $f_{LS}$ are the PDFs of the time-to-readmission for the Short-Stay and Long-Stay groups, with shape parameters $m$ and $m + r$ respectively, and $p$ is the probability of a patient being in the Short-Stay group, which can be obtained by

$$p = \frac{\lambda_{SS}}{\lambda_{SS} + \lambda_{m}}.$$

Following the methods discussed, we propose that the optimal cut-off point for the readmission time window is the point that separates the two components in (6), which, as
mentioned earlier, are corresponding to the readmission from inpatient and outpatient care spells one-to-one. Thus, the solution $t^*$ to

$$p f_{ss}(t) = (1 - p)f_{ls}(t)$$  \hspace{1cm} (7)$$

will give the optimal readmission timeframe. In order to solve (7), we need to estimate the $2(m + r) - 1$ unknown parameters in (5) using approaches such as maximum likelihood (Asmussen, Nerman, Olsson 1996), moment matching (Johnson, 1993), or probabilistic clustering (Reinecke, 2012) that best fit with empirical data. Observing the time to readmission data $t = (t_1, t_2, \ldots, t_N)$, in the current paper, we use the EM (Expectation-Maximization) algorithm to maximize the general log-likelihood function

$$\sum_{i=n}^{N} \log \left( \pi \exp(Qt)(-Q1) \right)$$

with EMpht software (Asmussen S EMpht software, 2013). Further, by altering the number of phases, we select the models that best compromise model parsimony and goodness of fit based on both Akaike’s Information Criterion (AIC) (Akaike, 1974) and Bayesian Information Criterion (BIC) (Schwarz, 1978).

### 2.3. Predicting potentially avoidable readmissions

In the interest of reducing avoidable readmissions, it is necessary to note that in most cases, including all patients in the intervention programs is neither possible nor economically feasible. Thus to exploit the full potentials of such plans and raise their sustainability, it is beneficial to target patient subsets that are at higher risk of being readmitted. In this regard, predictive modeling approaches turned out to be promising not only in readmission risk prediction models, but also in other healthcare research areas such as hospital profiling based on patient health outcomes (Krumholz et al., 2006),
chronic disease management programs (Bayerstadler et al., 2013), and patient no-show problems (Alaeddini et al., 2011). Employing advanced statistical and/or machine-learning algorithms, such models typically try to predict the probability of an outcome given a set amount of health data including administrative, claim, or even medical laboratory data.

Generally, risk of readmission needs to be assessed in two different episodes of the intervention programs, namely, pre-discharge and post-discharge. In the former, controlled variables that can be reasonably achieved before hospital discharge (for instance initial diagnosis) is fed into the model and the results are used to identify high-risk subgroups to receive the pre-discharge interventions like patient education and medication reconciliation. The latter, in contrast, make use of relatively all captured information such as LOS of the index hospitalization or principal diagnosis at discharge, and pinpoint high-risk cohorts to be assigned to post-discharge interventions like follow-up telephone calls and timely ambulatory visits. Also according to the type and timing of data gathered, predictive models can be applied for either profiling hospitals based on rate of readmission or predicting the chance of rehospitalization for a given patient.

Suppose $D$ and $\delta$ denote the time to readmission and the readmission status ($1=$ readmitted within $D$ days of the discharge, $0=$ Otherwise). Two modeling families with distinct objectives can be thought of for predicting patient readmission. The first group, which we call classification models, focus on readmission indicator $\delta$ and try to estimate it by first learning an algorithm based on inputted features and known class labels. These methods mostly use algorithmic models and treat the data mechanism as unknown (black box). Such models are usually prone to overfitting the training dataset in the case of small
sample sizes and/or repeated measurements. Nonetheless, they are computationally fast and easy to implement with minimal assumptions about the underlying mechanism that generates the data.

The second group, which we name timing-based models, concentrate on \( D \) and try to relate some of its probability functions to a given set of covariates in parametric (accelerated failure time models) or semi-parametric (proportional hazards models) fashion. As opposed to the first class, these methods are rather data models: the parametric timing-based methods have distributional assumptions for \( D \), and the semi-parametric ones have proportionality assumptions of the covariate effects. Nevertheless, they are capable of dealing with small (to medium) samples and also are able to update readily to take in new observations with minimum structural changes. In addition, models of this class have nice probabilistic interpretations of the outcome and they can incorporate correlations among the observations in the modeling process. Examples of the first group in readmission studies includes logistic regression (Shulan, Gao, Moore, 2013), random forest (Au et al., 2012), and support vector machines (Zhang et al., 2013), while the second group includes the Cox proportional hazard model (Hernandez, 2010), and the lognormal frailty model. Although each model has its own merits and specific applicability, overall, it is found that most of the described techniques perform poorly in terms of discrimination power and predictive accuracy.

Besides, according to current problems in readmission reduction programs, no consensus exists on the chosen set of patient (and system) factors that deemed related to the likelihood of readmission. This usually happens in studies comprising dissimilar health care settings (e.g., Medicare versus private health insurance) or diverse patient
populations (e.g., VA versus Non-VA). For instance, in a study of UK inpatients, the popular LACE measure (Length of stay, Acuity of the admission, Charlson comorbidity score (Charlson et al., 1987), and Emergency department visits within six months) which works well in a number of UK populations, is found to be mediocre in predicting 30-day readmission rates. Therefore, we believe that in our study, a data-driven patient-centered approach should be developed to guide the decisions upon the readmission intervention programs. To this end, we do not impose a priori candidate variables to the modeling process nor do we limit our analysis to the previously-selected risk factors from other studies.

Beyond these aspects, in order to fill the gaps in the literature and satisfy specific requirements of our modeling environment, we determined that a desired PM proposal should:

- Be able to handle censored observations, which are common in time-to-event data.
- Have the means to deal with repeated measure and recurrent event cases that may happen in longitudinal event history analysis.
- Incorporate patients’ past history of readmission into the modeling framework.
- Carry information about the timing of readmission.
- Manage many relevant risk factors without having computational or inferential problems such as overspecification or multicolinearity.
- Not be overly complex but should be computationally effective and easy to implement.
- Be as stable as possible in a complex data environment.
• Discriminate very high from very low risk patients and be comparable (or superior) to the existing methods in terms of such performance indices as $c$-statistics.

To fulfill the mentioned criteria, as well as to take advantages of both data models and algorithmic models, we propose our modeling methodology in the next section.

2.3.1. Phase-type Survival Forest

Decision trees are powerful and flexible non-parametric classifiers that use *inductive* inference for exploratory knowledge discovery. Due to their simple-to-comprehend and intuitive representation of information, decision trees have gained lots of attention in many disciplines such as computational biology, health informatics, medical imaging, and biomedical engineering (Breiman, 1993). A survival tree (Davis, Anderson, 1989) is a special kind of classification and regression tree (CART) for survival data that partitions the covariate space recursively to build groups (nodes in the tree) of subjects that are homogeneous with respect to the outcome of interest. This is typically done by maximizing a measure of node homogeneity like Wasserstein metric between the survival functions (Gordon, Olshen, 1985) or logrank statistics (Ciampi et al., 1986). A regular algorithm begins at the root node with all records and exhaustively searches all potential binary splits with the attributes, then picks the best one according to a splitting criterion such as a homogeneity measure. However, this process may lead to a large tree that usually overfits the data. To alleviate, a pruning mechanism is employed to find a subtree of appropriate size, or alternatively an ensemble approach (such as bagging or random forest) can be worked with which avoids the problem of selecting a single tree. Random Forest (Breiman, 2001) is a popular ensemble method that grows many (de-correlated)
classification trees by bootstrapping a training sample and then producing a label that is
the mode of all votes from the individual trees.

Following what was proposed, here we develop a special case of Breiman’s RF, a
phase-type survival forest (PHSF), that 1) uses the PH likelihood (with censored
observations) as its splitting criterion for each tree grown, and 2) deals with repeated
measure and recurrent readmission situations by performing bootstrap sample at a subject
(patient) level.

• **Splitting criterion**

  We chose minimization of the weighted average information criterion (Wu,
Sepulveda, 1998) as the splitting criterion to induce individual trees. WIC is a weighted
average of BIC and bias-corrected AIC (Hurvich, Tsai 1989) which works better than (or at
least as well as) other criteria in both small and large sample sizes. Recalling (2) and (3),
the full log-likelihood function with censored observations becomes

\[
L = \sum_{i=1}^{N} \alpha_i \log(f(t_i)) + (1 - \alpha_i) \log(S(t_i)),
\]

where \(\alpha_i\) is an indicator which equals 1, if \(t_i\) is a complete time for the \(i\)-th
hospitalization, and becomes zero if \(t_i\) is a censored case (that is, no readmission occurs
before the end of study). Notice that, censorship may occur for the three acute conditions
(and the COPD) if no readmission is seen within 30 (or \(T\) days of discharge. The WIC is
calculated as

\[
WIC(d) = -2L + d + \left\{ \frac{d \left[ \left( \log(N) - 1 \right) \log(N) \right] (N - (d + 1))^2 + 2N \left( N + (d + 1) \right) }{ 2N + \log(N)(N - (d + 1))(N - (d + 1)) } \right\} 
\]
in which $d = 2(m + r) - 1$, is the PH number of degrees of freedom, and $N$ is the total number of sampled records.

In such a manner, at each node of a tree, if covariate $l$ has $G$ values and breaks the node into partition set $(l_1, l_2, \ldots, l_G)$, then the total WIC for the split can be expressed by the sum of singular WICs of every sub-group partitioned by the covariate:

$$WIC_{\text{full}}(d_{\text{full}}) = \sum_{g=1}^{G} WIC_{l_g}(d_{l_g}).$$

Therefore, the information gain is defined as the improvement made in the WIC after splitting the node:

$$IG_l = (WIC_R(d_R)) - WIC_{\text{full}}(d_{\text{full}}),$$

where $R$ stands for the node before partition (i.e., the parent node). Beginning from the root node, at every single node, we apply one covariate at a time and record the gain for partitioning by that covariate. Then, we repeat this with other attributes and select a split that minimizes the WIC the most (or yields the largest gain) to recursively partition into child nodes. Also, if no positive gain can be obtained at a node by any possible split, the node becomes a terminal node.

• **Forest development**

As mentioned before, since patients (can) have multiple records in the dataset, repeated measures and recurrent events are likely. In this case, the bootstrapped samples are dependent and chances of having correlated observations in the in-bag training set are high. Consequently, trees grown may be correlated and overfitting is plausible. To
alleviate this problem, we developed the PHSF algorithm (Algorithm 1) that performs subject-specific bootstrapping rather than using traditional replicate-based bootstrap. According to the algorithm, a subject classification is calculated as the label with the maximum number of votes cast across all records for that subject among all trees. The PHSF is able to produce predictions for specific replicates of a subject, and it can also be reduced to the original random forest if no replicate per subject is available. Consistent with the rule-of-thumb, subject-level bootstrapping performed in the algorithm ensures that about 63% of the subjects (rather than replicates) are elected in-bag. In this way subjects with more replicates cannot dominate the training process.

Algorithm 1. Phase-type Survival Forest

I. For $b = 1$ to $B$:

   a) Take a bootstrap sample (i.e., a random sample chosen with replacement) of size $S$ at the subject level (patient) from the training data. Assuming $n_j$ records per patient $j$, $N = n_1 + n_2 + \ldots + n_S$.

   b) Grow an unpruned tree $T_b$ on each bootstrap by repeating the following steps, until no improvement is made in (11).

      i. Select $\nu'$ variables at random from the whole $\nu$ variables. Normally $\nu'$ should be much less than $\nu$, such as $\sqrt{\nu}$ or even 1.

      ii. Following the splitting criterion introduced, pick the best variable among the $\nu'$, and split the node into two child nodes.

II. Output the ensemble of trees $\{T_b\}_1^B$.

To make a prediction for a new patient $x$:

Let $\hat{C}_b(x_{(i)})$ be the class prediction of the $b$th tree for replicate $i$ of the patient. Then

$$\hat{C}_{PHSF}(x) = \text{majority vote}\left\{\hat{C}_b(x_{(i)})\right\}_1^B.$$
Considering that the PHSF generates proportions of votes for each class, similar to data models, we can have an (unbiased) estimate of the probability that a patient is readmitted. Further, like the original version of the random forest, the out-of-bag (OOB) data (which includes about one-third of all subjects) is used to get a running unbiased estimate of the classification error in both replicate and subject levels. Finally, like Breiman’s RF algorithm, we use the permutation-based measure to get a raw importance score for variable \( v \) as:

\[
I_v = \frac{1}{B} \sum_{b=1}^{B} \left( P_{c,b} - P_{c,b}^v \right). \tag{12}
\]

In the formula, \( P_{c,b} \) is the proportion of correctly classified replicates out of total OOB replicates in a given tree, and \( P_{c,b}^v \) is the proportion of OOB replicates classified right after variable \( v \) is randomly permuted across all OOB cases.

### 2.4. Performance evaluation measures

We compare the PHSF algorithm with four popular classification methods: Breiman’s Random Forest, Logistic Regression, Neural Network (NN), and Support Vector Machine (SVM). To evaluate the predictive accuracy of the approaches, we use sensitivity (also called true positive rate or recall), specificity, positive predictive value (or precision), negative predictive value, F-measure, Matthews correlation coefficient, and the area under the receiver operating characteristic curve (AUROC). Denoting True Positive (Negative) and False Positive (Negative) outcomes as TP (TN) and FP (FN), the predictive measures are computed as
Sensitivity (specificity) determines the proportions of actual positives (negatives) that are correctly classified as such. Positive predictive value (PPV) measures the proportion of positive predictions that are true positive, while negative predictive value (NPV) indicates the proportions of negative test outcomes that are true negatives. The F-score can be interpreted as a harmonic mean of precision and recall, with a best value at 1 and a worst at zero. The Matthews correlation coefficient (MCC) is a correlation coefficient between observed and predicted binary tuples, which works well in class-imbalanced situations where the classes can be of very different sizes. Expectedly, it returns a real value in \([-1, +1]\), in which +1 represents a perfect prediction, zero means no better than random prediction, and −1 shows total disagreement between prediction and observation. The ROC curve is a graphical tool that exemplifies the performance of a classifier by plotting, at various cut-off points for the predicted risk, the sensitivity vs. one minus the specificity. In other words, moving along the ROC from bottom-left to top-right trades off false positives for false negatives. The AUROC (or c-statistics) can then be defined as the proportion of times a given classifier correctly discriminates a random pair of patients with and without readmission. Stated differently, an AUROC of 0.77 indicates that a patient with readmission is credited with a higher prediction value than a patient without readmission 77% the time, for a random pair of patients with and without readmission. A
value of 0.5 for the AUROC shows that the model does not work better than a random pick; values between 0.7–0.8 suggest a modest separation ability; and values bigger than 0.8 imply good discriminative power. A simple approach to calculating AUROC for binary classification is presented by (Hand, Till, 2001) as

\[
A = \frac{S_0 - n^+ (n^- + 1)/2}{n^+ n^-},
\]

(14)

where \(n^+\) and \(n^-\) are the number of positive and negative entries, respectively, and \(S_0 = \sum r_i\), in which \(r_i\) is the rank of the \(i\)-th positive example in the ranked list.
Chapter III Result and Analyses

In this section, we describe steps to implement the proposed methods with the VHA data. First, data preprocessing is presented in Section 4.1. Then we perform the PAR algorithm to recognize avoidable readmissions from all other types of outcome. After that, we fit the proposed Coxian PH distribution to COPD time-to-readmission data and find the optimal cut-off for the time interval. Finally, predictive modeling with the PHSF algorithm as well as details about model calibration and validation are presented.

3.1. Data

The dataset used in this retrospective cohort study is provided by the Veteran Health Administration (VHA), which is the largest single medical system in the United States, with 152 medical centers and nearly 1400 outpatient clinics. We analyze inpatient administrative records gathered from four medical facilities in the State of Michigan, namely, Ann Arbor, Battle Creek, Detroit, and Saginaw, to identify all hospitalizations for Heart Failure (HF), Acute Myocardial Infarction (AMI), Pneumonia (PN), and Chronic Obstructive Pulmonary Disease (COPD) from Fiscal Year 2011 to FY12. Cohorts are marked with ICD-9-CM (International Classification of Diseases, Ninth Revision, Clinical Modification) codes, similar to the coding utilized by the CMS for calculating hospital readmission rates.

There were no major changes in the hospital bed supplies, and in the patient admission/discharge processes through that period of time. During a hospital stay, patients may move to different acute wards within the hospital and their episodes of care are carefully tracked with standard computerized means. We use additional data files for
patients with chronic conditions as well as patients exposed to environmental hazards such as Agent Orange, to effectively illustrate those impacts on the risk of readmission.

The original set contains 7200 randomly selected records, which correspond to 2985 distinct adult patients with principal (or secondary) discharge diagnoses of HF, AMI, PN, and COPD. General exclusions include: (1) Hospital admissions within 24 hours of index discharge, (2) Hospitalizations with a length of stay less than 24 hours (observation stays) or followed by a death, (3) Patients transferred to another acute care facility, (4) Patients discharged against medical advice. To count readmissions in the last month of FY12, the first month of FY13 is taken into account.

In additions, we omit stays in long term care, nursing home, psychiatry, rehabilitation, and hospice wards. However, as we are interested in modeling the effect of patient’s related factor changes (over time) on the risk of readmission, unlike most studies in the literature (Joynt, Orav, Jha, 2011), we do not exclude recurrent (re)admissions of the same patient from the analyses. We also design both external and internal model validations by using stratified split sample and bootstrap resampling methods.

3.1.1. Controlled variables

We aggregate patient level data files with provider and station levels in order to obtain various types of risk factors for this study. To achieve a better picture of the data environment, we further arrange them into five groups: (1) Demographics: age at discharge, sex, race, and marital status; (2) Socioeconomic: means tested income, and insurance status (Medicare, Medicaid, private, none); (3) Utilization: length of stay of the index hospitalization (LOS), treating facility, source of admission (direct from home, outpatient clinic, transition from any of the four VA hospital, VA Nursing Home Care
Unit (NHCU), and VA domiciliary), primary care provider, enrollment priority, and average distance (between patient’s home zip code and the zip code of the facility he/she got admitted); (4) Service based: Agent Orange status, Prisoner Of War (POW) status, and radiation status; and (5) Comorbidity and severity: Diagnosis Related Group (DRG), Hierarchical Condition Category (HCC), and Care Assessment Need (CAN) score. The variables were selected based on the relevant medical literature and confirmed by a group of Veteran Affairs (VA) health professionals.

The enrollment priority is a priority level assigned according to the veteran’s severity of service-connected disabilities and the VA means test. The DRG is a validated reimbursement classification scheme exploited to identify the cost of services that a hospital renders. In its basic version, the groups are organized with respect to their similarities in patient diagnosis, age, sex, and the presence of complications or comorbidities; then a measure of cost is attached to each group (Fetter et al., 1980).

HCCs have been used ad hoc, mainly for case-mix and risk adjustment in healthcare utilization and payment systems. Each HCC group forms a set of clinically and cost-similar conditions reflecting hierarchies among related diseases as defined by the ICD-9-CM codes (Pope, 2004). We create dummy variables for both the DRG and HCC variables in the regression studies; that is, if a patient is a member of the category, he or she is given a 1 on this variable; otherwise the score remains zero. The CAN score is a general illness severity score that reflects the likelihood of admission or death within a specified time period, and it works somewhat similar to diagnostic cost group (DxCG) risk score (Sales, 2013). The score is commonly expressed as a percentile ranging from 0 (lowest risk) to 99 (highest risk) and it shows how a VA patient is compared with others.
pertaining to the chances of hospitalization or death. It is interesting to note that all predictor variables except LOS are real time and would be available before patient discharge, so they can be employed in planning for pre-discharge (transitional care) intervention programs.

3.1.2. Study outcomes

The main outcome is rate of avoidable readmission after discharge. Unlike the large literature that studies only the occurrence of readmission by logistic (or probit) regression methods (Berry et al., 2013; Pracht, Bass 2011), our current approach is a hybrid of both occurrence and timing of readmission, which enables us to directly incorporate the effect of partially known information (censored observations) into the risk of readmission. For hospitalizations after HF, AMI, and PN, we follow the CMS approach and define the readmission time interval as 30 days; if no consecutive admission is occurred within 30 days after the most recent admission, the outcome is flagged as censored. For COPD patients, however, we do not adopt the 30-day cutoff, and instead develop an approach to optimally determine the interval that best stratifies the quickly-readmitted and slowly-readmitted patient groups. We further modify the approach introduced by (Goldfield et al., 2008) to distinguish between avoidable and unpreventable outcomes.

The most common causes of readmission for the four cohorts as well as their changes over time are also investigated as secondary health outcomes.

3.1.3. Data preprocessing

Since real world data generally contain missing values, noise (e.g., errors and outliers), and inconsistent records, data preprocessing is essential for ensuring valid
analytics. In this regard, added to what is given in the PAR algorithm (section II, part k), we perform the following tasks:

   a) Create attributes for time-to-readmission, readmission status, LOS, and sequence of (repeated) readmissions using admission and discharge dates.
   b) In predictive model building, we use the default replacement method of Breiman’s algorithm for missing values. For univariate analysis, however, missing values are imputed with the hot-deck method (Ford, 1983).
   c) Identify and remove extreme records (outliers) with Local Outlier Factor (LOF) technique (Breunig et al., 2000).
   d) Correct error records and flawed data combinations (e.g., POW: Yes, Veteran: No).
   e) Discretize attributes like distance into three levels (near: below 25 miles, middle: between 25 and 50 miles, far: above 50 miles) by $k$-means clustering.

Following these steps, the number of records is reduced to 6975 with 2813 distinct patients.

3.1.4. Statistics

Our main outcome was avoidable readmission measured by the PAR metric in the first 30 days of hospital discharge. We first examine the presence of any difference in the baseline characteristics between the cohorts using univariate logistic regression. Since the same patient could have several avoidable readmissions during the study, we used generalized estimation equation to adjust for serial correlations among readmissions of the same patient.

Then, using the entire set of patient risk factors, we performed a random forest
analysis. Random forest (Breiman, 2001a) is a popular nonparametric method that grows many classification trees by bootstrap resampling technique to estimate the aggregated probability of an outcome. Although they were recently adopted in estimating propensity scores (HSR paper, 2013), few researches have studied the use of random forest to predict the risk of readmission (AHJ paper, 2012). Each tree provides a classification based on a set of randomly chosen predictor variables that are used to split the data at each node.

With this set of trees, the ability of each predictor to separate the patient who had or did not have the outcome is assessed and weighted with respect to the overall quality of the tree. Then importance of each covariate in all trees is summarized by a Gini index, which tells how much accuracy of the prediction is lost if the variable is not included. Such methods proved to increase the accuracy of prediction compared to classical statistical methods such as logistic and probit regression (Breiman, 2001b).

Since we are interested in studying the effect of having previous readmissions on the likelihood of outcome, we modify the random forest algorithm in a way that it can handle the correlation among repeated measures and recurrent events of the same subject. The basic idea is to have the forest take a bootstrap sample at the patient level rather than at the replicate level, i.e. doing subject-specific bootstrap instead of traditional replicate-based bootstrap. This way, when a particular patient is chosen at random, all of its replicates (repeated measures) that had the outcome (recurrent events) or did not have the outcome are attached to it. Hence, trees grown are not correlated and overfitting is avoided. For instance, patients with more repeated measures cannot dominate the learning process in the training data (HCMS paper, 2014).
We started by including all risk factors into the random forest to estimate the predicted probability of avoidable readmission. We additionally created a new variable called ‘sequence’ for determining how many times a given patient was readmitted in the study. Except age, length of stay, CAN score, Charlson comorbidity index, and sequence, all other covariates are entered as dummy variables. We set the number of trees to grow and the number of variables to randomly split at each node as 5,000 and 5, respectively. The latter number is the suggested default and equals to the square root of the total number of variables in the algorithm. We also investigated what the optimal cutpoint for continuous variables should be that most discriminate high vs. low risk patients using operating characteristic curves.

We then performed two sensitivity analyses: (1) sensitivity of random forest error rates to our selected parameters by letting the number of trees to change between 2,000 to 5,000 and the number of randomly chosen variables to vary between three to seven, and (2) sensitivity of error rates to class weights by setting different weights for the two cohorts that had or did not have the outcome. Finally, we conducted internal validation with same population underlying the sample, as well as external validation with a new patient sample. We used R platform for all analyses and statistical computing (RCD, 2005).

3.2. Potentially avoidable readmissions rates

Using 30-day (and T-day; see Section 4.3) readmission timeframes for the three acute conditions (and COPD), we begin by classifying all records to admissions and readmissions. Removing instances from the admission and readmission sets that meet one or more exclusion criteria (see section III of the PAR algorithm), we initially identify
total of 5,449 eligible admissions and 968 readmissions. Of the 968 readmissions, 173 cases were found not clinically related to their prior admissions (see PAR algorithm, section V), from which 27 cases are fitted in either “death,” “transfer,” or “against-medical-advice” groups and thus be dropped. The remaining 146 readmissions were then reclassified as eligible admissions, resulting in 5,595 eligible admissions. Hence, we end up having 795 PARs, from which 596 examples belong to a PAR series with only one PAR, and 78 match to a PAR series with two or more PARs. Consequently, the total number of unique PAR series becomes 674, and the PAR rate (see section IX of the PAR algorithm) is found to be 12.05 percent. Following the same approach, rates of PAR for HF, AMI, PN, and COPD are 13.26, 12.47, 11.16, and 11.33 percent.

The facility-adjusted PAR rates vary from 12.37% to 13.69% for HF; 11.83%–13.16% for AMI; 10.74%–11.93% for PN, and 10.68%–12.13% for COPD. From all HF avoidable readmissions, 86.3% are readmitted once, 11.4% are readmitted twice and 2.3% are readmitted three or more times. These rates are (81.7%; 14.6%; 3.7%), (88.4%; 10.9%; 0.7%), and (83.2%; 14.7%; 2.1%) for AMI, PN, and COPD respectively.

The pattern of PAR rates for the three acute conditions and the COPD during cumulative periods after discharge (days 0–7, 0–15, 0–21, and 0–30) are outlined in Table 1. As shown, of all 30-day avoidable readmissions, nearly 58% of the HF, 55% of the AMI, and 60% of the PN cohorts occurred within 15 days after hospital discharge. In other words, the majority of acute (avoidable) readmissions happens relatively soon after discharge, and they remain common even after two weeks of discharge. However, only around 58% of all COPD (avoidable) readmissions take place until the third week after discharge, and nearly 22% is left beyond the 30 day interval, which supports our
argument about the inappropriateness of the 30-day timeframe for the chronic disease. This finding can be of great value for health professionals when they plan to allocate inpatient and early outpatient intervention programs to both acute and chronic conditions.

The mean (standard deviation) patient age of the readmitted cohort is 78.6 years (3.5 years) for HF, 80.3 years (4.1 years) for AMI, 79.3 years (2.9 years) for PN, and 76.2 years (3.1 years) for COPD. Frequent comorbid conditions among readmissions are coronary artery disease (CAD), atrial fibrillation, and diabetes for the HF cohort; anemia, congestive heart failure, and vascular disease with complications for the AMI cohort; chronic obstructive pulmonary disease, congestive heart failure, and cardiorespiratory failure and shock for the PN cohort; and chronic bronchitis, pneumonia, and diabetes mellitus for the COPD cohort.

Table 1 Distribution of avoidable readmissions over time

<table>
<thead>
<tr>
<th>Cohort</th>
<th>Days following discharge</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>0–7</td>
</tr>
<tr>
<td>Heart Failure</td>
<td>28.6%</td>
</tr>
<tr>
<td>Acute Myocardial Infarction</td>
<td>33.4%</td>
</tr>
<tr>
<td>Pneumonia</td>
<td>31.1%</td>
</tr>
<tr>
<td>COPD</td>
<td>21.1%</td>
</tr>
</tbody>
</table>

The most common diagnoses of 30-day (or $T$-day; see Section 4.3) readmission after HF, AMI, PN, and COPD hospitalizations are displayed in Table 2. It appears that after admission for HF and AMI, readmissions happen mostly for heart failure (39.6% and 28.3% of readmissions, respectively), but following hospitalizations for PN and COPD, patients get readmitted because of COPD (21.4% and 32.5%, in turn). Also, the top five
readmission diagnoses contribute to 63.2% of all readmissions after HF, 59.4% of all readmissions after AMI, 55.6% of all readmissions after PN, and 65.1% of all readmissions after COPD.

Further, we realized that the most frequent reasons for avoidable readmissions in all conditions are related to “recurrence or extension of the reason (Section V, part b)” and “medical complications (Section V, part d)”, with an average of 54.7% and 23.2% through all the hospitals. As expected, in none of the acute and chronic conditions is the proportion of non-clinically related readmissions over 15.4 percent.

### Table 2 Top readmission diagnoses for patients hospitalized with HF, AMI, PN, and COPD

<table>
<thead>
<tr>
<th>Rank</th>
<th>HF cohort</th>
<th>AMI cohort</th>
<th>PN cohort</th>
<th>COPD cohort</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Diagnosis</td>
<td>Percent of PAR</td>
<td>Diagnosis</td>
<td>Percent of PAR</td>
</tr>
<tr>
<td>1</td>
<td>Heart failure</td>
<td>39.6%</td>
<td>Heart failure</td>
<td>28.3%</td>
</tr>
<tr>
<td>2</td>
<td>Renal failure</td>
<td>9.3%</td>
<td>Coronary artery disease</td>
<td>13.7%</td>
</tr>
<tr>
<td>3</td>
<td>Arrhythmias</td>
<td>6.7%</td>
<td>Pneumonia</td>
<td>8.6%</td>
</tr>
<tr>
<td>4</td>
<td>Cardio-respiratory failure and shock</td>
<td>4.1%</td>
<td>Septicemia/Shock</td>
<td>5.5%</td>
</tr>
<tr>
<td>5</td>
<td>Pneumonia</td>
<td>3.5%</td>
<td>Renal failure</td>
<td>3.3%</td>
</tr>
</tbody>
</table>
Next, we compared percentages of readmissions calculated by our method (PAR) to those of the 3M method for the three acute conditions in the four hospitals (Figure 6). In our method, consistent with the literature (Medicare Payment Advisory Commission, 2007), we observe that a greater proportion of all readmissions can be avoided in the first two weeks after discharge, but the contribution declines as time passes. Compared to the 3M approach, our method considers (slightly) fewer rehospitalizations as being avoidable and produces lower rates of readmission throughout all periods after discharge. A probable reason for this may be related to the CMS- and VHA-specific exclusions of our method, which is not found in the 3M approach. Besides, almost the same trend (not shown here) is seen for the COPD readmissions but over an extended time interval following discharge.

Figure 6 Percent of readmission over
3.3. Optimal COPD readmission timeframe

In this section, we fit the proposed Coxian PH distribution to COPD time-to-readmission data in order to find the optimal cut-off point that defines avoidable readmissions. Using empirical data, we first examine the percentile distribution of times in Table 3.

<table>
<thead>
<tr>
<th>Percentile</th>
<th>0</th>
<th>10</th>
<th>25</th>
<th>50</th>
<th>75</th>
<th>90</th>
<th>100</th>
</tr>
</thead>
<tbody>
<tr>
<td>Day</td>
<td>1</td>
<td>7</td>
<td>19</td>
<td>36</td>
<td>88</td>
<td>174</td>
<td>283</td>
</tr>
</tbody>
</table>

As shown, the median time-to-(avoidable) readmission is about 36 days and the distribution is (highly) right skewed, with more than half of patients readmitted after the 30th day from discharge. This implies that, unlike acute conditions, poor quality of inpatient care for chronic conditions may reveal itself after 30 days from discharge. So setting the 30-day as a fixed timeframe for both acute and chronic conditions may not be appropriate.

We then applied the EMph software to estimate the phase-type generator $Q$ in (5) using COPD time-to-readmission data from FY 11–12. In brief, the program starts with an initial guess $Q^{(0)}$ (for the non-zero elements in (5)) and proceeds with a number of iterations of the EM algorithm to increase the log-likelihood function

$$
\sum_{i=0}^{\infty} \log \left( \pi \exp(Qt)(-Q1) \right).
$$

Fixing the maximum number of iterations at 5000 runs and Runge-Kutta step length at $\frac{0.1}{\max_i |Q_{ii}|}$ (in which $\max_i |Q_{ii}|$ is the largest absolute value of the diagonal element of
the last estimate of $Q$), we configure different Coxian PH structures by modifying the order of the sub-class Markov processes (i.e., parameters $m$ and $r$). This way, we start with $m=1$, examine various levels of $r$ from 1 to 10, and pick the best in terms of AIC and BIC; then we repeat this for $m=2$ until $m=10$. We stop the search if the log-likelihood does not improve in any intermediate level. Also due to non-identifiability of the parametrization of the phase-type distribution (O’Cinneide CA, 1990), we do several fits starting with various initial values produced in previous runs. The results of best fits at each level of $m$ are then summarized in Table 4.

It is apparent that there is no improvement in the fits after the fourth phase of the Short-Stay group (i.e., $m=4$). Hence an order 6 of the Coxian PH distribution with 4 and 6 phases for the Short-Stay and Long-Stay groups respectively is considered to most suitably represent the time-to-readmission process of the COPD patients in the dataset. Note that we do not show fits after ($m=5$) as they provide no further enhancements.

<table>
<thead>
<tr>
<th>Fit</th>
<th>$r$</th>
<th>AIC</th>
<th>BIC</th>
</tr>
</thead>
<tbody>
<tr>
<td>$m=1$</td>
<td>3</td>
<td>35443.4</td>
<td>35443.02</td>
</tr>
<tr>
<td>$m=2$</td>
<td>2</td>
<td>35181.3</td>
<td>35180.90</td>
</tr>
<tr>
<td>$m=3$</td>
<td>1</td>
<td>34077.7</td>
<td>34077.32</td>
</tr>
<tr>
<td>$m=4$</td>
<td>2</td>
<td>33816.5</td>
<td>33818.28</td>
</tr>
<tr>
<td>$m=5$</td>
<td>2</td>
<td>33844.2</td>
<td>33851.54</td>
</tr>
</tbody>
</table>

The estimates of the intensity rates in (5) along with their standard errors are calculated in Table 5. Given the small amounts of error, we see that the parameters are well estimated with EMpht. Also note that $\lambda_1$, $\lambda_2$, and $\lambda_3$ belong to the Short-Stay
group, while $\lambda_4$ and $\lambda_5$ are related to the Long-Stay group. According to the table, the probability of a patient being in the Short-Stay group is calculated as

$$p = \frac{1.26}{1.26 + 1.58} = 0.4437,$$

which means that the COPD patients spend about 44.37% of their time in the Short-Stay group in the community before returning to the hospital.

Then, in order to solve (7) and obtain the optimal COPD readmission timeframe, we need to derive the PDFs $f_{SS}$ and $f_{LS}$. This can be done based on a convolution of a set of independent exponential variables ($X_i$) as follows (Ross, 2009):

$$f_{SS} = f_{X_1 + X_2 + \ldots + X_m}(x)$$

$$= \int_0^x \int_0^t \int_0^{t-m} f_{X_1}(t_1) f_{X_2}(t_2 - t_1)$$

$$\times L \times f_{X_m}(x-t_{m-1}) \, dt_1 \, dt_2 \, L \, dt_{m-1}$$

$$= \left[ \prod_{i=1}^{m} (\lambda_i + \lambda_{j0}) \right] e^{-(\lambda_i + \lambda_{j0})x}$$

$$\times \sum_{j=1}^{m} \sum_{k=1}^{m} \prod_{k \neq j} (\lambda_k + \lambda_{k0}) \left( \lambda_i + \lambda_{j0} \right)$$

$$f_{LS} = f_{X_1 + X_2 + \ldots + X_{m+r}}(x) = \left[ \prod_{i=1}^{m+r} (\lambda_i + \lambda_{i0}) \right] e^{-(\lambda_i + \lambda_{i0})x}$$

$$\times \sum_{j=1}^{m+r} \sum_{k=1}^{m+r} \prod_{k \neq j} (\lambda_k + \lambda_{k0}) \left( \lambda_i + \lambda_{j0} \right)$$

Note that the escape rate $\lambda_{i0}$ is zero for all phases except $m$ and $m+r$, that is,
\( \lambda_{m_0} = \lambda_{SS}, \quad \lambda_{m+r-1} = \lambda_{LS} \)

Finally, by substituting (15) in (7) with \( p = 0.4437 \), we compute \( t^* \) (or \( T \) in the PAR algorithm) as 42 days, which is pretty close to, but more accurate than what we observe in Figure 1. Thus, for the COPD cohort we should utilize a 42-day timeframe to count the correct number of avoidable readmissions in our study.

3.4. Predicting the risk of avoidable readmissions

In this section, we first perform some descriptive analytics on the patient risk factors for the two cohorts within each condition. Afterwards, steps for predictive modeling along with details about model validation and calibration are described. We then end by doing performance evaluation and comparison studies.

Table 5 Estimated intensity rates for the COPD Coxian PH model

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Estimate</th>
<th>Standard Error</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \lambda_1 )</td>
<td>0.04</td>
<td>0.008</td>
</tr>
<tr>
<td>( \lambda_2 )</td>
<td>3.62</td>
<td>0.126</td>
</tr>
<tr>
<td>( \lambda_3 )</td>
<td>5.17</td>
<td>0.233</td>
</tr>
<tr>
<td>( \lambda_4 )</td>
<td>1.58</td>
<td>0.075</td>
</tr>
<tr>
<td>( \lambda_5 )</td>
<td>0.96</td>
<td>0.039</td>
</tr>
<tr>
<td>( \lambda_{SS} )</td>
<td>1.26</td>
<td>0.097</td>
</tr>
<tr>
<td>( \lambda_{LS} )</td>
<td>0.83</td>
<td>0.004</td>
</tr>
</tbody>
</table>

3.4.1 Descriptive Analytics

Baseline patient characteristics in PAR and No-readmission cohorts are displayed in Table 6 (for Heart Failure and Acute Myocardial Infarction) and Table 7 (for Pneumonia and COPD). The presence of any significant difference between the cohorts was also
tested using univariate logistic regression and the results are shown in terms of $P$-Values [missing values are imputed by the hot-deck method]. Since the same patient could have several avoidable readmissions during the study period, we used generalized estimation equation to adjust for serial correlations among readmissions of the same patient.

During the study, a total of 5,595 eligible admissions were made in the four VA hospitals, out of which about 14.21% were followed by an unnecessary rehospitalization. Note that this rate is different from what is reported in Section 4.2 (which is 12.05%) because here we count each readmission separately rather than as members of a PAR series. In all conditions, the populations are generally male (>86%), married (>51%), older (>67 years), and live within 25 miles of a VA facility (>60%).

More than 21% in all conditions do not have private insurance or insurance through Medicare or Medicaid programs. More than half of patients in all conditions are admitted directly from their home and more than 50% have one to four past-year hospitalizations. On average, the care assessment score is higher in respiratory diseases (near 69) compared to circulatory conditions (about 66). Almost 18% of the patients are also diagnosed with more than ten HCCs (not shown in the tables).

Note that in the attribute “source of admission,” class ‘transfer’ is related to those patients who are transferred only among the four VA hospitals, and ‘Other’ is related to some other admission sources such as observation/examination, non-VA hospitals not under VA auspices, community nursing homes under (or not under) VA auspices, non-veteran hospitals, etc. Further, priority groups 1, 2, and 3 are generally assigned to veterans with service-connected disabilities of > 50%, [30%, 50%), and [20%, 30%), respectively. Other groups are as follows: 4, catastrophically disabled veterans; 5, low
income or Medicaid; 6, Agent Orange or Gulf War veterans; 7, non-service connected with income being below HUD; and 8, non-service connected with income being above HUD. For each condition, patient comorbidities are identified with the help of Comorbidity Software (Kaboli et al., 2012), using ICD-9-CM and DRG codes from the index hospitalization and any admission in the 12 months prior.

It is observed that patients who are subsequently readmitted are elderly and usually have a greater number of comorbidities. Male patients have on average a greater chance to be readmitted in HF and COPD cohorts rather than females, but this cannot be generalized since the VA sample here contains only about 8% female patients. The analysis shows that length of stay is not generally associated with odds of avoidable readmission, when patient and facility characteristics are not controlled for.

However, after adjusting for the case-mix and service-mix (not shown here), the relation tends to be negative (about 7.3% increase for each in-hospital day lower than expected), which implies that shorter individual LOS is generally connected with higher risk of readmission. Therefore, consistent with (Kaboli et al., 2012), we observe that significant reduction in LOS, without simultaneously improving inpatient care, is more likely to result in premature discharge and rehospitalization. Further, enrollment priority turns out to be highly linked with odds of readmission in all conditions, especially when it comes to catastrophically disabled veterans (increases of .2% in AMI to 10.9% in HF). Furthermore, the odds of avoidable readmissions are significantly higher in patients exposed to ionizing radiation and Agent Orange in all conditions. Among the comorbid conditions, having diabetes and cancer increases the chance of readmission, as does
having mental disorders and substance abuse (with harsher effect in circulatory conditions).

### 3.4.2 Predictive modeling with PHSF

Following Algorithm 1, we used the entire set of patient risk factors to develop a readmission prediction model. Additionally, we create two more covariates, namely, “sequence” and “Charlson comorbidity index” and entered them into the analysis. For non-categorical variables in the candidate set (i.e., age, LOS, CAN score, sequence, and Charlson index), we evaluated different cut-off points to split the dataset into binary partitions and explore the optimal cutpoint that most discriminates high vs. low risk using operating characteristic curves (with whole dataset). We then used this ROC-generated cutpoint for further analyses. Also for categorical features with more than two classes (like race), following (Friedman, Hastie, Tibshirani, 2009) we optimally select a series of binary splits (instead of multiway splits) that produce the best discrimination results.

We begin with the baseline model that uses all sampled data points (5,595 records) in the subject-specific bootstrapped PHSF and we let the forest internally perform cross-validation using OOB samples during each run. The number of trees and the number of variables to try at each split are set to 6,000 and 5, respectively. Also we set the cutpoints with respect to minimizing the WIC criterion (see Section 3.1.1) as follows: Age, 68 (years); LOS, 5 (days); CAN score, 66; sequence, 3; and Charlson index, 4.5. Results of variable importance are summarized in Table 8 (Sig. stands for significance level).

As illustrated, almost all statistically significant variables (Sig. <.05) refer to overall health and agedness factors, which may reflect a generalized vulnerability to disease
among recently discharged patients—inpatients regularly lose their strength and develop new difficulties in doing their day-to-day activities (Gill et al., 2010). Interestingly, ‘sequence’ turns out to be (positively) related to readmission risk, which highlights the fact that the chance of unnecessary returns to hospital is greater in patients with prior history of readmission.

In the baseline model, the c-statistics is .793; sample-level OOB error rates are 3.16%, 2.35%, and 8.05% for overall, No-readmission class, and PAR class, respectively; and there are large interactions [based on Breiman’s variable interaction model [46]] between Agent Orange and Radiation, between Priority and LOS, and between Priority and Insurance, to name a few.
<table>
<thead>
<tr>
<th>Characteristic</th>
<th>Heart Failure (n=1674)</th>
<th>Acute Myocardial Infarction (n=1417)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>No Readmission (n=1447)</td>
<td>PAR (n=227)</td>
</tr>
<tr>
<td>Age (years)</td>
<td>68.6 (5.2)</td>
<td>71.3 (3.2)</td>
</tr>
<tr>
<td>Sex, Male</td>
<td>1406 (97.2)</td>
<td>215 (96.9)</td>
</tr>
<tr>
<td>Race</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Black</td>
<td>986 (68.1)</td>
<td>193 (85.0)</td>
</tr>
<tr>
<td>White</td>
<td>432 (29.8)</td>
<td>29 (12.8)</td>
</tr>
<tr>
<td>Other</td>
<td>29 (2.1)</td>
<td>5 (2.2)</td>
</tr>
<tr>
<td>Marital status</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Current spouse</td>
<td>839 (57.9)</td>
<td>137 (58.3)</td>
</tr>
<tr>
<td>Never married</td>
<td>307 (21.2)</td>
<td>52 (21.4)</td>
</tr>
<tr>
<td>Previously married</td>
<td>301 (20.9)</td>
<td>38 (20.3)</td>
</tr>
<tr>
<td>Primary insurance</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Medicare</td>
<td>732 (50.6)</td>
<td>126 (55.5)</td>
</tr>
<tr>
<td>Medicaid</td>
<td>249 (17.2)</td>
<td>27 (11.9)</td>
</tr>
<tr>
<td>Private</td>
<td>107 (7.4)</td>
<td>25 (11.0)</td>
</tr>
<tr>
<td>Not insured</td>
<td>359 (24.8)</td>
<td>49 (21.6)</td>
</tr>
<tr>
<td>Length of stay (days)</td>
<td>5.2 (6.1)</td>
<td>6.2 (4.4)</td>
</tr>
<tr>
<td>Source of admission</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Direct from home</td>
<td>797 (55.1)</td>
<td>129 (56.8)</td>
</tr>
<tr>
<td>Outpatient clinic</td>
<td>392 (27.1)</td>
<td>63 (27.8)</td>
</tr>
<tr>
<td>Transfer</td>
<td>17 (1.2)</td>
<td>3 (1.3)</td>
</tr>
<tr>
<td>VA NHCU</td>
<td>62 (4.3)</td>
<td>12 (5.3)</td>
</tr>
<tr>
<td>VA Domiciliary</td>
<td>13 (0.9)</td>
<td>4 (1.8)</td>
</tr>
<tr>
<td>Other</td>
<td>166 (11.5)</td>
<td>16 (7.0)</td>
</tr>
<tr>
<td>Enrollment priority</td>
<td></td>
<td></td>
</tr>
<tr>
<td>1</td>
<td>126 (8.7)</td>
<td>17 (7.5)</td>
</tr>
<tr>
<td>2</td>
<td>167 (11.5)</td>
<td>9 (4.0)</td>
</tr>
<tr>
<td>3</td>
<td>293 (20.2)</td>
<td>38 (16.7)</td>
</tr>
<tr>
<td>4</td>
<td>173 (12.0)</td>
<td>52 (22.9)</td>
</tr>
<tr>
<td>5</td>
<td>316 (21.8)</td>
<td>66 (29.1)</td>
</tr>
<tr>
<td>6</td>
<td>115 (7.9)</td>
<td>15 (6.6)</td>
</tr>
<tr>
<td>7</td>
<td>103 (7.1)</td>
<td>19 (8.4)</td>
</tr>
<tr>
<td>8</td>
<td>154 (10.6)</td>
<td>11 (4.8)</td>
</tr>
<tr>
<td>Distance to hospital</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Near (&lt;25m)</td>
<td>856 (59.2)</td>
<td>155 (68.3)</td>
</tr>
<tr>
<td>Middle ([25, 50]m)</td>
<td>549 (37.9)</td>
<td>69 (30.4)</td>
</tr>
<tr>
<td>Far (&gt;50m)</td>
<td>42 (2.9)</td>
<td>3 (1.3)</td>
</tr>
<tr>
<td>Characteristic</td>
<td>Heart Failure (n=1674)</td>
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Table 7 Baseline characteristics

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<th>COPD (n=1198)</th>
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<td>Age (years)</td>
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<td>7</td>
<td>37 (3.3)</td>
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Table 7 continued

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<td>P-Value</td>
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<tr>
<td>All others</td>
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• **Model calibration**

We then calibrated the baseline model as follows: 1) we focused only on the 16 most important variables found in the baseline model; 2) we imputed missing values based on Breiman’s replacement technique; 3) we modified the optimal cut-off points with regards to maximizing the $c$-statistics (the new cutpoints are 69 years for age, 70 for CAN score, and 4.7 for Charlson index, while others remain unchanged); and 4) we altered the class weights to 1 on class ‘No-readmission’ and 8 on class ‘PAR’, to adjust for the imbalanced prediction errors in the classes. Then we rerun the model with 10,000 trees and 4 variables to try at each split.

Depiction of variable importance for the calibrated model is shown in Table 9. Expectedly, the ranking of variables does not change but we achieved better results in terms of scores and significance levels. It is noticed that, though Mental disorder and Malignant neoplasm are only marginally significant, we decide to keep them in the final model since 1) they are both medically significant in contribution to the risk of readmission, and 2) they together contribute largely to the model discrimination ability.

In the calibrated model, the $c$-statistics jumps to .836; no serious interactions remain among variables; and the overall, No-readmission, and PAR error rates become 3.67%, 2.51%, and 2.64%, respectively. It is remarkable that the calibrated model considerably decreases PAR misclassification rate, but at the expense of increasing the overall error rate a little bit. We perceive that this tuning in class weights is really appealing for our situation because in readmission prediction models, the cost of false negatives (which correspond to readmitted patients incorrectly predicted as No-readmission) is usually
much higher than the cost of false positives (which correspond to non-readmitted patients incorrectly predicted as PAR cases).

Since the PHSF method takes an ensemble approach of trees, as we mentioned earlier, we can obtain an unbiased estimate of PAR probability for each patient. Therefore, it is possible to further check the model calibration by evaluating predicted and actual PAR rates at different risk deciles. These results appear in Table 10 and Figure 4.

We note that, both on average and over the whole range of predictions, the predicted probability of readmission matches up well with the actual probabilities. Average predicted readmission (not shown here) also monotonically increases with growing risk, ranging from 8.79% in the lowest decile to 43.75% in the highest, a range of 34.96% in total. For the 12% of readmissions that happens between deciles four and five, the PHSF model under-predicts by roughly 8.5%. It also over-predicts by about 4%–14% for the small number of readmissions (21%) which occur in deciles 6–10.

![Figure 7 Calibration curve for the PHSF model](image-url)
• **Model validation**

Here, we used the calibrated model and studied its internal validity (also called reproducibility), based on the same population underlying the sample. To this end, since the PHSF does perform bootstrapping internally, we slightly modified the split-sample technique for our purposes: we randomly partitioned the sample into 50% training and 50% testing sets and redid this 7 times.

For each partition we ran the PHRF algorithm and obtained the $c$-statistics. The average $c$-statistics for the seven runs of training sets reached .839 and for the test sets, it was .821. Hence, there exists an “optimism” of .018 in the mean AUROCs for the training and testing splits, and as a result, the internally-validated (or optimism-corrected) $c$-statistics is estimated as .818.

To provide more robust evidence of validity, we further conducted external (in fact: spatial) validation (also called generalizability) with a new sample of 478 patients admitted (with primary diagnosis of HF, AMI, PN, and COPD) in the months of August and September 2012. It is noted that we included the same patient factors studied in the new sample. The $c$-statistics in the external sample decreased to .809 (a decrease of .027) which is slightly more than results from internal validation (a decrease of .018). However, both internal and external validations confirm the superiority of our proposal over the current approaches in terms of discrimination power and stability. Nonetheless, we obtain greater $c$-statistics (at least .813) when the PHSF is applied separately on each condition. It should also be remarked that with the current sample data, the CMS endorsed model can only produce a $c$-statistics of about .63.
Table 9 Variable importance for the calibrated PHSF model

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<tr>
<th>Attribute</th>
<th>Raw score</th>
<th>Z-score</th>
<th>Sig.</th>
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<td>Age</td>
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<td>Charlson CI</td>
<td>7.06</td>
<td>2.398</td>
<td>.008</td>
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<tr>
<td>No. of Past-year hospitalization</td>
<td>7.18</td>
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<td>Sequence</td>
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<td>Vascular disease w/c</td>
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<td>Priority</td>
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### Table 10 Calibration by risk decile for the PHSF model

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<th>Sample size</th>
<th>Predicted PAR</th>
<th>Observed PAR</th>
<th>O/P ratio</th>
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### Table 11 Performance comparisons of our model over the selected methods

<table>
<thead>
<tr>
<th>Method</th>
<th>Predictive accuracy measure</th>
<th>Sensitivity</th>
<th>Specificity</th>
<th>PPV</th>
<th>NPV</th>
<th>F-score</th>
<th>MCC</th>
<th>MSE</th>
<th>AUROC</th>
</tr>
</thead>
<tbody>
<tr>
<td>Our proposal</td>
<td></td>
<td>91.95%</td>
<td>97.65%</td>
<td>86.61%</td>
<td>98.65%</td>
<td>.892</td>
<td>.874</td>
<td>.032</td>
<td>.836</td>
</tr>
<tr>
<td>Random Forest</td>
<td></td>
<td>88.43%</td>
<td>97.35%</td>
<td>84.70%</td>
<td>98.07%</td>
<td>.865</td>
<td>.843</td>
<td>.039</td>
<td>.802</td>
</tr>
<tr>
<td>SVM</td>
<td></td>
<td>86.16%</td>
<td>97.52%</td>
<td>85.20%</td>
<td>97.70%</td>
<td>.857</td>
<td>.833</td>
<td>.041</td>
<td>.775</td>
</tr>
<tr>
<td>Logistic Regression</td>
<td></td>
<td>83.40%</td>
<td>97.21%</td>
<td>83.19%</td>
<td>97.25%</td>
<td>.833</td>
<td>.805</td>
<td>.048</td>
<td>.721</td>
</tr>
<tr>
<td>Neural Network</td>
<td></td>
<td>82.39%</td>
<td>97.06%</td>
<td>82.28%</td>
<td>97.08%</td>
<td>.823</td>
<td>.794</td>
<td>.051</td>
<td>.704</td>
</tr>
</tbody>
</table>
3.4.3 Numerical comparisons

In this section, we evaluate the proposed PHSF method with Logistic Regression (LR), Breiman’s Random Forest (RF), Support Vector Machine (SVM), and Neural Network (NN) in terms of predictive measures introduced in previous section (plus mean squared error). The models are built and compared with the R version 3.0.2 (RDC Team, 2005) using packages randomForest (Liaw, Wiener, 2002), e1071 (Dimitriadou et al., 2008), glm2 (Marschner, 2011), and also MATLAB neural network toolbox (Demuth, Beale, 1993).

It is worth mentioning that we used different kernels such as polynomial and radial basis function for the SVM method; and for the NN approach, we also tested for two and three layers with different numbers of sigmoid hidden neurons and linear output neurons. For the pure random forest method, we did the same calibration as with the PHSF, and for the logistic regression, we used generalized estimation equation to account for clustering at the patient level.

The comparison results are summarized in Table 11 and Figure 8. As shown, the proposal works better than other alternatives in all predictive criteria. The Breiman’s random forest approach and SVM produce very close results in this sample but the NN approach seems unable to compete with other models having a modest discrimination of about 0.7. Not surprisingly, all models predict ‘No-readmission’ cases better than the PAR cases. It is of interest that SVM slightly outperforms the RF in terms of precision (.5% higher) and true negative rate (.17% higher).

Furthermore, in the overall spectrum of false positive rates, the proposal assigns a higher probability of readmission for a patient with PAR compared to a ‘No-readmission’ patient, about 83.6% of the times. Looking at different ROC stairs graphs, we can infer that, with a false positive rate between .09 to .25, our PHSF is placed higher than others,
but it falls behind the SVM and NN in case of very small rates of false positive. In higher false positive rates, we observe that RF and SVM are very similar in discrimination ability and they work as well as PHSF beyond .7 false positive rate. However, logistic regression turns out to fall short at a type I error rate of .8 to .9.

Figure 8 ROC curves for different predictive models
Chapter IV Conclusion

Hospital readmission is disruptive to patients and costly to healthcare systems. About one in five Medicare fee-for-service beneficiaries, totaling over 2.3 million patients, are re-hospitalized within 30 days after discharge, incurring an annual cost of $17 billion, which constitutes near 20% of Medicare’s total payment. However it is reported by the Medicare Payment Advisory Commission that about 75% of such readmissions can and should be avoided because they are the results of a fragmented healthcare system that leaves discharged patients with preventable flaws such as hospital-acquired infections and other complications, poor planning for follow-up care transitions, inadequate communication of discharge instructions, and failure to reconcile and coordinate medications.

Variations in rate of readmission by medical facility and by geographic region also indicate that some hospitals perform better than others at containing readmission rates. In addition, effective October 2012, as directed by Patient Protection and Affordable Care Act (PPACA), the Centers for Medicare and Medicaid Services (CMS) started to cut hospitals’ reimbursement funds that have excess readmission rates for their heart failure, myocardial infarction, and pneumonia patients. Hence, reducing unnecessary rehospitalization through care transition programs has attracted policymakers and health organizations as a way to simultaneously improve quality of care and reduce costs. Yet, there is a lack of analytical tools that help understand the care transition dynamics at various patients’ health episodes and effectively provide predictions of readmission risks.
of different patient groups and hospital operation units by using diverse data from electronic health records.

Concentration on reducing unnecessary readmission has never been higher, especially with the CMS augmenting the rates of penalties and introducing new waves of diseases that will be under scrutiny during next years. In response to this policy shift, hospitals and clinicians are become more interested in analytics ways to identify patients at elevated risk of avoidable readmission, since such tools can ultimately be used to guide more appropriate discharge planning and efficient resource utilization. Although a variety of approaches have been proposed to identify patients with higher risk, their potentials have been limited mainly because they do not incorporate timing of readmission in their prediction and/or they are not accurate enough.

In this study, we make several contributions to readmission reduction studies. First, we address the problem of characterizing avoidable (or unnecessary) readmissions from all other types of outcomes. Our algorithm (PAR) is based on administrative data and takes a more accurate look at preventability components of rehospitalization compared to existing methods. We also suggest using a more comprehensive risk adjustment tool (DCG/HCC) in counting avoidable readmissions, as well as getting help from other sources of information, like clinic visits between index admission and readmission, in assessing the avoidability of readmissions.

Second, we assert that the government-endorsed 30-day timeframe that is used to count readmissions is not “optimal” for chronic conditions such as COPD. Therefore, we develop a stochastic model based on Coxian phase-type distribution to analytically calculate the optimum cut-point that best stratifies among quickly-readmitted and slowly-
readmitted COPD patients. We then adopt the new time window in the PAR algorithm to adjust for COPD readmissions.

Third, by combining algorithmic and data models, we put forward a hybrid predictive approach that exploits good aspects of classification and timing-based analytics models. We then demonstrate the superiority of our model over current solutions with respect to various accuracy criteria. Further, to confirm that the high discrimination ability of our proposal is irrespective to overfitting, we perform internal and external validation practices. Also, unlike some studies in the literature, we do not limit our work to a specific disease or within a specific hospital (Smith et al., 1996), but instead we aggregate data from four different VA facilities containing inpatients diagnosed with four different conditions.

Even though our results introduce new aspects of readmission studies, one should pay attention to some limitations in interpreting and generalizing them. First, the data used in the study is from one region (Veteran Integrated Service Network 11, Veterans In Partnership) in the State of Michigan, with a veteran population that is mostly male and veteran, and a government-funded care delivery system; hence the results may not be identical in other health care systems. Second, the study is limited to administrative data (that are regularly available to all health plans) and it does not have laboratory test results and vital signs such as hemoglobin or serum level at discharge, which may affect the risk of unnecessary readmission.

In future work, we plan to use our proposal to compare and profile the hospitals on their readmission rates using proper risk adjustment for case mix and service mix. The approach currently employed by the CMS (and the VHA) is to calculate a ratio of
observed to expected outcomes for a given hospital, and evaluate it across the normal range of all other hospitals given the same mix. Methods in this context are primarily based on models in which the hospital effects on outcome are taken as random. Nonetheless, they have been recently argued because 1) they often produce biased estimates of outcomes at the provider level; and 2) they cannot prevent confounding issues when the patient characteristics are correlated with facility effects (Kalbfleisch, Wolfe, 2013).
REFERENCES


Demuth H, Beale M (1993) Neural network toolbox for use with MATLAB.


ABSTRACT

AN ANALYTICS APPROACH TO REDUCING HOSPITAL READMISSION

by

ISSAC SHAMS

August 2014

Advisor: Dr. Kai Yang

Major: Industrial Engineering

Degree: Doctor of Philosophy

One of the significant sources of waste in the United States health care systems is preventable hospital readmission. About 2.3 million Medicare fee-for-service beneficiaries are re-hospitalized within 30 days after discharge which incurs an annual cost of $17 billion. However, it is reported by the Medicare Payment Advisory Commission that about 75% of such readmissions can and should be avoided because they are the results of factors such as poor planning for follow up care transitions, inadequate communication of discharge instructions, and failure to reconcile and coordinate medications. Hence, reducing unnecessary rehospitalization through care transition and systems engineering principles has attracted policymakers and health organizations as a way to simultaneously improve quality of care and reduce costs.

In this dissertation we investigated predictive and prescriptive analytics approaches for discharge planning and hospital readmission problem. Motivated by the gaps in research, we first develop a new readmission metric based on administrative data that can
identify potentially avoidable readmissions from all other types of readmission. The approach is promising and uses a comprehensive risk adjustment, Diagnostic Cost Group Hierarchical Condition Category, to assess the clinical relevance between a readmission and its initial hospitalizations. Next, we tackle the difficulties around selecting an appropriate readmission time interval by proposing a generic Continuous Time Markov Chain (CTMC) approach conceptualizing the movements of patients after discharge. We found that cutoff point defining readmission time interval must not depend on the instantaneous risk of readmission but rather it has to be based on quality of inpatient or outpatient care received. We further assert that the government endorsed 30 day time window which has been used for profiling hospitals and public reporting is not appropriate for chronic conditions such as chronic obstructive pulmonary disease. Thus, we propose a special case of the CTMC method and obtain the “optimal” cut-point that best stratifies among inpatient and outpatient care episodes.

Third, we proposed a novel tree-based prediction method, phase-time survival forest (PTSF), for patient risk of readmission that combines good aspects of traditional classification methods and timing-based models. The method is simple to implement and can be able to (1) model the effect of partially known information (censored observations) into the risk of readmission, and (2) directly incorporate patient’s history of readmission and risk factors changes over time. The latter property is highly favorable especially when repeated measurements of patient factors or recurrent readmissions are likely. The basic idea is quite generic and it works by modifying the traditional replicate based bootstrap samples to account for correlations among repeated records of a subject. We demonstrated the superiority of our model over current solutions with respect to
various accuracy and misclassification criteria. Further, to confirm that the high discrimination ability of our proposal is irrespective to overfitting, we performed internal and external validation with 2011–12 Veterans Health Administration data from inpatients hospitalized for heart failure, acute myocardial infarction, pneumonia, or chronic obstructive pulmonary disease in the Mid-West facilities. Results indicated improved discrimination power compared to the literature (c-statistics greater than 80%) and good calibration.

Overall, the current research outlined a successful multifaceted analytics framework that enables medical decision makers to systematically characterize, predict, and reduce avoidable readmissions and contribute to patient care quality improvements.
AUTOBIOGRAPHICAL STATEMENT

Issac Shams was born in Tehran, Iran on February 4, 1986. He received the Bachelor of Science in Industrial Engineering in 2008 and Master of Science degree in Industrial Engineering in 2011 from Iran University of Science and Technology. In 2011, he got admitted for Ph.D. program in the Industrial and Systems Engineering at the Wayne State University, Detroit, Michigan / USA. When he was Ph.D. student, he worked as a research assistant in Healthcare Systems Engineering Group under supervision of Dr. Kai Yang. After his graduation, he plans to continue his research as a postdoctoral fellow in department of Industrial and Operations Engineering at University of Michigan, Ann Arbor.

During his studies at Wayne State University and Iran University of Science and Technology, he made a number of technical presentations at INFORMS, IIE and several conferences and he nominated three times for best paper award in WCE and IAENG conferences. His articles have been published and/or are under review in journals like IIE Transactions, Healthcare Management Science, Computer and Industrial Engineering, Intelligent Manufacturing Systems and Health Service Research. He is a member of INFORMS, IIE, ASQ, ASA, IMS and he is certified by CSSBB, SAS 9, and EFQM.