A Weighted Moving Average Process for Forecasting

Shou Hsing Shih  
University of South Florida, sshih@mail.usf.edu

Chris P. Tsokos  
University of South Florida, profcpt@cas.usf.edu

Follow this and additional works at: http://digitalcommons.wayne.edu/jmasm
Part of the Applied Statistics Commons, Social and Behavioral Sciences Commons, and the Statistical Theory Commons

Recommended Citation
DOI: 10.22237/jmasm/1209615240
Available at: http://digitalcommons.wayne.edu/jmasm/vol7/iss1/15
A Weighted Moving Average Process for Forecasting

Shou Hsing Shih       Chris P. Tsokos
University of South Florida

The object of the present study is to propose a forecasting model for a nonstationary stochastic realization. The subject model is based on modifying a given time series into a new k-time moving average time series to begin the development of the model. The study is based on the autoregressive integrated moving average process along with its analytical constrains. The analytical procedure of the proposed model is given. A stock XYZ selected from the Fortune 500 list of companies and its daily closing price constitute the time series. Both the classical and proposed forecasting models were developed and a comparison of the accuracy of their responses is given.

Key words: ARIMA, moving average, stock, time series analysis

Introduction


The subject of the present study is to begin with a given time series that characterizes an economic or any other natural phenomenon and as usual, is nonstationary. Box and Jenkins (1994) have introduced a popular and useful classical procedure to develop forecasting models that have been shown to be quite effective. In the present study, we introduce a procedure for developing a forecasting model that is more effective than the classical approach is introduced. For a given stationary or nonstationary time series, \( \{x_t\} \), generate a k-day moving average time series, \( \{y_t\} \), and the developmental process begins.

Basic concepts and analytical methods are reviewed that are essential in structuring the proposed forecasting model. The review is based on the autoregressive integrated moving average processes. The accuracy of the proposed forecasting model is illustrated by selecting from the list of Fortune 500 companies, company XYZ, and considering its daily closing prices for 500 days. The classical time series model for the subject information along with the proposed process was developed. A statistical comparison based on the actual and forecasting residuals is given, both in tabular and graphical form.

Proposed Forecasting Model: k-th Moving Average

Before introducing the proposed forecasting model, several important mathematical concepts will be defined that are essential in developing the analytical process. It
A WEIGHTED MOVING AVERAGE PROCESS FOR FORECASTING

is known that it is not possible to proceed in building a time series model without conforming to certain mathematical constrains such as stationarity of a given stochastic realization. Almost always, the time series that are given are nonstationary in nature and then, it is necessary to proceed to reduce it into being stationary. Let \( \{x_t\} \) be the original time series. The difference filter is given by

\[
(1 - B)^d,
\]

where \( B^d x_t = x_{t-d} \), and \( d \) is the degree of differencing of the series.

In time series analysis, the primary use for the \( k \)-th moving average process is for smoothing a realized time series. It is very useful in discovering a short-term, long-term trends and seasonal components of a given time series. The \( k \)-th moving average process of a time series \( \{x_t\} \) is defined as follows:

\[
y_t = \frac{1}{k} \sum_{j=0}^{k-1} x_{t-k+j} ,
\]

where \( t = k, k+1, \ldots, n \). It can be seen that as \( k \) increases, the number of observations \( k \) of \( \{y_t\} \) decreases, and \( \{y_t\} \) gets closer and closer to the mean of \( \{x_t\} \) as \( k \) increases. In addition, when \( k = n \), \( \{y_t\} \) reduces to only a single observation, and equals \( \mu \), that is

\[
y_t = \frac{1}{n} \sum_{j=1}^{n} x_j = \mu ,
\]

The proposed model is developed by transforming the original time series \( \{x_t\} \) into \( \{y_t\} \) by applying (2). After establishing the new time series, usually nonstationary, the process of reducing it into a stationary time series is begun. Kwiatkowski, Phillips, Schmit, and Shin (1992) introduced the KPSS Test to check the level of stationarity of a time series. The differencing order \( d \) is applied to the new time series \( \{y_t\} \) for \( d = 0,1,2, \ldots \), then verify the stationarity of the series with the KPSS test until the series become stationary. Therefore, the nonstationary time series is reduced into a stationary one after a proper number of differencing. The model building procedure is then developed via the proposed forecasting model.

After choosing a proper degree of differencing \( d \), assume different orders for the autoregressive integrated moving average model, ARIMA\((p,d,q)\), also known as Box and Jenkins method, where \((p,d,q)\) represent the order of the autoregressive process, the order of differencing and the order of the moving average process, respectively. The ARIMA\((p,d,q)\) is defined as follows:

\[
\phi_p(B)(1 - B)^d y_t = \theta_q(B) \epsilon_t ,
\]

where \( \{y_t\} \) is the realized time series, \( \phi_p \) and \( \theta_q \) are the weights or coefficients of the AR and MA that drive the model, respectively, and \( \epsilon_t \) is the random error. Write \( \phi_p \) and \( \theta_q \) as

\[
\phi_p(B) = (1 - \phi_1 B - \phi_2 B^2 - \ldots - \phi_p B^p) ,
\]

and

\[
\theta_q(B) = (1 - \theta_1 B - \theta_2 B^2 - \ldots - \theta_q B^q) .
\]

In time series analysis, sometimes it is very difficult to make a decision in selecting the best order of the ARIMA\((p,d,q)\) model when there are several models that all adequately represent a given set of time series. Hence, Akaike’s information criterion (AIC) (1974), plays a major role when it comes to model selection. AIC was introduced by Akaike in 1973, and it is defined as:

\[
\text{AIC}(M) = -2 \ln[\text{maximum likelihood}] + 2M ,
\]

where \( M \) is the number of parameters in the model and the unconditional log-likelihood function suggested by Box, Jenkins, and Reinsel (1994), is given by

\[
\ln L(\phi, \mu, \theta, \sigma^2) = -\frac{n}{2} \ln 2\pi \sigma^2 - \frac{S(\phi, \mu, \theta)}{2\sigma^2} ,
\]

where \( S(\phi, \mu, \theta) \) is the unconditional sum of squares function given by
\[ S(\phi, \mu, \theta) = \sum_{t=-\infty}^{n} [E(\varepsilon_t | \phi, \mu, \theta, y)]^2 \]  

(9)

where \( E(\varepsilon_t | \phi, \mu, \theta, y) \) is the conditional expectation of \( \varepsilon_t \) given \( \phi, \mu, \theta, y \).

The quantities \( \hat{\phi}, \hat{\mu}, \) and \( \hat{\theta} \) that maximize (8) are called unconditional maximum likelihood estimators. Since \( \ln L(\phi, \mu, \theta; \sigma^2_{\varepsilon}) \) involves the data only through \( (\phi, \mu, \theta; S) \), these unconditional maximum likelihood estimators are equivalent to the unconditional least squares estimators obtained by minimizing \( S(\phi, \mu, \theta) \).

In practice, the summation in (9) is approximated by a finite form

\[ S(\phi, \mu, \theta) = \sum_{t=M}^{n} [E(\varepsilon_t | \phi, \mu, \theta, y)]^2 \]  

(10)

where \( M \) is a sufficiently large integer such that the back cast increment \( |E(\varepsilon_t | \phi, \mu, \theta, y) - E(\varepsilon_{t-1} | \phi, \mu, \theta, y)| \) is less than any arbitrary predetermined small \( \varepsilon \) value for \( t \leq -(M + 1) \). This expression implies that \( E(\varepsilon_t | \phi, \mu, \theta, y) \equiv \mu \); hence, \( E(\varepsilon_t | \phi, \mu, \theta, y) \) is negligible for \( t \leq -(M + 1) \).

After obtaining the parameter estimates \( \hat{\phi}, \hat{\mu}, \) and \( \hat{\theta} \), the estimate \( \hat{\sigma}^2_{\varepsilon} \) of \( \sigma^2_{\varepsilon} \) can then be calculated from

\[ \hat{\sigma}^2_{\varepsilon} = \frac{S(\hat{\phi}, \hat{\mu}, \hat{\theta})}{n} \]  

(11)

For an ARMA\((p,q)\) model based on \( n \) observations, the log-likelihood function is

\[ \ln L = -\frac{n}{2} \ln 2\pi \sigma^2_{\varepsilon} - \frac{1}{2} \frac{n}{2} S(\phi, \mu, \theta). \]  

(12)

Proceed to maximize (12) with respect to the parameters \( \phi, \mu, \theta, \) and \( \sigma^2_{\varepsilon} \), from (11),

\[ \ln \hat{L} = -\frac{n}{2} \ln \hat{\sigma}^2_{\varepsilon} - \frac{n}{2} (1 + \ln 2\pi). \]  

(13)

Because the second term in expression (13) is a constant, we can reduce the AIC to the following expression

\[ \text{AIC}(M) = n \ln \hat{\sigma}^2_{\varepsilon} + 2M. \]  

(14)

Then, an appropriate time series model is generated and the statistical process with the smallest AIC can be selected. The model identified will possess the smallest average mean square error. The development of the model is summarized as follows.

- Transform the original time series \( \{x_t\} \) into a new series \( \{y_t\} \).
- Check for stationarity of the new time series \( \{y_t\} \) by determining the order of differencing \( d \), where \( d = 0, 1, 2, \ldots \) according to KPSS test, until stationarity is achieved.
- Decide the order \( m \) of the process. For this case, let \( m = 5 \) where \( p + q = m \).
- After \( (d, m) \) is selected, list all possible set of \( (p, q) \) for \( p + q \leq m \).
- For each set of \( (p, q) \), estimate the parameters of each model, that is, \( \phi_1, \phi_2, \ldots, \phi_p, \theta_1, \theta_2, \ldots, \theta_q \).
- Compute the AIC for each model, and choose the one with smallest AIC.

According to the criterion mentioned above, the ARIMA\((p,d,q)\) model can be obtained that best fit a given time series, where the coefficients are \( \phi_1, \phi_2, \ldots, \phi_p, \theta_1, \theta_2, \ldots, \theta_q \).

Using the model that we developed for \( \{y_t\} \) and subject to the AIC criteria, we forecast values of \( \{y_t\} \) and proceed to apply the back-shift operator to obtain estimates of the original phenomenon \( \{x_t\} \), that is,

\[ \hat{x}_t = k \hat{y}_{t-k} - x_{t-1} - x_{t-2} - \ldots - x_{t-k+1}. \]  

(15)

The proposed model and the corresponding procedure discussed in this section shall be illustrated with real economic application and the results will be compared with the classical time series model.
A WEIGHTED MOVING AVERAGE PROCESS FOR FORECASTING

Figure 1. Daily Closing Price for Stock XYZ

Figure 2. Comparisons on Classical ARIMA Model VS. Original Time Series for the Last 100 Observations
Application: Forecasting Stock XYZ

A stock was selected from Fortune 500 companies that we identify a (XYZ). The daily closing price for 500 days constitutes the time series \( \{ x_t \} \). A plot of the actual information is given by Figure 1.

First, develop a time series forecasting model of the given nonstationary data using the ordinary Box and Jenkins methodology. Secondly, we shall modify the given data, Figure 1, to develop the proposed time series forecasting model. A comparison of the two models will be given.

The general theoretical form of the ARIMA(p,d,q) is given by

\[
\phi_p(B)(1-B)^d x_t = \theta_q(B)\epsilon_t
\]  \hspace{1cm} (16)

Following the Box and Jenkins’ methodology (1994), the classical forecasting model with the best AIC score is the ARIMA(1,1,2). That is, a combination of first order autoregressive (AR) and a second order moving average (MA) with a first difference filter. Thus, write it as

\[
(1-.9631B)(1-B)x_t = (1-1.0531B+.0581B^2)\epsilon_t
\]  \hspace{1cm} (17)

After expanding the autoregressive operator and the difference filter,

\[
(1-1.9631B+.9631B^2)x_t = (1-1.0531B+.0581B^2)\epsilon_t
\]  \hspace{1cm} (18)

and rewrite the model as

\[
\begin{array}{c|c|c|c|c}
\bar{r} & S_r^2 & S_r & S_r/\sqrt{n} \\
0.02209169 & 0.1445187 & 0.3801562 & 0.0170011 \\
\end{array}
\]
A WEIGHTED MOVING AVERAGE PROCESS FOR FORECASTING

Table 2. Actual and Predicted Price

<table>
<thead>
<tr>
<th>N</th>
<th>Actual Price</th>
<th>Predicted Price</th>
<th>Residuals</th>
</tr>
</thead>
<tbody>
<tr>
<td>476</td>
<td>26.78</td>
<td>26.8473</td>
<td>-0.0673</td>
</tr>
<tr>
<td>477</td>
<td>26.75</td>
<td>26.7976</td>
<td>-0.0476</td>
</tr>
<tr>
<td>478</td>
<td>26.67</td>
<td>26.7673</td>
<td>-0.0972</td>
</tr>
<tr>
<td>479</td>
<td>26.8</td>
<td>26.6922</td>
<td>0.1078</td>
</tr>
<tr>
<td>480</td>
<td>26.73</td>
<td>26.8064</td>
<td>-0.0764</td>
</tr>
<tr>
<td>481</td>
<td>26.78</td>
<td>26.7490</td>
<td>0.0310</td>
</tr>
<tr>
<td>482</td>
<td>26.27</td>
<td>26.7911</td>
<td>-0.5211</td>
</tr>
<tr>
<td>483</td>
<td>26.12</td>
<td>26.3277</td>
<td>-0.2077</td>
</tr>
<tr>
<td>484</td>
<td>26.32</td>
<td>26.1631</td>
<td>0.1569</td>
</tr>
<tr>
<td>485</td>
<td>25.98</td>
<td>26.3364</td>
<td>-0.3564</td>
</tr>
<tr>
<td>486</td>
<td>25.86</td>
<td>26.0349</td>
<td>-0.1749</td>
</tr>
<tr>
<td>487</td>
<td>25.65</td>
<td>25.9068</td>
<td>-0.2568</td>
</tr>
<tr>
<td>488</td>
<td>25.67</td>
<td>25.6670</td>
<td>0.0031</td>
</tr>
<tr>
<td>489</td>
<td>26.02</td>
<td>25.7119</td>
<td>0.3081</td>
</tr>
<tr>
<td>490</td>
<td>26.01</td>
<td>26.0335</td>
<td>-0.0235</td>
</tr>
<tr>
<td>491</td>
<td>26.11</td>
<td>26.0427</td>
<td>0.0674</td>
</tr>
<tr>
<td>492</td>
<td>26.18</td>
<td>26.1343</td>
<td>0.0457</td>
</tr>
<tr>
<td>493</td>
<td>26.28</td>
<td>26.2032</td>
<td>0.0768</td>
</tr>
<tr>
<td>494</td>
<td>26.39</td>
<td>26.2986</td>
<td>0.0914</td>
</tr>
<tr>
<td>495</td>
<td>26.46</td>
<td>26.4043</td>
<td>0.0557</td>
</tr>
<tr>
<td>496</td>
<td>26.18</td>
<td>26.4743</td>
<td>-0.2943</td>
</tr>
<tr>
<td>497</td>
<td>26.32</td>
<td>26.2219</td>
<td>0.0981</td>
</tr>
<tr>
<td>498</td>
<td>26.16</td>
<td>26.3354</td>
<td>-0.1754</td>
</tr>
<tr>
<td>499</td>
<td>26.24</td>
<td>26.1953</td>
<td>0.0447</td>
</tr>
<tr>
<td>500</td>
<td>26.07</td>
<td>26.2602</td>
<td>-0.1902</td>
</tr>
</tbody>
</table>

\[ x_t = 1.9631x_{t-1} - .9631x_{t-2} + 0.581ε_{t-2} \]
\[ ε_t = -1.0531ε_{t-1} + 0.0581ε_{t-2} \] (19)

by letting \( ε_t = 0 \), there is the one day ahead forecasting time series of the closing price of stock XYZ as

\[ \hat{x}_t = 1.9631x_{t-1} - .9631x_{t-2} \]
\[ -1.0531ε_{t-1} + 0.0581ε_{t-2} \] (20)

Using the above equation, graph the forecasting values obtained by using the classical approach on top of the original time series, as shown by Figure 2.

The basic statistics that reflect the accuracy of model (20) are the mean \( \bar{r} \), variance \( S^2_r \), standard deviation \( S_r \) and standard error \( \frac{S_r}{\sqrt{n}} \) of the residuals. Figure 3 gives a plot of the residual and Table 1 gives the basic statistics.

Furthermore, restructure the model (20) with \( n = 475 \) data points to forecast the last 25
observations using only the previous information. The purpose is to see how accurate our forecast prices are with respect to the actual 25 values that have not been used. Table 2 gives the actual price, predicted price, and residuals between the forecasts and the 25 hidden values.

The average of these residuals is \( \bar{r} = -0.05608 \).

Proceed to develop the proposed forecasting model. The original time series of stock XYZ daily closing prices is given by Figure 1. The new time series is being created by \( k = 3 \) days moving average and the analytical form of \( \{ y_t \} \) is given by

\[
y_t = \frac{x_{t-2} + x_{t-1} + x_t}{3} \quad (21)
\]

Figure 4 shows the new time series \( \{ y_t \} \) along with the original time series \( \{ x_t \} \), that will be used to develop the proposed forecasting model.

Following the procedure stated above, the best model that characterizes the behavior of \( \{ y_t \} \) is ARIMA (2,1,3). That is, \[
(1-0.8961B-0.0605B^2)(1-B)y_t = (22) \\
(1+0.0056B-0.0056B^2-B^3)e_t
\]

Expanding the autoregressive operator and the first difference filter, we have

\[
(1-1.8961B+0.8356B^2+0.0605B^3)y_t = (23) \\
(1+0.0056B-0.0056B^2-B^3)e_t
\]

Thus, write (23) as

\[
y_t = 1.8961y_{t-1} - 0.8356y_{t-2} - 0.0605y_{t-3} \\
+ e_t + 0.0056e_{t-1} - 0.0056e_{t-2} - e_{t-3} \quad (24)
\]

The final analytical form of the proposed forecasting model can be written as

\[
y_t = 1.8961y_{t-1} - 0.8356y_{t-2} - 0.0605y_{t-3} \\
+ 0.0056e_{t-1} - 0.0056e_{t-2} - e_{t-3} \quad (25)
\]

Using the above equation, a plot of the developed model (25), showing a one day ahead
A WEIGHTED MOVING AVERAGE PROCESS FOR FORECASTING

Figure 5. Comparisons on Our Proposed Model VS. Original Time Series for the Last 100 Observations

Figure 6. Time Series Plot for Residuals for Our Proposed Model
### Table 3. Basic Evaluation Statistics

<table>
<thead>
<tr>
<th>( \tilde{r} )</th>
<th>( S^2 )</th>
<th>( S_r )</th>
<th>( S_r / \sqrt{n} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.01016814</td>
<td>0.1437259</td>
<td>0.3791119</td>
<td>0.01698841</td>
</tr>
</tbody>
</table>

### Table 4. Actual and Predicted Price

<table>
<thead>
<tr>
<th>N</th>
<th>Actual Price</th>
<th>Predicted Price</th>
<th>Residuals</th>
</tr>
</thead>
<tbody>
<tr>
<td>476</td>
<td>26.78</td>
<td>26.8931</td>
<td>-0.1131</td>
</tr>
<tr>
<td>477</td>
<td>26.75</td>
<td>26.7715</td>
<td>-0.0215</td>
</tr>
<tr>
<td>478</td>
<td>26.67</td>
<td>26.7121</td>
<td>-0.0421</td>
</tr>
<tr>
<td>479</td>
<td>26.8</td>
<td>26.7239</td>
<td>0.0761</td>
</tr>
<tr>
<td>480</td>
<td>26.73</td>
<td>26.7854</td>
<td>-0.0554</td>
</tr>
<tr>
<td>481</td>
<td>26.78</td>
<td>26.6892</td>
<td>0.0908</td>
</tr>
<tr>
<td>482</td>
<td>26.27</td>
<td>26.8292</td>
<td>-0.5592</td>
</tr>
<tr>
<td>483</td>
<td>26.12</td>
<td>26.3027</td>
<td>-0.1827</td>
</tr>
<tr>
<td>484</td>
<td>26.32</td>
<td>26.0808</td>
<td>0.2392</td>
</tr>
<tr>
<td>485</td>
<td>25.98</td>
<td>26.3603</td>
<td>-0.3803</td>
</tr>
<tr>
<td>486</td>
<td>25.86</td>
<td>25.9868</td>
<td>-0.1268</td>
</tr>
<tr>
<td>487</td>
<td>25.65</td>
<td>25.8443</td>
<td>-0.1943</td>
</tr>
<tr>
<td>488</td>
<td>25.67</td>
<td>25.7115</td>
<td>-0.0414</td>
</tr>
<tr>
<td>489</td>
<td>26.02</td>
<td>25.6499</td>
<td>0.3701</td>
</tr>
<tr>
<td>490</td>
<td>26.01</td>
<td>25.9650</td>
<td>0.0450</td>
</tr>
<tr>
<td>491</td>
<td>26.11</td>
<td>26.0526</td>
<td>0.0574</td>
</tr>
<tr>
<td>492</td>
<td>26.18</td>
<td>26.0912</td>
<td>0.0888</td>
</tr>
<tr>
<td>493</td>
<td>26.28</td>
<td>26.1449</td>
<td>0.1351</td>
</tr>
<tr>
<td>494</td>
<td>26.39</td>
<td>26.3090</td>
<td>0.0810</td>
</tr>
<tr>
<td>495</td>
<td>26.46</td>
<td>26.3752</td>
<td>0.0848</td>
</tr>
<tr>
<td>496</td>
<td>26.18</td>
<td>26.4223</td>
<td>-0.2423</td>
</tr>
<tr>
<td>497</td>
<td>26.32</td>
<td>26.2461</td>
<td>0.0739</td>
</tr>
<tr>
<td>498</td>
<td>26.16</td>
<td>26.2964</td>
<td>-0.1364</td>
</tr>
<tr>
<td>499</td>
<td>26.24</td>
<td>26.1437</td>
<td>0.0963</td>
</tr>
<tr>
<td>500</td>
<td>26.07</td>
<td>26.2678</td>
<td>-0.1978</td>
</tr>
</tbody>
</table>
A WEIGHTED MOVING AVERAGE PROCESS FOR FORECASTING

Table 5. Basic Comparison on Classical Approach VS. Our Proposed Model

<table>
<thead>
<tr>
<th></th>
<th>$\bar{r}$</th>
<th>$S_r^2$</th>
<th>$S_r$</th>
<th>$S_r/\sqrt{n}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Classical</td>
<td>0.02209169</td>
<td>0.1445187</td>
<td>0.3801562</td>
<td>0.0170011</td>
</tr>
<tr>
<td>Proposed</td>
<td>0.01016814</td>
<td>0.1437259</td>
<td>0.3791119</td>
<td>0.01698841</td>
</tr>
</tbody>
</table>

forecasting along with the new time series, $\{y_t\}$, is displayed by Figure 5. Note the closeness of the two plots that reflect the quality of the proposed model.

Similar to the classical model approach that we discussed earlier, use the first 475 observations $\{y_1, y_2, \ldots, y_{475}\}$ to forecast $\hat{y}_{476}$. Then, use the observations $\{y_1, y_2, \ldots, y_{476}\}$ to forecast $\hat{y}_{477}$, and continue this process until forecasts are obtained for all the observations, that is, $\{\hat{y}_{476}, \hat{y}_{477}, \ldots, \hat{y}_{500}\}$. From equation (21), the relationship can be seen between the forecasting values of the original series $\{x_t\}$ and the forecasting values of 3 days moving average series $\{y_t\}$, that is,

$$\hat{x}_t = 3\hat{y}_t - x_{t-1} - x_{t-2}$$  \hspace{1cm} (26)

Hence, after $\{\hat{y}_{476}, \hat{y}_{477}, \ldots, \hat{y}_{500}\}$ is estimated, use the above equation, (26), to solve the forecasting values for $\{x_t\}$. Figure 6 is the residual plot generated by the proposed model, and followed by Table 3, that includes the basic evaluation statistics.

Both of the above displayed evaluations reflect on accuracy of the proposed model. The actual daily closing prices of stock XYZ from the 476th day along with the forecasted prices and residuals are given in Table 4.

The results given above attest to the good forecasting estimates for the hidden data.

Comparison of the Forecasting Models

The two developed models are compared. The classical process is given by

$$\hat{x}_t = 1.9631x_{t-1} - .9631x_{t-2} - .10531\varepsilon_{t-1} + .0581\varepsilon_{t-2}$$  \hspace{1cm} (27)

In the proposed model, the following inversion is used to obtain the estimated daily closing prices of stock XYZ, that is,

$$\hat{y}_t = 1.8961y_{t-1} - .8356y_{t-2} - .0605y_{t-3} + .0056\varepsilon_{t-1} - .0056\varepsilon_{t-2} - \varepsilon_{t-3}$$ \hspace{1cm} (28)

in conjunction with

$$\hat{x}_t = 3\hat{y}_t - x_{t-1} - x_{t-2}$$  \hspace{1cm} (29)

Table 5 given is a comparison of the basic statistics used to evaluate the two models under investigation. The average mean residuals between the two models show that the proposed model is overall approximately 54% more effective in estimating one day ahead the closing price of Fortune 500 stock XYZ.

Conclusion

In the present study a new time series model is introduced that is based on the actual stochastic realization of a given phenomenon. The proposed model is based on modifying the given economic time series, $\{x_t\}$, and smoothing it with k-time moving average to create a new time
The basic analytical procedures are developed through the developing process of a forecasting model. A step-by-step procedure is memorized for the final computational procedure for a nonstationary time series. To evaluate the effectiveness of our proposed model, we selected a company from the Fortune 500 list, company XYZ, the daily closing prices of the stock for 500 days was used as our time series data, \( \{ x_t \} \), which was as usual nonstationary. We developed the classical time series forecasting model using the Box and Jenkins methodology and also our proposed model, \( \{ y_t \} \), based on a 3-way moving average smoothing procedure. The analytical form of the two forecasting models is presented and a comparison of them is also given. Based on the average mean residuals, the proposed model was significantly more effective in such terms of predicting the closing daily prices of the stock XYZ.

References


