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# A Comparison of the Spearman-Brown and Flanagan-Rulon Formulas for Split Half Reliability under Various Variance Parameter Conditions

## David A. Walker Northern Illinois University

Differences between the Spearman-Brown and Flanagan-Rulon formulas are examined when the variance parameters for two halves of a test had the following ratios: 1.0, 1.1, 1.2, 1.3, 1.4, 1.5, 1.6, 1.7, 1.8, 1.9, 2.0 and also had a correlation between the two halves of a test at 1.00, .95, .90, .80, .70, .60, .50, .40, .30, .20, .10, .05. It was found that use of the Spearman-Brown formula to estimate the population ρ when the ratio between the standard deviations on two halves of a test is disparate, or beyond .9 to 1.1, was not warranted. Applied and theoretical examples are employed, as well as syntax for user application.

Key words: Split half reliability, Spearman-Brown, Flanagan-Rulon

#### Introduction

Examination of the difference between estimators of the population  $\rho$  for split-half reliability has been studied in the past (Charter, 1996, Cronbach, 1951, Feldt & Brennan, 1989, Kelley, 1942, Rulon, 1939, Stanley, 1971). To estimate the score reliability of a test split in half, the Spearman-Brown formula is the typical method used. Charter (1996) showed that:

$$r = 2r_{xy} / (1 + r_{xy}) \tag{1}$$

where,  $r_{xy}$  = the correlation between the two halves of a test.

One major assumption with this formula is that the two halves of a test have equal variance parameters. Rulon (1939, attributed to Flanagan) proposed a split-half formula for use when the variance parameters where unequal. Charter (1996) showed that:

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$$r = (4r_{xy} SD_x SD_y) / (SDx^2 + SDy^2 + 2r_{xy} SD_x SD_y)$$
(2)

where,  $SD_x$  and  $SD_y$  are the standard deviations for the two halves of the test.

Cronbach (1951), and more recently Charter (1996), found that when the standard deviations of the two halves of a test are not equal, that is, the previously-noted major assumption guiding the Spearman-Brown formula is violated; its use will lead to an overestimation of the reliability coefficient.

#### Purpose

The purpose of this research is to elaborate upon the work of Cronbach (1951) and Charter (1996) and strengthen the evidence in the literature that indicates that in most instances when unequal standard deviations for two halves of a test are present, regardless of the correlation between the two halves, the Flanagan-Rulon formula is the better estimator of p in a splithalves reliability situation. Thus, this research will build upon Cronbach's work and show, via various graphs and a detailed table, the differences between the Spearman-Brown formula and the Flanagan-Rulon formula when the variance parameters for two halves of a test have the following ratios (either greater or lesser): 1.0, 1.1, 1.2, 1.3, 1.4, 1.5, 1.6, 1.7, 1.8, 1.9. 2.0 and also have a correlation between the two halves of a test at 1.00, .95, .90, .80, .70,

.60, .50, .40, .30, .20, .10, .05. As well, SPSS (Statistical Package for the Social Sciences) syntax is provided in the Appendix section for users to create Tables 1 and 2 or calculate a Spearman-Brown or Flanagan-Rulon value given certain data.

#### Results

As was found by both Cronbach (1951) and Charter (1996), a large discrepancy between the variance parameters on the two halves of a test results in a substantial decrease in r. A small difference between standard deviations has the opposite effect, which is to be expected. Cronbach noted that when the ratio between the standard deviations of the two halves of a test are .9 to 1.1, the results from either the Spearman-Brown or the Flanagan-Rulon

formulas are virtually the same and thus, the former formula should be used.

For example from empirical data, Gordon (1970) used the Musical Aptitude Profile (i.e., n = 190, under normal distribution. and with non-missing data) and estimated the split half reliability via the Spearman-Brown method. These data yielded a range of ratios between variance parameters of .9 to 1.1 (i.e., .949 to 1.141), which produced Spearman-Brown and Flanagan-Rulon values that were nearly identical. That is, there was no discrepancy between the Spearman-Brown formula results and Flanagan-Rulon estimates (i.e., the ratio of Spearman-Brown to Flanagan-Rulon ranged from 1.000 to 1.005). Thus, in this instance, the Spearman-Brown formula did not over-estimate the population p and was the proper choice.

Table 1. Comparison of SB and FR Estimates Using the Musical Aptitude Profile

$\mathcal{L}_{xy}$	$\mathrm{SD}_1$	$\mathrm{SD}_2$	SD Ratio	SB	FR	Ratio of
						SB to FR
(05	0.57	10.00	040	020	010	1 001
.695	9.57	10.08	.949	.820	.819	1.001
.600	10.01	9.59	1.044	.750	.750	1.000
.818	9.17	8.93	1.027	.900	.900	1.000
.600	7.66	7.29	1.051	.750	.749	1.001
.575	9.33	8.69	1.074	.730	.729	1.002
.786	7.71	6.76	1.141	.880	.876	1.005
.563	9.28	9.03	1.028	.720	.720	1.000
.600	10.20	9.14	1.116	.750	.747	1.004
.538	8.96	8.28	1.082	.700	.698	1.002
.818	7.95	7.22	1.101	.900	.898	1.003
.905	7.06	6.56	1.076	.950	.949	1.001

 $r_{xy}$  = correlation between two halves of a test, SD<sub>1</sub> & SD<sub>2</sub> = standard deviations for two halves of a test, SD Ratio = SD<sub>1</sub> / SD<sub>2</sub>, SB = Spearman-Brown, FR = Flanagan-Rulon, Ratio of SB to FR = SB / FR

*Note*. Table adapted from Gordon (1970), where SB was reported only and not  $r_{xy}$ . To calculate  $r_{xy}$  the inverse of the SB formula was applied, where  $r_{xy} = \frac{(SB_r/2)}{(1-r_{SB})}$ .

The current research extended Cronbach (1951) and Charter's (1996) work by creating a detailed table and figures which demonstrated that the range of the ratio between the standard deviations for two halves of a test could not be extended beyond .9 to 1.1. Table 2 shows that the deviation between the results yielded by the Spearman-Brown and Flanagan-Rulon formulas

when the variance parameter ratio was .9 to 1.1 had a decrease in r of < 1% and a Spearman-Brown to Flanagan-Rulon ratio range difference < 1%. This was not the case, though, when the variance parameter ratio was .8 to 1.2. The Spearman-Brown to Flanagan-Rulon ratio was  $\geq$  1% starting at  $r_{xy}$  = .70, which generated a ratio = 1.010, and ended at  $r_{xy}$  = .05 or a ratio = 1.016.

Table 2. Comparison of SB and FR Formulas under Various  $r_{xy}$  and Variance Parameter Conditions

#### Ratio of SDs for Two Halves

	Two		Ratio	
$\mathbf{r}_{\mathbf{x}\mathbf{y}}$	Halves	SB	FR	SB to FR
1.00	2.000	1.000	.889	1.125
.95	2.000	.974	.864	1.128
.90	2.000	.947	.837	1.132
.80	2.000	.889	.780	1.139
.70	2.000	.824	.718	1.147
.60	2.000	.750	.649	1.156
.50	2.000	.667	.571	1.167
.40	2.000	.571	.485	1.179
.30	2.000	.462	.387	1.192
.20	2.000	.333	.276	1.208
.10	2.000	.182	.148	1.227
.05	2.000	.095	.077	1.238
1.00	1.900	1.000	.904	1.107
.95	1.900	.974	.878	1.109
.90	1.900	.947	.852	1.112
.80	1.900	.889	.795	1.118
.70	1.900	.824	.732	1.125
.60	1.900	.750	.662	1.133
.50	1.900	.667	.584	1.142
.40	1.900	.571	.496	1.152
.30	1.900	.462	.397	1.164
.20	1.900	.333	.283	1.178
.10	1.900	.182	.152	1.194
.05	1.900	.095	.079	1.203

Table 2. Continued

1.00	1.800	1.000	.918	1.089
.95	1.800	.974	.893	1.091
.90	1.800	.947	.866	1.094
.80	1.800	.889	.809	1.099
.70	1.800	.824	.746	1.105
.60	1.800	.750	.675	1.111
.50	1.800	.667	.596	1.119
.40	1.800	.571	.507	1.127
.30	1.800	.462	.406	1.137
.20	1.800	.333	.290	1.148
.10	1.800	.182	.157	1.162
.05	1.800	.095	.081	1.169
1.00	1.700	1.000	.933	1.072
.95	1.700	.974	.907	1.074
.90	1.700	.947	.881	1.076
.80	1.700	.889	.823	1.080
.70	1.700	.824	.759	1.085
.60	1.700	.750	.688	1.090
.50	1.700	.667	.608	1.096
.40	1.700	.571	.518	1.103
.30	1.700	.462	.415	1.111
.20	1.700	.333	.298	1.120
.10	1.700	.182	.161	1.131
.05	1.700	.095	.084	1.137
1.00	1.600	1.000	.947	1.056
.95	1.600	.974	.921	1.058
.90	1.600	.947	.894	1.059
.80	1.600	.889	.837	1.063
.70	1.600	.824	.772	1.066
.60	1.600	.750	.701	1.070
.50	1.600	.667	.620	1.075
.40	1.600	.571	.529	1.080
.30	1.600	.462	.425	1.087
.20	1.600	.333	.305	1.094
.10	1.600	.182	.165	1.102
.05	1.600	.095	.086	1.107

Table 2. Continued

1.00	1.500	1.000	.960	1.042
.95	1.500	.974	.934	1.043
.90	1.500	.947	.908	1.044
.80	1.500	.889	.850	1.046
.70	1.500	.824	.785	1.049
.60	1.500	.750	.713	1.052
.50	1.500	.667	.632	1.056
.40	1.500	.571	.539	1.060
.30	1.500	.462	.434	1.064
.20	1.500	.333	.312	1.069
.10	1.500	.182	.169	1.076
.05	1.500	.095	.088	1.079
1.00	1.400	1.000	.972	1.029
.95	1.400	.974	.947	1.029
.90	1.400	.947	.920	1.030
.80	1.400	.889	.862	1.032
.70	1.400	.824	.797	1.034
.60	1.400	.750	.724	1.036
.50	1.400	.667	.642	1.038
.40	1.400	.571	.549	1.041
.30	1.400	.462	.442	1.044
.20	1.400	.333	.318	1.048
.10	1.400	.182	.173	1.052
.05	1.400	.095	.090	1.054
1.00	1.300	1.000	.983	1.017
.95	1.300	.974	.957	1.018
.95 .90	1.300 1.300	.974 .947	.957 .930	1.018 1.018
.95 .90 .80	1.300 1.300 1.300	.974 .947 .889	.957 .930 .872	1.018 1.018 1.019
.95 .90 .80 .70	1.300 1.300 1.300 1.300	.974 .947 .889 .824	.957 .930 .872 .807	1.018 1.018 1.019 1.020
.95 .90 .80 .70 .60	1.300 1.300 1.300 1.300 1.300	.974 .947 .889 .824 .750	.957 .930 .872 .807 .734	1.018 1.018 1.019 1.020 1.022
.95 .90 .80 .70 .60	1.300 1.300 1.300 1.300 1.300 1.300	.974 .947 .889 .824 .750	.957 .930 .872 .807 .734 .652	1.018 1.018 1.019 1.020 1.022 1.023
.95 .90 .80 .70 .60 .50	1.300 1.300 1.300 1.300 1.300 1.300 1.300	.974 .947 .889 .824 .750 .667	.957 .930 .872 .807 .734 .652 .558	1.018 1.019 1.020 1.022 1.023 1.025
.95 .90 .80 .70 .60 .50 .40	1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.300	.974 .947 .889 .824 .750 .667 .571	.957 .930 .872 .807 .734 .652 .558	1.018 1.019 1.020 1.022 1.023 1.025 1.027
.95 .90 .80 .70 .60 .50 .40	1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.300	.974 .947 .889 .824 .750 .667 .571 .462	.957 .930 .872 .807 .734 .652 .558 .450	1.018 1.018 1.019 1.020 1.022 1.023 1.025 1.027 1.029
.95 .90 .80 .70 .60 .50 .40 .30 .20	1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.300	.974 .947 .889 .824 .750 .667 .571 .462 .333	.957 .930 .872 .807 .734 .652 .558 .450 .324	1.018 1.018 1.019 1.020 1.022 1.023 1.025 1.027 1.029 1.031
.95 .90 .80 .70 .60 .50 .40	1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.300	.974 .947 .889 .824 .750 .667 .571 .462	.957 .930 .872 .807 .734 .652 .558 .450	1.018 1.018 1.019 1.020 1.022 1.023 1.025 1.027 1.029
.95 .90 .80 .70 .60 .50 .40 .30 .20 .10	1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.300	.974 .947 .889 .824 .750 .667 .571 .462 .333 .182 .095	.957 .930 .872 .807 .734 .652 .558 .450 .324 .176 .092	1.018 1.018 1.019 1.020 1.022 1.023 1.025 1.027 1.029 1.031 1.033
.95 .90 .80 .70 .60 .50 .40 .30 .20 .10 .05	1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.300	.974 .947 .889 .824 .750 .667 .571 .462 .333 .182 .095	.957 .930 .872 .807 .734 .652 .558 .450 .324 .176 .092	1.018 1.018 1.019 1.020 1.022 1.023 1.025 1.027 1.029 1.031 1.033
.95 .90 .80 .70 .60 .50 .40 .30 .20 .10 .05	1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.200 1.200 1.200	.974 .947 .889 .824 .750 .667 .571 .462 .333 .182 .095	.957 .930 .872 .807 .734 .652 .558 .450 .324 .176 .092	1.018 1.018 1.019 1.020 1.022 1.023 1.025 1.027 1.029 1.031 1.033 1.008 1.009 1.009
.95 .90 .80 .70 .60 .50 .40 .30 .20 .10 .05	1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.200 1.200 1.200 1.200	.974 .947 .889 .824 .750 .667 .571 .462 .333 .182 .095 1.000 .974 .947 .889	.957 .930 .872 .807 .734 .652 .558 .450 .324 .176 .092 .992 .966 .939 .881	1.018 1.018 1.019 1.020 1.022 1.023 1.025 1.027 1.029 1.031 1.033 1.008 1.009 1.009
.95 .90 .80 .70 .60 .50 .40 .30 .20 .10 .05	1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.200 1.200 1.200 1.200 1.200	.974 .947 .889 .824 .750 .667 .571 .462 .333 .182 .095 1.000 .974 .947 .889 .824	.957 .930 .872 .807 .734 .652 .558 .450 .324 .176 .092 .992 .966 .939 .881 .816	1.018 1.019 1.020 1.022 1.023 1.025 1.027 1.029 1.031 1.033 1.008 1.009 1.009 1.010
.95 .90 .80 .70 .60 .50 .40 .30 .20 .10 .05 1.00 .95 .90 .80 .70	1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.200 1.200 1.200 1.200 1.200 1.200	.974 .947 .889 .824 .750 .667 .571 .462 .333 .182 .095 1.000 .974 .947 .889 .824 .750	.957 .930 .872 .807 .734 .652 .558 .450 .324 .176 .092 .966 .939 .881 .816 .742	1.018 1.018 1.019 1.020 1.022 1.023 1.025 1.027 1.029 1.031 1.033 1.008 1.009 1.009 1.010 1.010
.95 .90 .80 .70 .60 .50 .40 .30 .20 .10 .05 .100 .95 .90 .80 .70 .60	1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.200 1.200 1.200 1.200 1.200 1.200 1.200	.974 .947 .889 .824 .750 .667 .571 .462 .333 .182 .095 1.000 .974 .947 .889 .824 .750 .667	.957 .930 .872 .807 .734 .652 .558 .450 .324 .176 .092 .992 .966 .939 .881 .816 .742 .659	1.018 1.018 1.019 1.020 1.022 1.023 1.025 1.027 1.029 1.031 1.033 1.008 1.009 1.009 1.010 1.010 1.011
.95 .90 .80 .70 .60 .50 .40 .30 .20 .10 .05 .100 .95 .90 .80 .70 .60 .50	1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.200 1.200 1.200 1.200 1.200 1.200 1.200 1.200	.974 .947 .889 .824 .750 .667 .571 .462 .333 .182 .095 1.000 .974 .947 .889 .824 .750 .667 .571	.957 .930 .872 .807 .734 .652 .558 .450 .324 .176 .092 .992 .966 .939 .881 .816 .742 .659 .565	1.018 1.018 1.019 1.020 1.022 1.023 1.025 1.027 1.029 1.031 1.033 1.008 1.009 1.009 1.010 1.010 1.011 1.011
.95 .90 .80 .70 .60 .50 .40 .30 .20 .10 .05 .100 .95 .90 .80 .70 .60 .50 .40	1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.200 1.200 1.200 1.200 1.200 1.200 1.200 1.200 1.200 1.200	.974 .947 .889 .824 .750 .667 .571 .462 .333 .182 .095 1.000 .974 .947 .889 .824 .750 .667 .571	.957 .930 .872 .807 .734 .652 .558 .450 .324 .176 .092 .992 .966 .939 .881 .816 .742 .659 .565 .456	1.018 1.019 1.020 1.022 1.023 1.025 1.027 1.029 1.031 1.033 1.008 1.009 1.009 1.010 1.010 1.011 1.012 1.013
.95 .90 .80 .70 .60 .50 .40 .30 .20 .10 .05 .100 .95 .90 .80 .70 .60 .50 .40 .30 .20 .20 .20 .20 .20 .20 .20 .20 .20 .2	1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.200 1.200 1.200 1.200 1.200 1.200 1.200 1.200 1.200 1.200 1.200 1.200 1.200 1.200	.974 .947 .889 .824 .750 .667 .571 .462 .333 .182 .095 1.000 .974 .947 .889 .824 .750 .667 .571 .462 .333	.957 .930 .872 .807 .734 .652 .558 .450 .324 .176 .092 .992 .966 .939 .881 .816 .742 .659 .565 .456 .329	1.018 1.018 1.019 1.020 1.022 1.023 1.025 1.027 1.029 1.031 1.033 1.008 1.009 1.009 1.010 1.010 1.011 1.012 1.013 1.014
.95 .90 .80 .70 .60 .50 .40 .30 .20 .10 .05 .100 .95 .90 .80 .70 .60 .50 .40	1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.300 1.200 1.200 1.200 1.200 1.200 1.200 1.200 1.200 1.200 1.200	.974 .947 .889 .824 .750 .667 .571 .462 .333 .182 .095 1.000 .974 .947 .889 .824 .750 .667 .571	.957 .930 .872 .807 .734 .652 .558 .450 .324 .176 .092 .992 .966 .939 .881 .816 .742 .659 .565 .456	1.018 1.019 1.020 1.022 1.023 1.025 1.027 1.029 1.031 1.033 1.008 1.009 1.009 1.010 1.010 1.011 1.012 1.013

Table 2. Continued

1.00	1.100	1.000	.998	1.002
.95	1.100	.974	.972	1.002
.90	1.100	.947	.945	1.002
.80	1.100	.889	.887	1.003
.70	1.100	.824	.821	1.003
.60	1.100	.750	.748	1.003
.50	1.100	.667	.665	1.003
.40	1.100	.571	.570	1.003
.30	1.100	.462	.460	1.003
.20	1.100	.333	.332	1.004
.10	1.100	.182	.181	1.004
.05	1.100	.095	.095	1.004
1.00	1.000	1.000	1.000	1.000
.95	1.000	.974	.974	1.000
.90	1.000	.947	.947	1.000
.80	1.000	.889	.889	1.000
.70	1.000	.824	.824	1.000
.60	1.000	.750	.750	1.000
.50	1.000	.667	.667	1.000
.40	1.000	.571	.571	1.000
.30	1.000	.462	.462	1.000
.20	1.000	.333	.333	1.000
.10	1.000	.182	.182	1.000
.05	1.000	.095	.095	1.000

Further, Figures 1 to 3 indicate that the Spearman-Brown formula's over-estimation tendencies become worse as the standard deviations for the two halves of a test become dissimilar and the correlation between the two halves moves into the moderate (i.e., > .30 < .70) and low ranges (i.e.,  $\leq .30$ ). Thus, in these circumstances, the use of the Flanagan-Rulon formula would provide the user with a more accurate estimation of the population  $\rho$ .

For example, in Figure 2, when the standard deviation ratio is a moderate 1.5 and the correlation between the two halves of a test is also a moderate .600, use of the Spearman-Brown formula yields an r = .750. The Flanagan-Rulon formula produces an r = .713,

or a discrepancy of nearly 4% showing a ratio of the Spearman-Brown being 1.052 times higher than the Flanagan-Rulon estimate. Thus, the Flanagan-Rulon formula in this case is the more accurate of the two in terms approximating the population p. Looking at Figure 3, when the standard deviation ratio is a large 1.9 and the correlation between the two halves of a test is a low .300, use of the Spearman-Brown formula yields an r = .462. The Flanagan-Rulon formula produces an r = .397, or an even more prominent discrepancy of 6.5% and a ratio of the Spearman-Brown formula yielding results 1.164 higher than the Flanagan-Rulon times estimation.

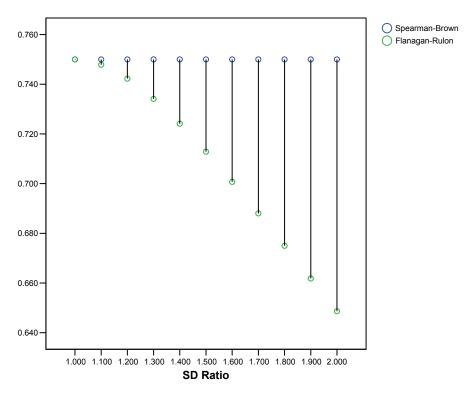


Figure 2. Example when  $r_{xy} = .600$  and SB = .750

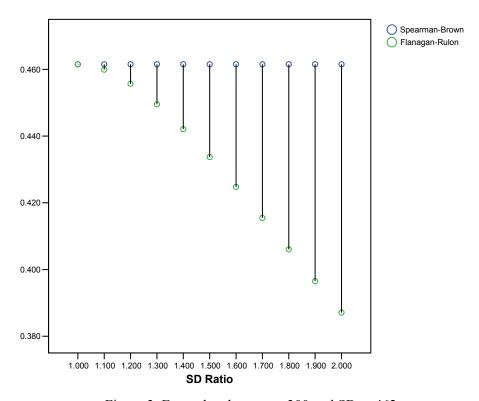


Figure 3. Example when  $r_{xy} = .300$  and SB = .462

## Application

The SPSS syntax found in the Appendix serves as a check on the variance parameter ratio range to determine which split half reliability formula to employ. The user types into the Begin Data section of the syntax the two standard deviation values for two halves of a test followed by the correlation between the two halves. The syntax is run and produces the following values:  $r_{xy}$ , SD<sub>1</sub>, SD<sub>2</sub>, the ratio of SD<sub>1</sub> to SD<sub>2</sub>, Spearman-Brown, Flanagan-Rulon, and the ratio of Spearman-Brown to Flanagan-Rulon. From these results, the user can determine if the ratio between the standard deviations of the two halves of a test are .9 to 1.1, which would also produce a Spearman-Brown to Flanagan-Rulon ratio < 1%, signifying use of the Spearman-Brown (i.e., no overestimation of the population  $\rho$ ). If the ratio range were beyond this threshold, the Spearman-Brown to Flanagan-Rulon ratio would be > 1%. which would indicate that the Flanagan-Rulon formula would be the more accurate estimator to use. Future research examining the ratio range of Spearman-Brown and Flanagan-Rulon formulas should include their performance with empirical data under biased distributional situations, with various sample sizes, and under an assortment of missing data conditions.

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```
Appendix. Syntax for Calculating Tables 1 and 2 or any SB or FR Value
***********************
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********************
DATA LIST LIST /sd1 sd2 (2f9.2) r (f9.3).
**NOTE: Below, insert the SD1 and SD2 values and the r value. **
BEGIN DATA
15 10 .95
14 10 .90
13 10 .80
12 10 .70
11 10 .60
10 10 .50
END DATA.
COMPUTE FR1 = (4*r)*(sd1)*(sd2).
COMPUTE FR2 = (sd1**2)+(sd2**2)+(2*r)*(sd1)*(sd2).
COMPUTE FR = FR1/FR2.
COMPUTE SBPF2 = (2*r)/(1+r).
COMPUTE SDRATIO = sd1/sd2.
COMPUTE RATIO = SBPF2/FR.
EXECUTE.
FORMAT FR TO RATIO (f9.3).
VARIABLE LABELS sdratio 'SD Ratio'ratio 'Ratio of SB to FR'/sbpf2 'Spearman-Brown'/r
'Correlation Between the Two Halves of a Test (rxy)'/sd1 'Standard Deviation for Test 1'/sd2 'Standard
Deviation for Test 2'/fr 'Flanagan-Rulon'/.
REPORT FORMAT=LIST AUTOMATIC ALIGN (LEFT)
MARGINS (*,120)
/VARIABLES= r sd1 sd2 sdratio sbpf2 fr ratio
 /TITLE "Comparison Between Spearman-Brown and Flanagan-Rulon".
```